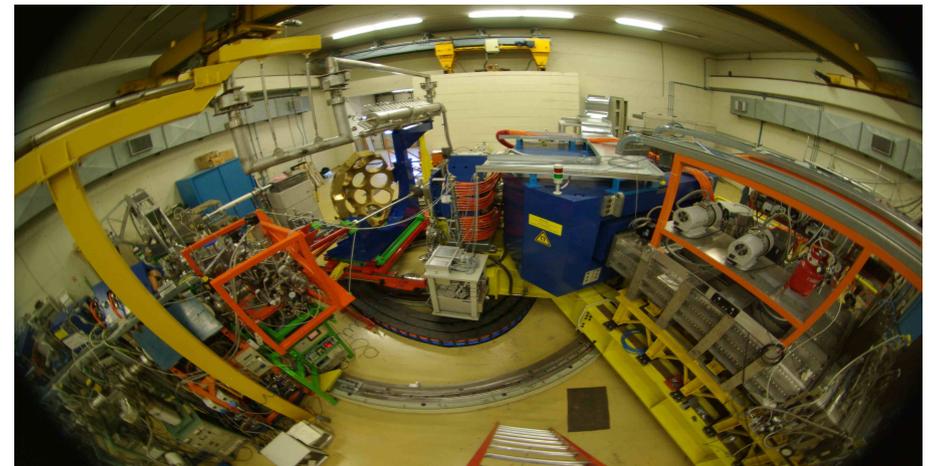
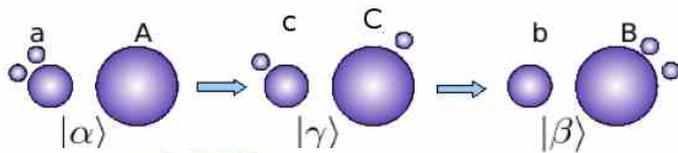
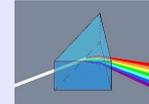
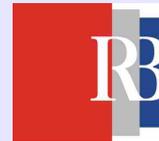


Recent studies of heavy ion transfer reactions using large solid angle magnetic spectrometers

Suzana Szilner
Ruđer Bošković Institute, Zagreb
PRISMA collaboration



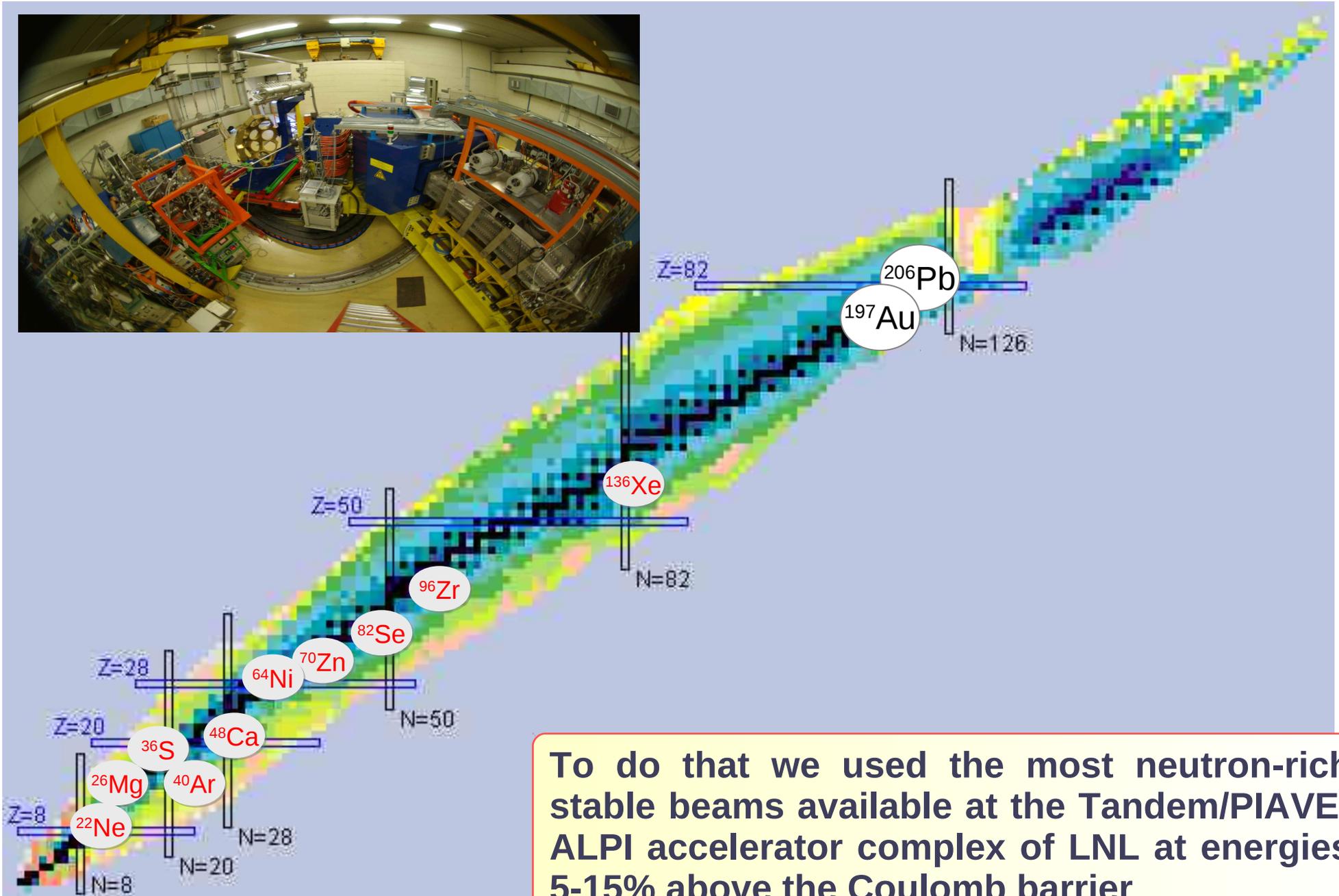
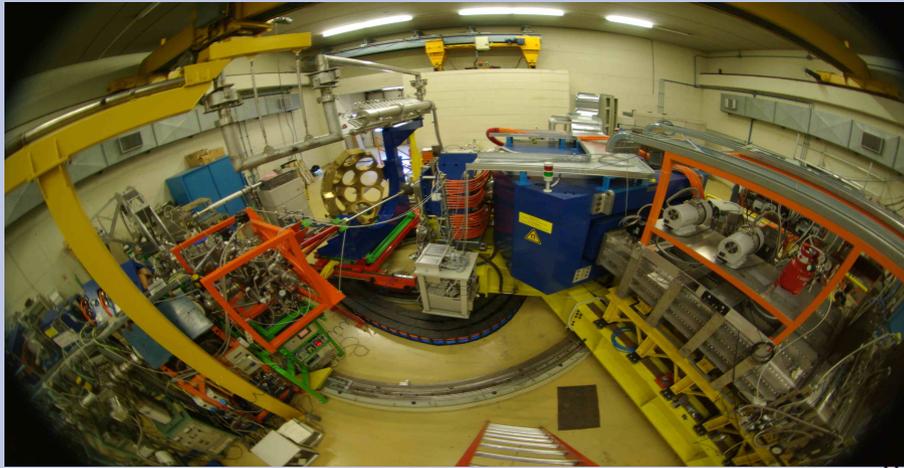
AFRICAN NUCLEAR PHYSICS CONFERENCE
(ANPC2021)



September 2021

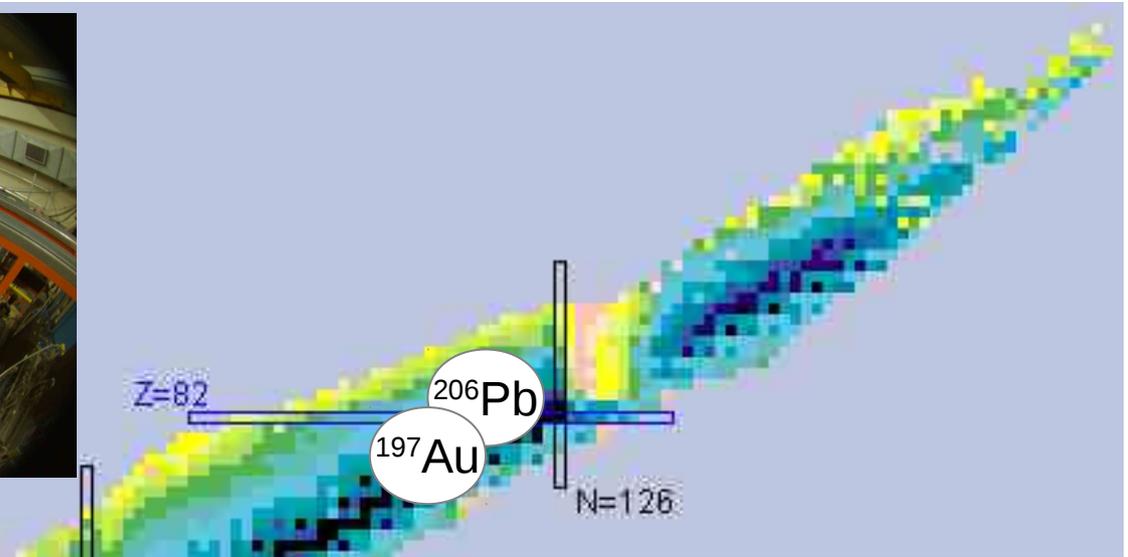
African Nuclear Physics Conference 2021

THE PRISMA + CLARA/AGATA CAMPAIGNS



To do that we used the most neutron-rich stable beams available at the Tandem/PIAVE-ALPI accelerator complex of LNL at energies 5-15% above the Coulomb barrier

THE PRISMA + CLARA/AGATA CAMPAIGNS



L. Corradi, G. Pollarolo, F. Galtarossa, A. Goasduff, D. Montanari, E. Fioretto, A.M. Stefanini, G. Montagnoli, G. Coucci, F. Scarlassara, J.J. Valiente-Dobon, D. Mengoni, G. de Angelis, A. Gottardo, T. Marchi, D. Testov...

A. Illana, L.P. Gaffney, Th. Kroll ...

J. Diklić, T. Mijatović, P. Čolović, D. Jelavić Malenica, N. Soić, N. Vukman, M. Milin

AGATA collaboration

Ruder Bošković Institute, Zagreb, Croatia

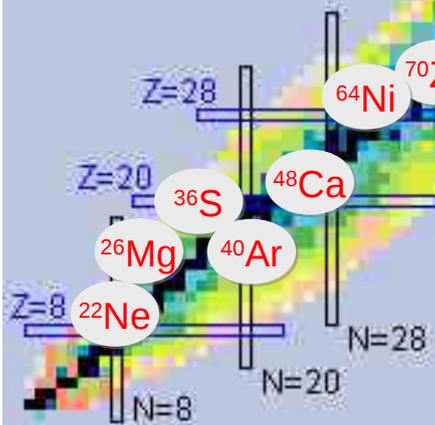
INFN - Laboratori Nazionali di Legnaro, Legnaro, Italy

INFN and Università di Torino, Italy

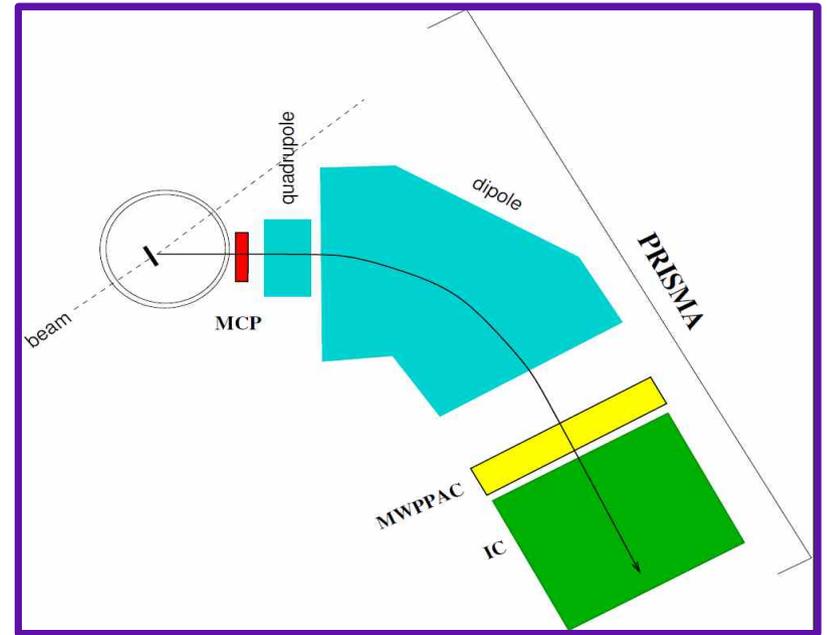
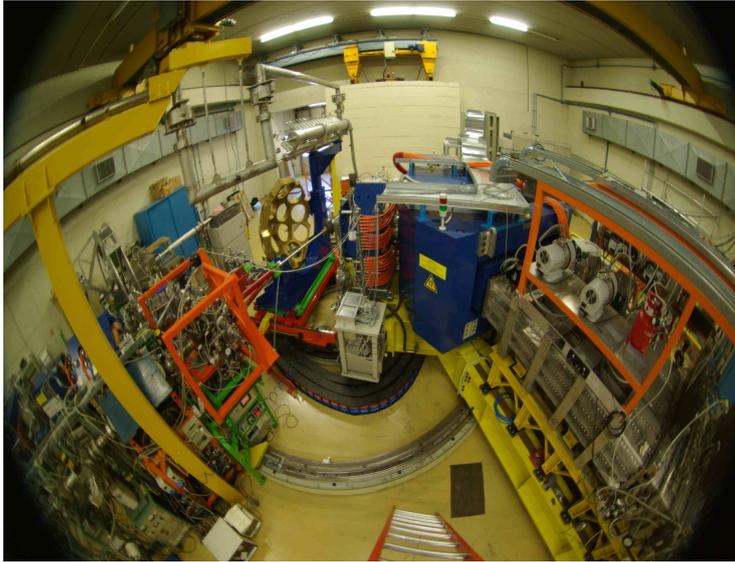
INFN and Università di Padova, Padova, Italy

University of Zagreb, Croatia

ISOLDE, CERN



Magnetic spectrometer PRISMA



magnets: quadrupole + dipole

detectors:

start detector: MCP – micro-channel plate

focal plane detectors: MWPPAC – multiwire parallel plate avalanche counter, IC – ionization chamber

PRISMA:

$\Omega \approx 80 \text{ msr}$ $B\rho_{\text{max}} = 1.2 \text{ Tm}$

$\Delta A/A \sim 1/200$

$\Delta Z/Z \sim 1/60$ for $Z=20$

E acceptance $\approx \pm 20\%$

position in MCP: X_i, Y_i

focal plane position: x_f, y_f

Time of Flight: $\text{ToF} = t_f - t_i$

energy loss, total energy: ΔE ,
E - IC



**event-by-event
trajectory
reconstruction**

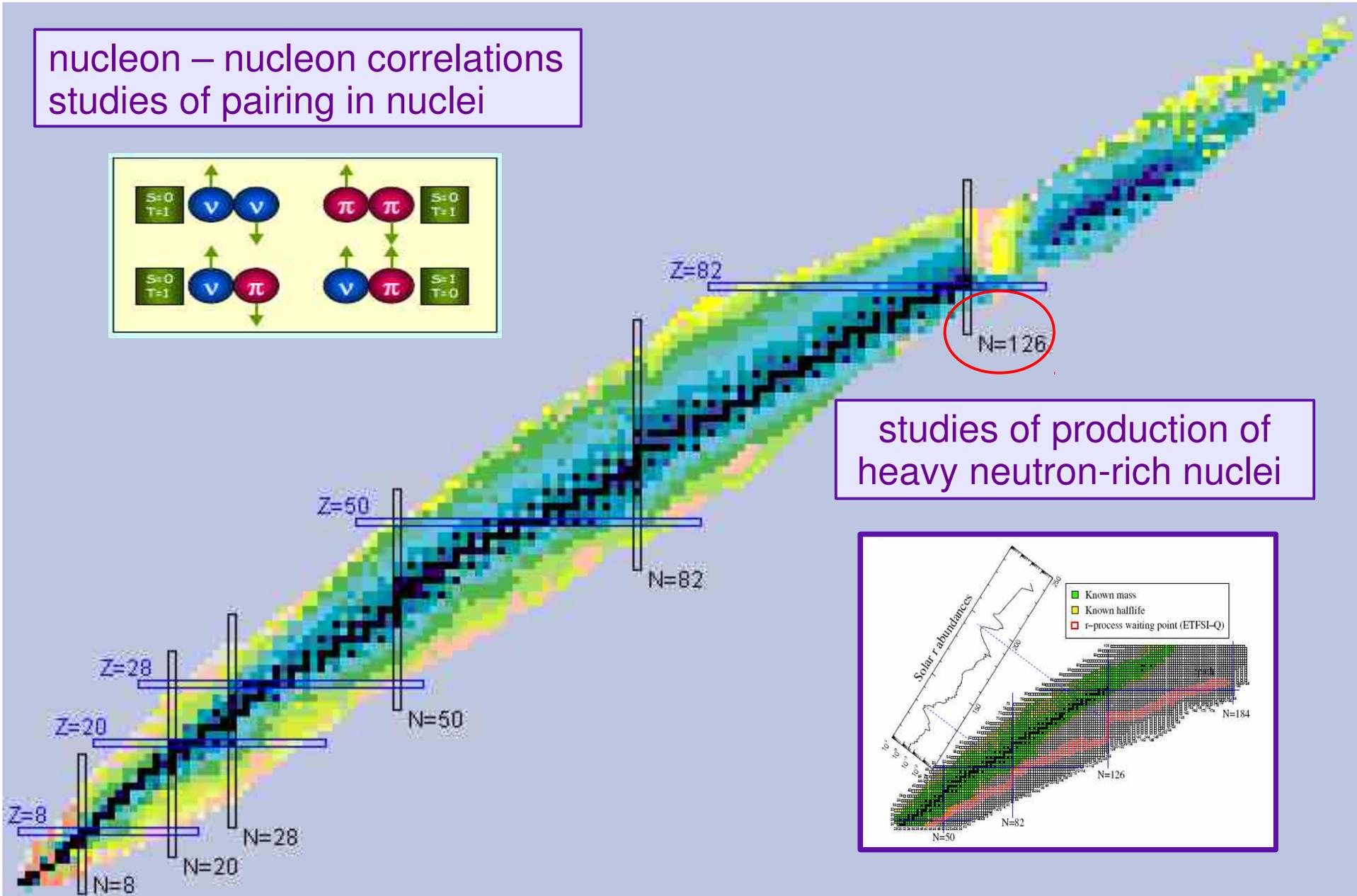
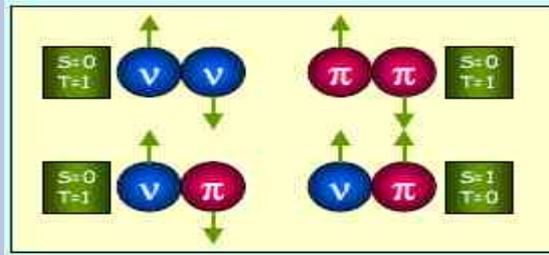


**A, q, Z, E, v
mass, charge,
atomic state,
energy, velocity**

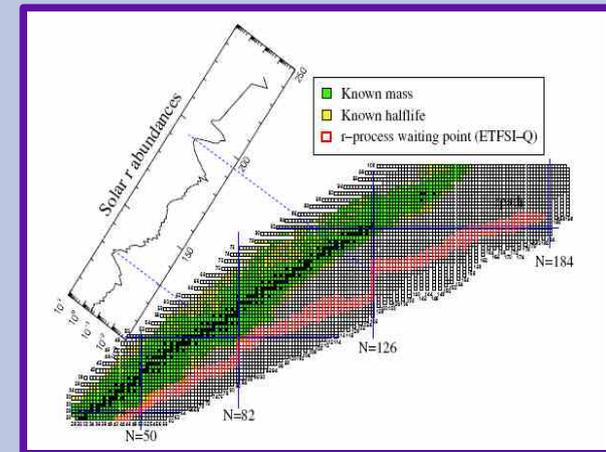
Heavy ion transfer reactions

Coulomb barrier energies

nucleon – nucleon correlations
studies of pairing in nuclei

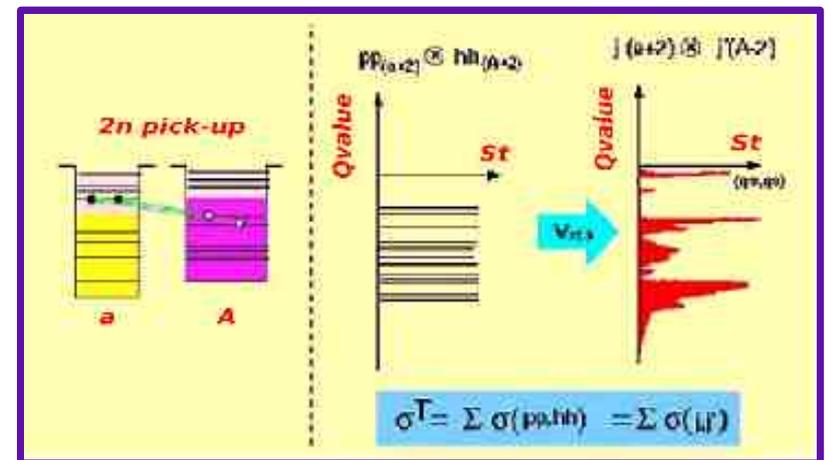
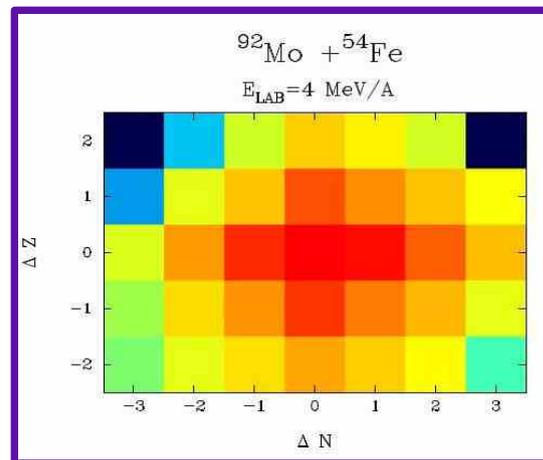
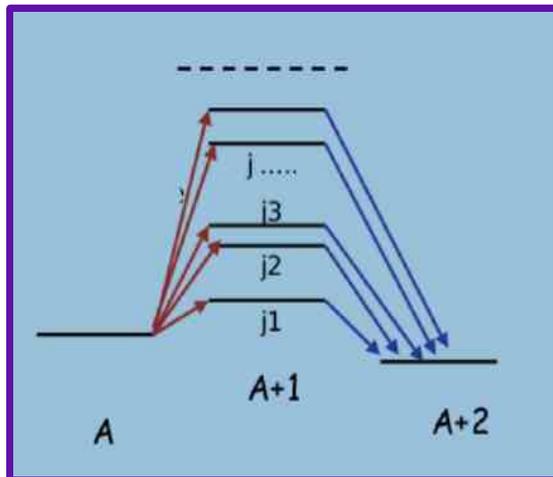


studies of production of
heavy neutron-rich nuclei



Probing nucleon-nucleon correlations in transfer reactions

The pairing interaction induces **particle-particle correlations** that are essential in defining the properties of finite quantum many body systems in their ground and neighboring states. These structure properties may influence in a significant way the evolution of the collision of two nuclei.



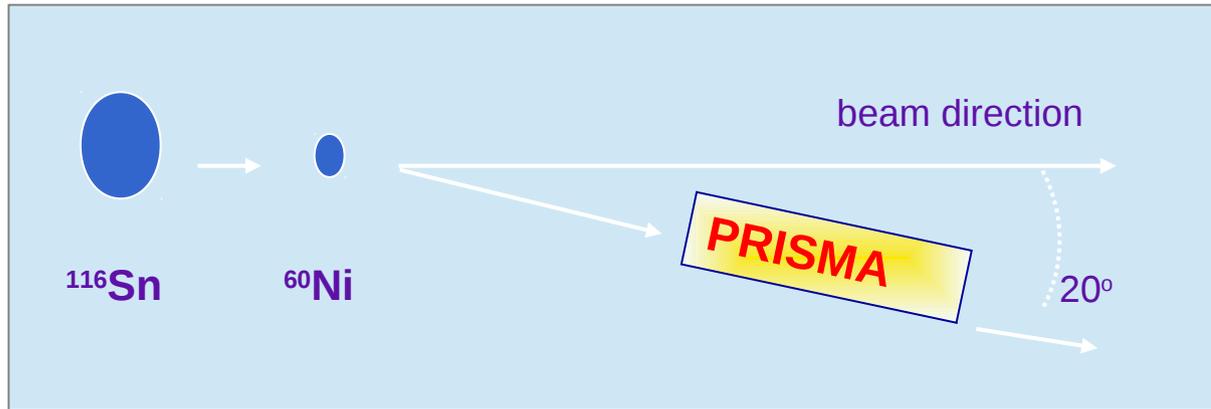
Heavy ion transfer reactions:

Advantages: test of correlation properties in transfer processes via simultaneous comparison of $\pm n$ and $\pm p$, and $\pm nn/\pm pp/\pm np$ pairs; transfer of “many” pairs

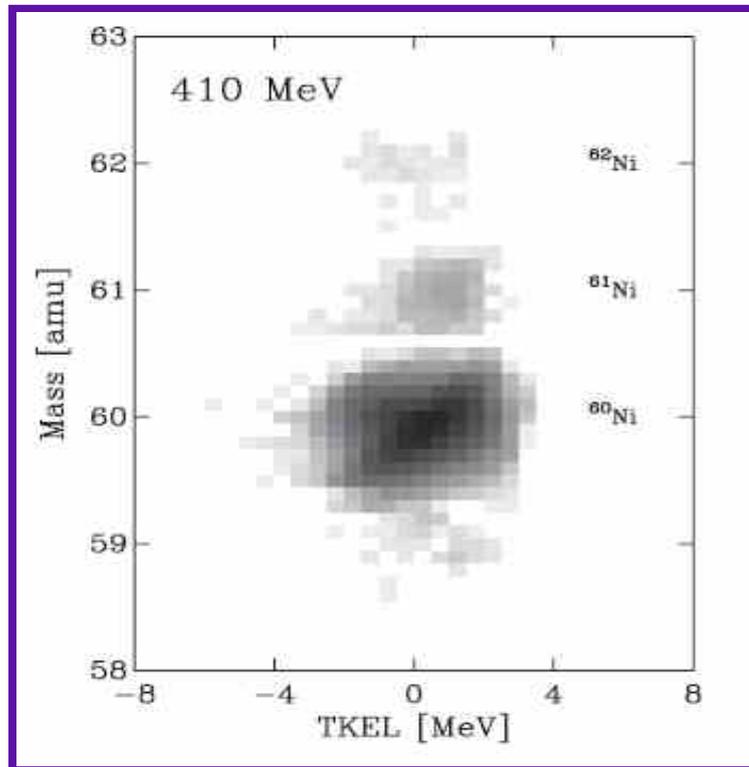
HI **drawbacks:** limited A,Z, energy resolutions (two-nucleon transfer \rightarrow redistribution of the strength around single particle states)



Nucleon-nucleon correlations studied with PRISMA



$^{116}\text{Sn}+^{60}\text{Ni}$, inverse kinematic, excitation function (detection of (lighter) target-like fragment in PRISMA:
 $E_{\text{beam}} = 500 \text{ MeV} - 410 \text{ MeV}$
($D \sim 12.3$ to 15.0 fm)



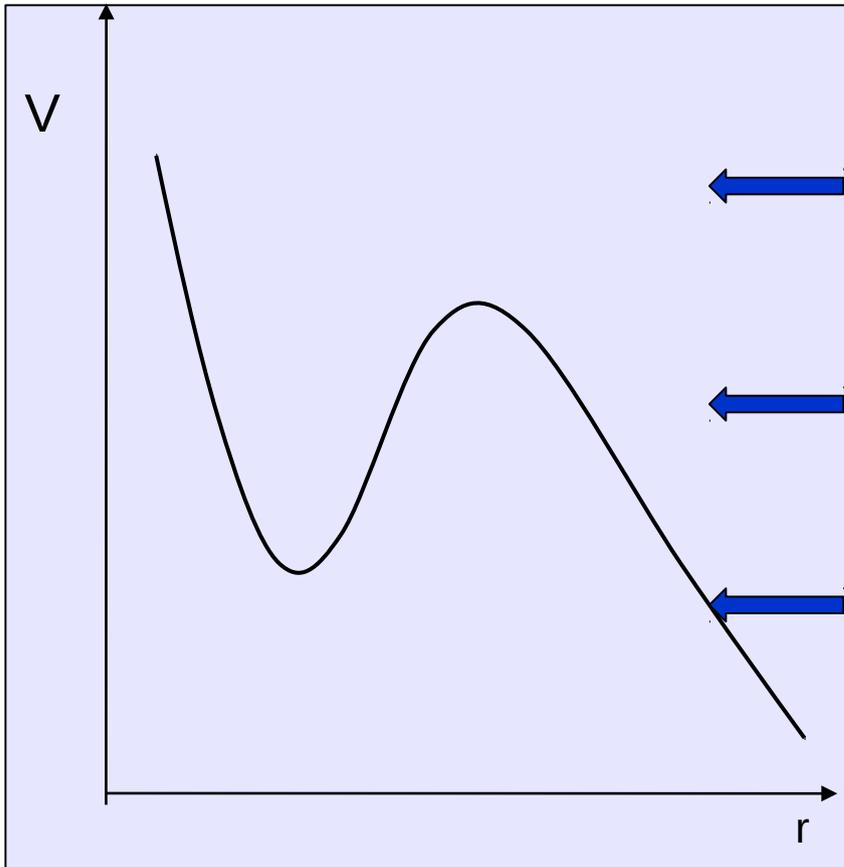
$^{96}\text{Zr}+^{40}\text{Ca}$, $^{116}\text{Sn}+^{60}\text{Ni}$, $^{92}\text{Mo}+^{54}\text{Fe}$, $^{206}\text{Pb}+^{116}\text{Sn}$
direct + inverse kinematic, PRISMA and
PRISMA+CLARA/AGATA/LaBr (7 experiments)

$^{96}\text{Zr}+^{40}\text{Ca}$: S. Szilner et al., Phys. Rev. C 76 (2007) 024604; L. Corradi et al., Phys. Rev. C 84 (2011) 034603

$^{116}\text{Sn}+^{60}\text{Ni}$: D. Montanari et al., Phys. Rev. Lett. 113 (2014) 052501; D. Montanari et al., Phys. Rev. C 93 (2016) 054623

Measurements below Coulomb barrier

A smooth transition between QE and DIC

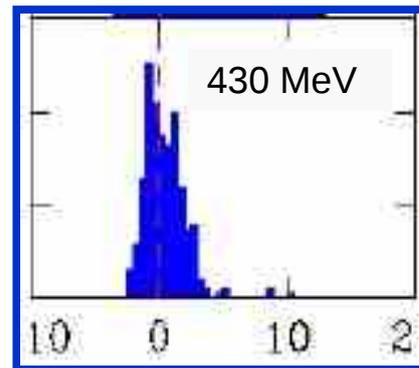
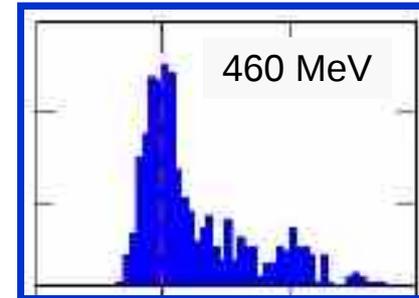
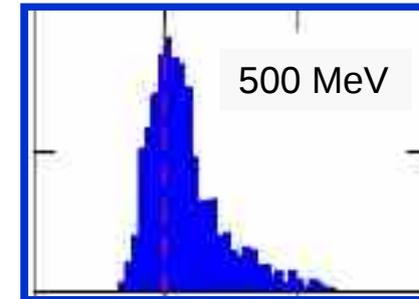


$$E > E_b$$

$$E \sim E_b$$

$$E < E_b$$

$$^{116}\text{Sn}(^{60}\text{Ni}, ^{62}\text{Ni})$$
$$Q_{\text{gs}} = +1.3 \text{ MeV}$$

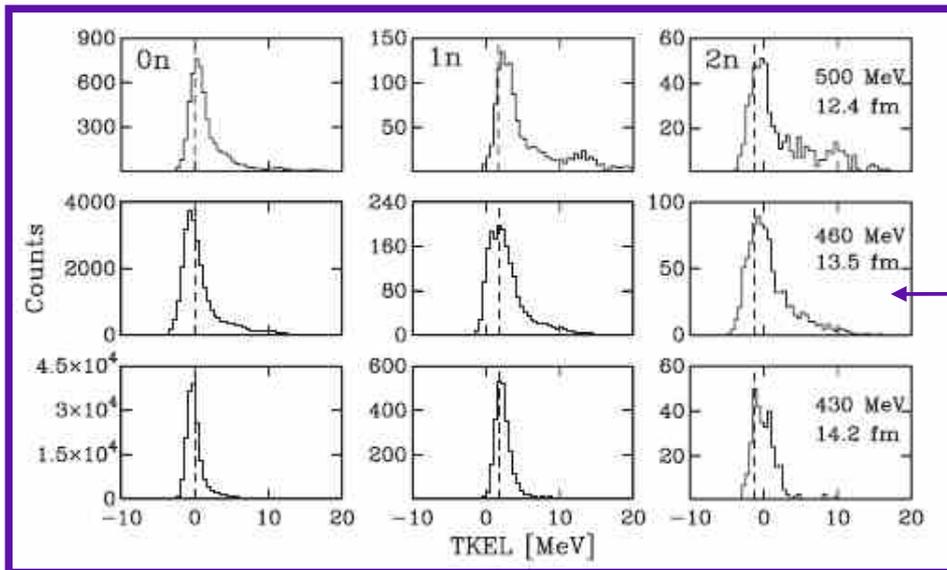


Below the barrier Q-values gets very narrow and without DIC components:

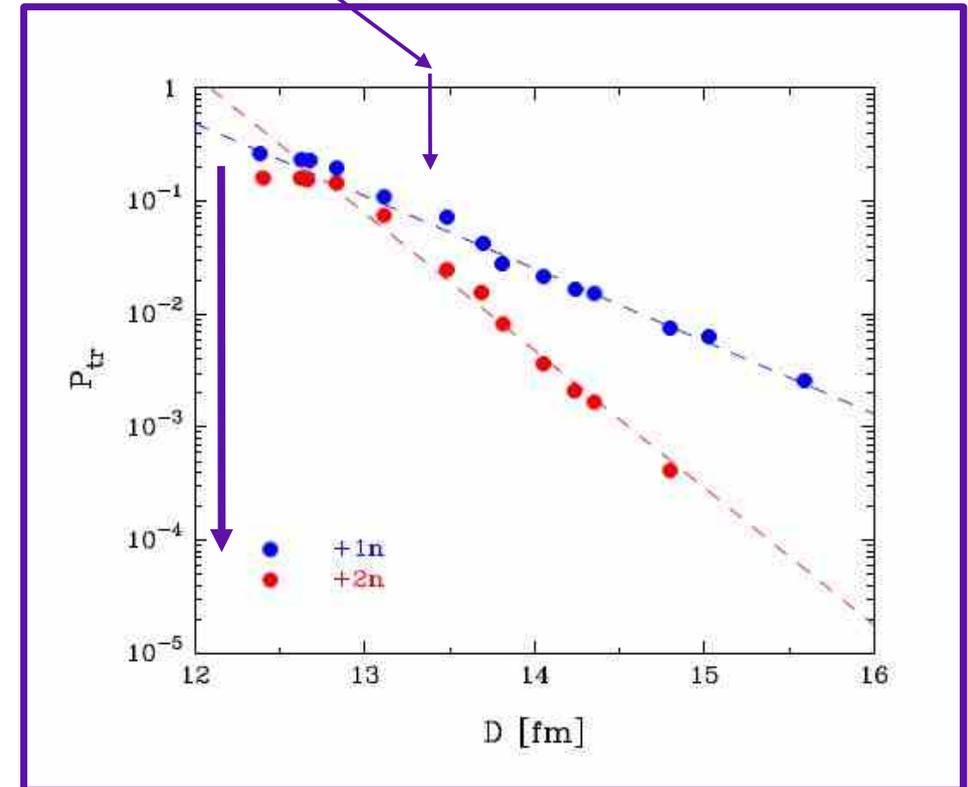
- 1) $E > E_b$, large number of open channels, DIC components / evaporation effects
- 2) $E < E_b$, narrow Q-value distributions (concentrated at "one state")

$^{116}\text{Sn} + ^{60}\text{Ni}$: neutron pair transfer far below the Coulomb barrier

Transfer strength very close to the g.s. to g.s. transitions



Coulomb barrier



D. Montanari et. al., Phys. Rev. Lett. 113 (2014) 052501

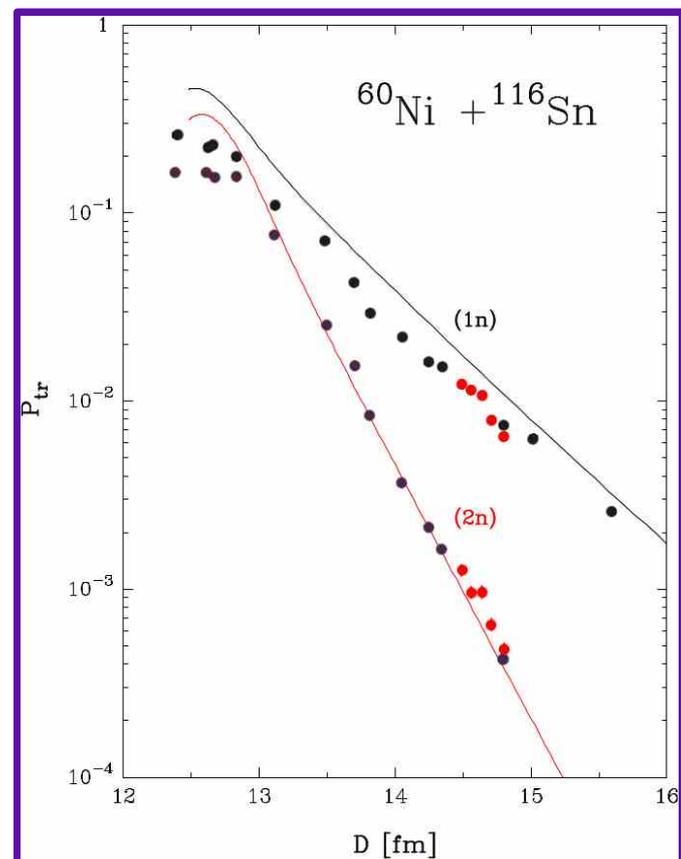
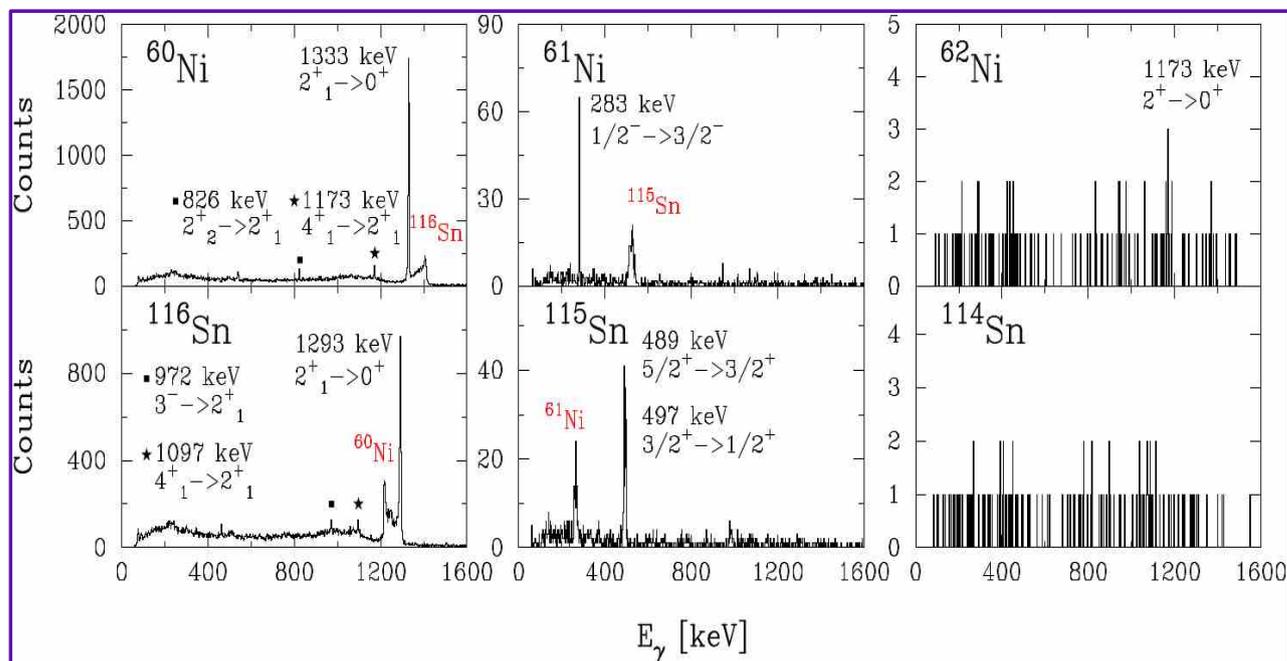
$$P_{tr} = \frac{d\sigma_{tr}}{d\sigma_{Ruth}}$$

$$D = \frac{Z_a Z_A e^2}{2E_{c.m.}} \left(1 + \frac{1}{\sin(\theta_{c.m.}/2)} \right)$$

$^{60}\text{Ni} + ^{116}\text{Sn}$, $^{40}\text{Ca} + ^{96}\text{Zr}$, $^{54}\text{Fe} + ^{92}\text{Mo}$: fragment - gamma measurements (PRISMA+CLARA/AGATA/LaBr)

$^{60}\text{Ni} + ^{116}\text{Sn}$: angular distributions measurement in “direct” kinematic:
 $E_{\text{beam}} = 245 \text{ MeV}$ at 70° ($D \sim 14.5 \text{ fm}$)

$$D = \frac{Z_a Z_A e^2}{2E_{\text{c.m.}}} \left(1 + \frac{1}{\sin(\theta_{\text{c.m.}}/2)} \right)$$



$^{60}\text{Ni} + ^{116}\text{Sn}$, $^{40}\text{Ca} + ^{96}\text{Zr}$, $^{54}\text{Fe} + ^{92}\text{Mo}$: fragment - gamma measurements (PRISMA+CLARA/AGATA/LaBr)

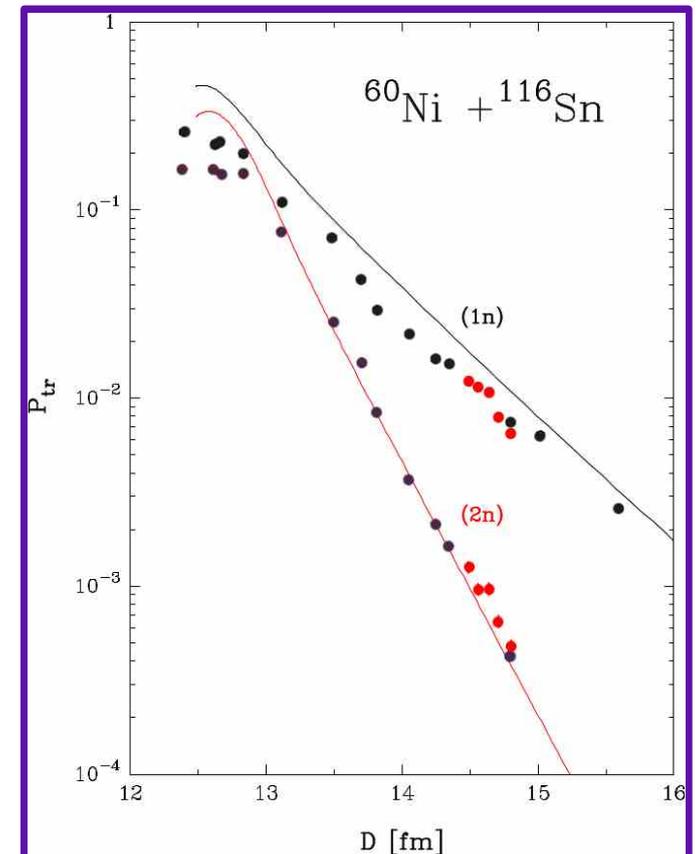
The strengths (normalized to $2^+ \rightarrow 0^+$ in ^{60}Ni) of the most important transitions are compared with a reaction code (DWBA, CC, SF) \rightarrow a direct check on the one-particle form factors (1n), and of the potential

(2n): $\sigma_{g.s.} = \sigma_{\text{tot}} - \sigma_{\text{exc}}$ \rightarrow the transitions to the excited states contribute to the total strength: $<24\%$, **dominant population of the ground states**

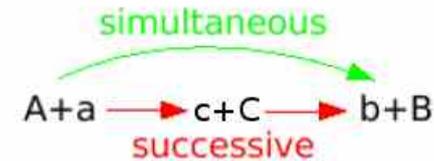
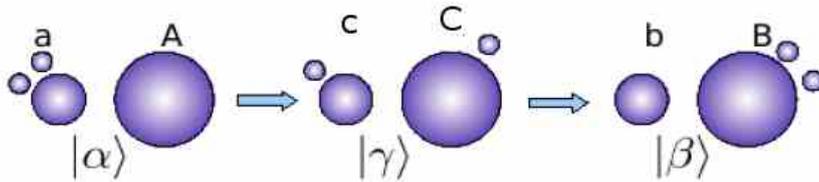
$$D = \frac{Z_a Z_A e^2}{2E_{\text{c.m.}}} \left(1 + \frac{1}{\sin(\theta_{\text{c.m.}}/2)} \right)$$

	Experiment	Theory
$^{116}\text{Sn}(2^+)$	0.792 ± 0.160	0.720
$^{116}\text{Sn}(4_1^+)$	0.042 ± 0.011	0.056
$^{60}\text{Ni}(4_1^+)$	0.060 ± 0.013	0.11
$^{115}\text{Sn}(5/2^+)$	0.018 ± 0.003	0.037
$^{61}\text{Ni}(1/2^-)$	0.014 ± 0.003	0.033
$^{62}\text{Ni}(2^+)$	< 0.00145	-

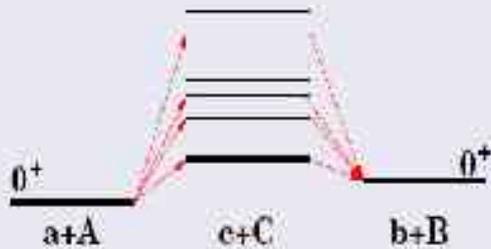
E_γ [keV]



$^{116}\text{Sn} + ^{60}\text{Ni}$: two particle transfer (semiclassical theory, microscopic calculations, 2nd order Born app.)



$$c_{\beta}(l) = c_{\beta}^{(1)} + c_{\beta}^{ort} + c_{\beta}^{succ}$$



	nlj
^{116}Sn	$1g_{9/2}$
	$2d_{5/2}$
	$1g_{7/2}$
	$3s_{1/2}$
	$2d_{3/2}$
	$1h_{11/2}$
	$2f_{7/2}$
^{60}Ni	$3p_{3/2}$
	$2p_{3/2}$
	$2p_{1/2}$
	$1f_{5/2}$
	$1g_{9/2}$

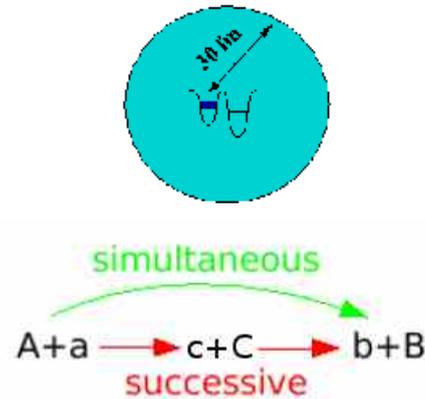
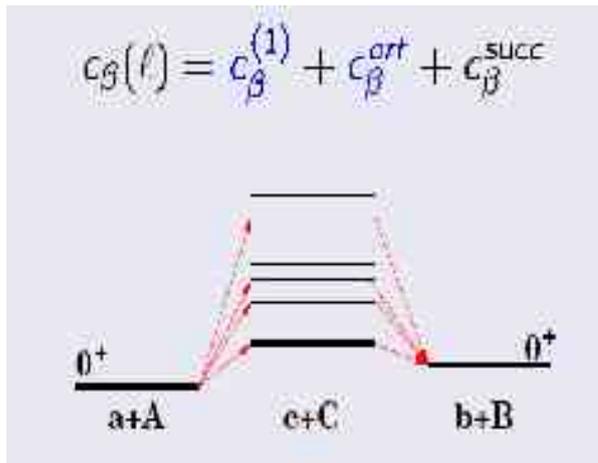
3 terms : simultaneous, orthogonal and successive

only the successive term contributes to the transfer amplitude (simultaneous component is canceled out by the nonorthogonality correction)

Only $0+$ to $0+$ transitions are included (BCS).

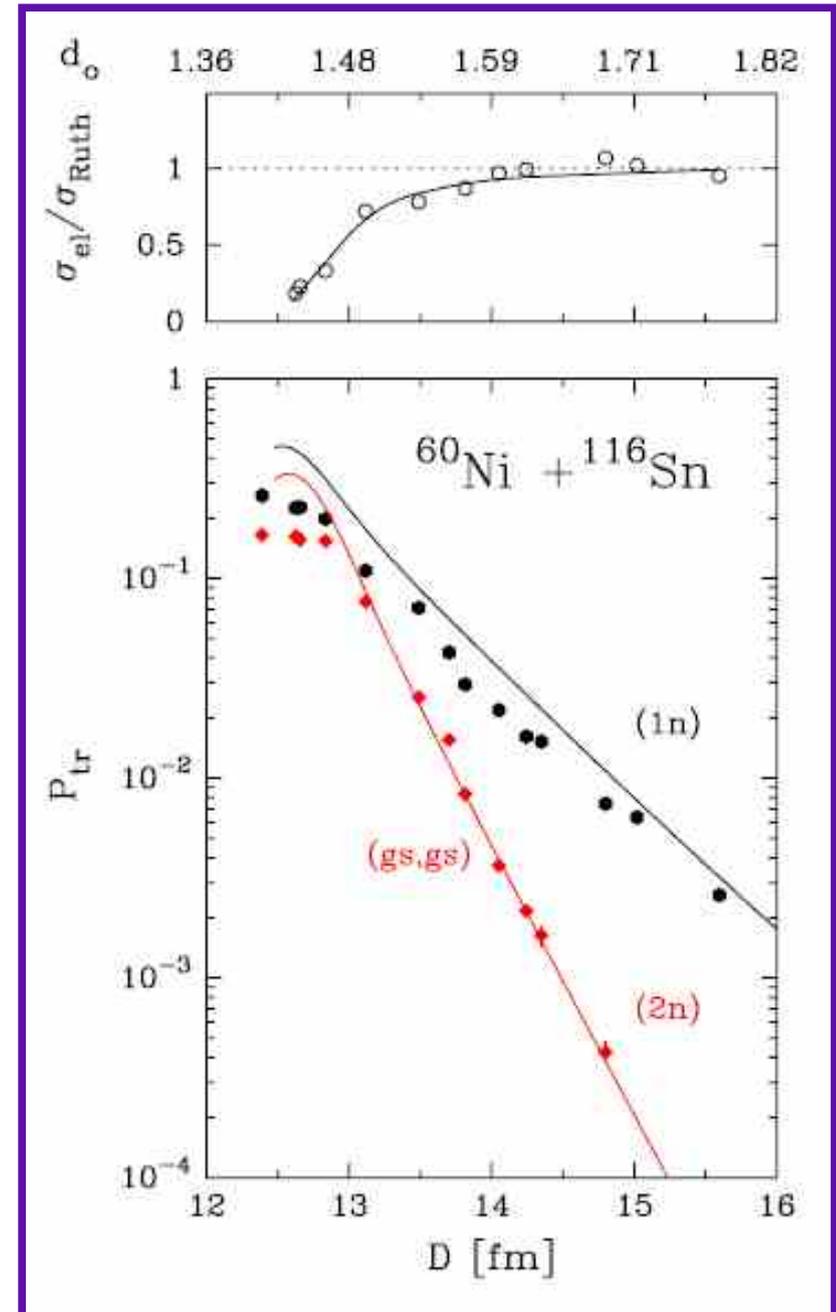
$$\begin{aligned}
 (c_{\beta})_{succ} &= \frac{1}{\hbar^2} \sum_{a_1, a'_1} B^{(A)}(a_1 a_1; 0) B^{(a)}(a'_1 a'_1; 0) 2 \frac{(-1)^{j_1 + j'_1}}{\sqrt{(2j_1 + 1)} \sqrt{(2j'_1 + 1)}} \sum_{m_1, m'_1} (-1)^{m_1 + m'_1} \\
 &\times \int_{-\infty}^{+\infty} dt f_{m_1 m'_1}(\mathcal{R}) e^{i[(E_{\beta} - E_{\gamma})t + \delta_{\beta\gamma}(t) + \hbar(m'_1 - m_1)\Phi(t)]/\hbar} \\
 &\times \int_{-\infty}^t dt f_{-m_1 - m'_1}(\mathcal{R}) e^{i[(E_{\gamma} - E_{\alpha})t + \delta_{\gamma\alpha}(t) - \hbar(m'_1 - m_1)\Phi(t)]/\hbar}
 \end{aligned}$$

$^{60}\text{Ni} + ^{116}\text{Sn}$: neutron pair transfer far below the Coulomb barrier



The experimental transfer probabilities are well reproduced, in **absolute values** and in **slope** by **microscopic** calculations which incorporate nucleon-nucleon **correlations**:

- ✓ a consistent description of (1n) and (2n) channels
- ✓ the formalism for (2n) incorporates the contribution from both the **simultaneous** and **successive** terms (only the **ground-to-ground-state** transition has been calculated)
- ✓ character of pairing correlations manifests itself equally well in simultaneous and in successive transfers due to the correlation length



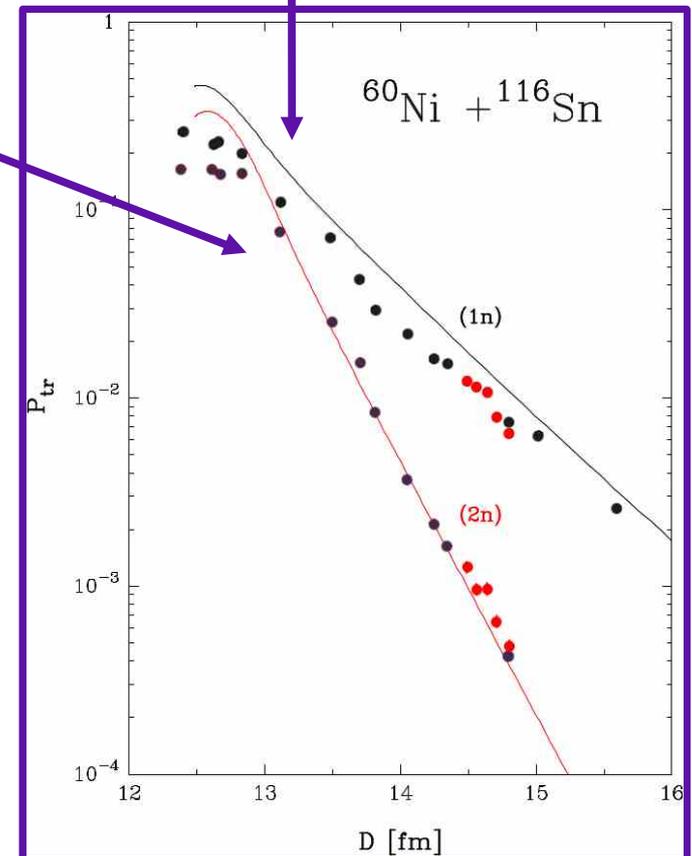
The Josephson effect in nuclear physics

For distances of closest approach compatible with the correlation length ξ the two nucleons behave like (quasi)bosons

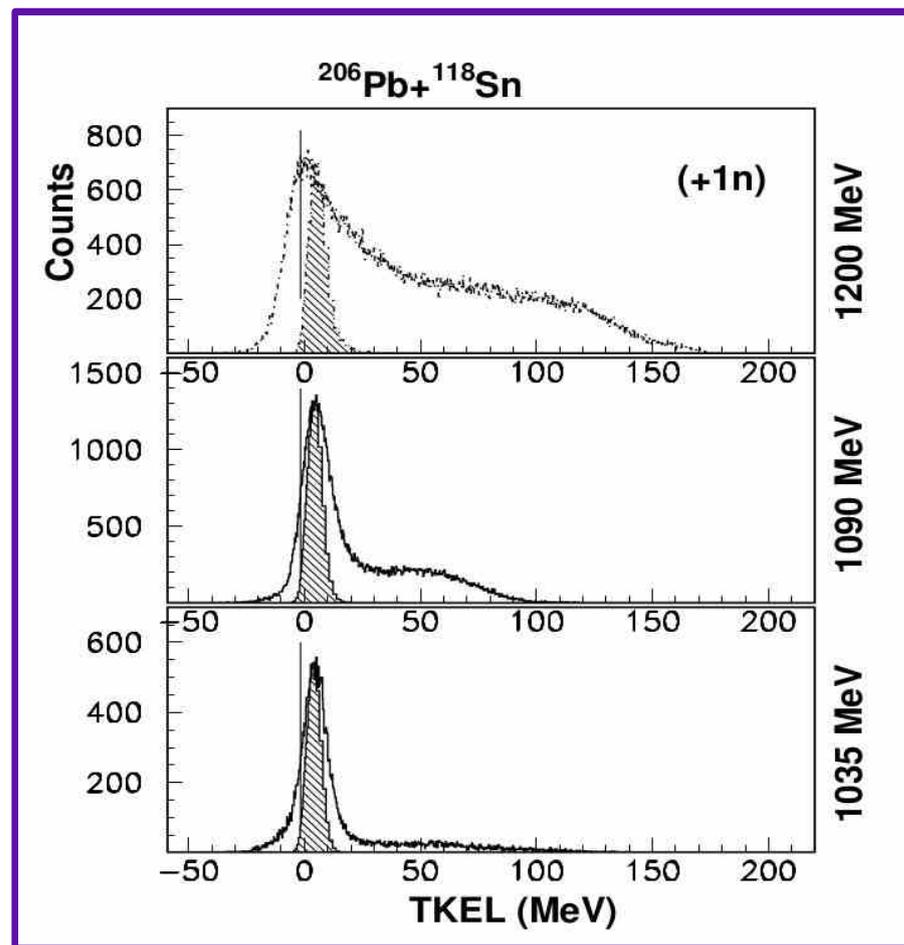
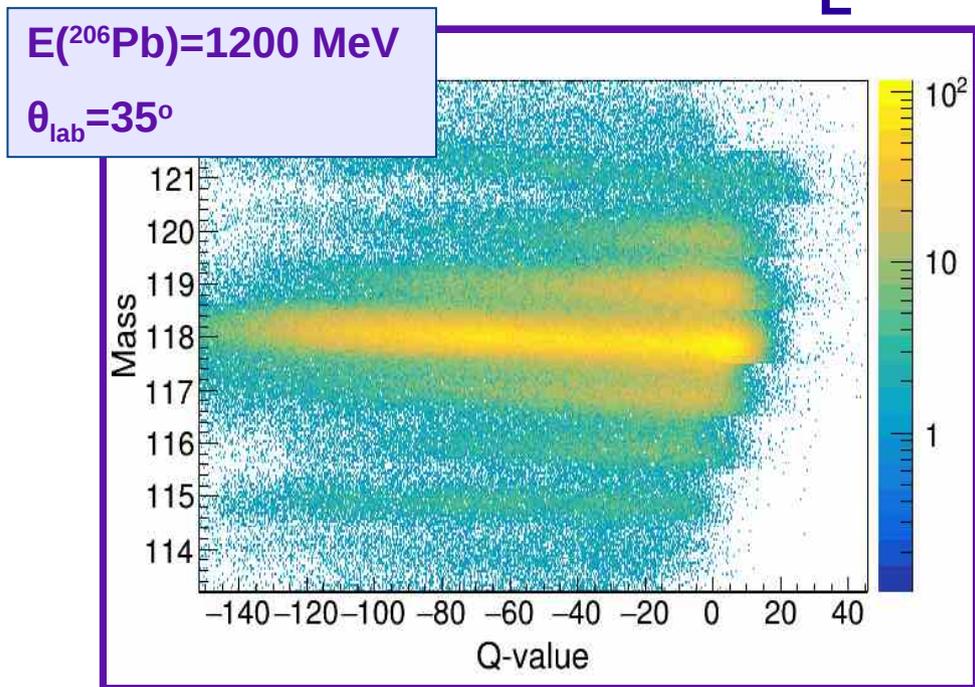
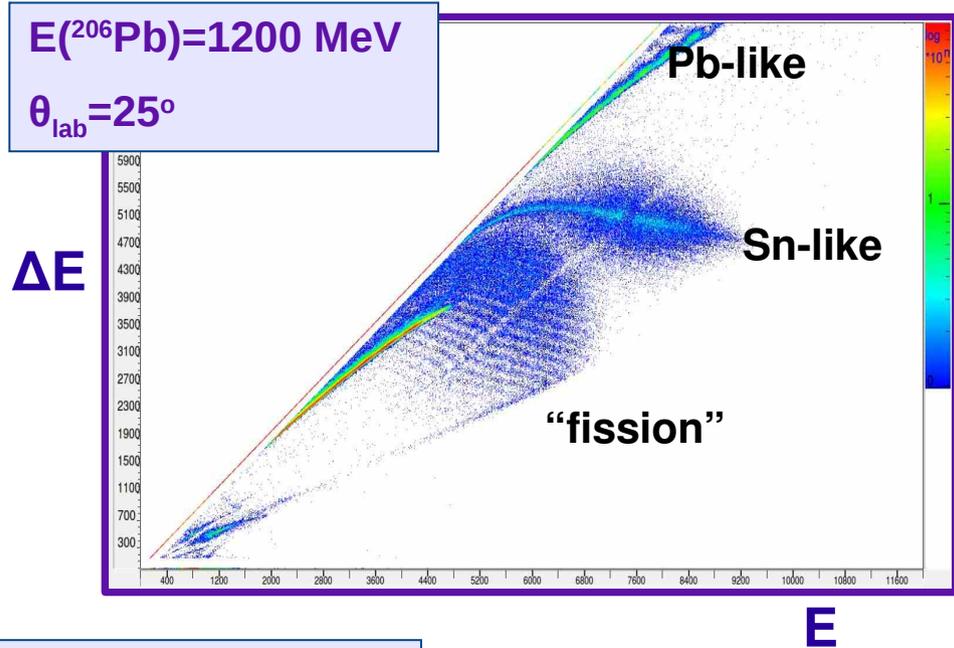
$$P_2 \approx P_1$$

At large distances of closest approach the Cooper pairs lose their (quasi)boson character and acquire a quasiparticle nature. One has a simple tunnelling of nucleons through the inner barrier

$$\xi = \frac{\hbar v_F}{\pi \Delta} \approx 13.5 \text{ fm}$$

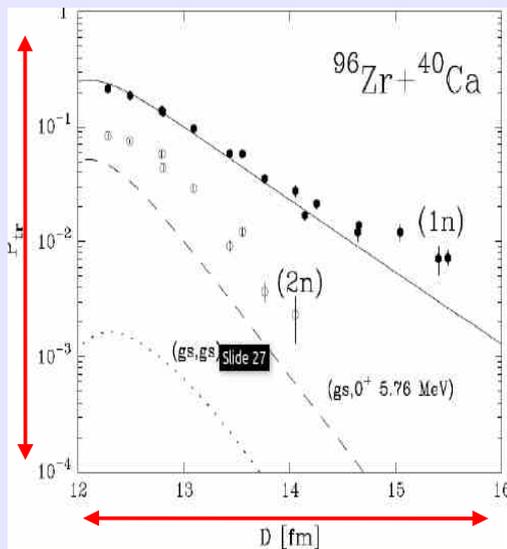


$^{206}\text{Pb} + ^{118}\text{Sn}$: complex reaction mechanism



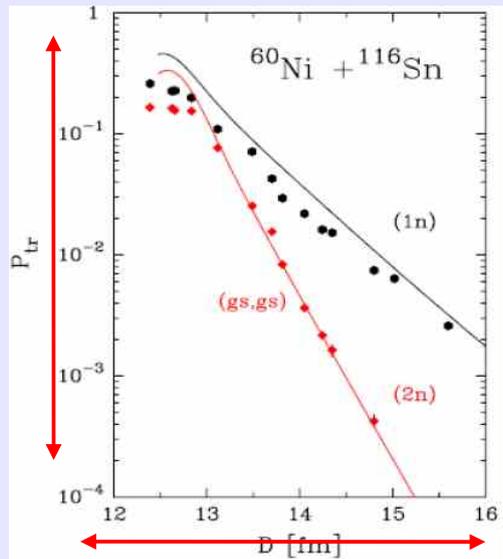
Nucleon transfer: exp. vs microscopic calculations

$^{96}\text{Zr} + ^{40}\text{Ca}$ ("closed shell")



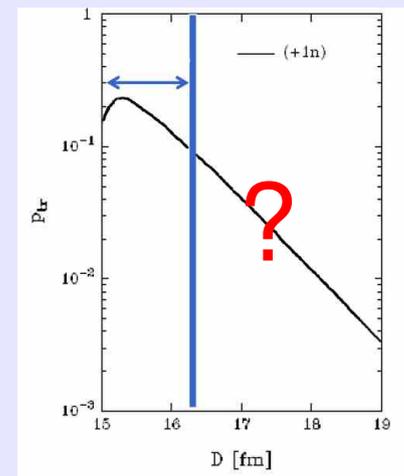
L. Corradi et al.,
PRC 84 (2011) 034603

$^{116}\text{Sn} + ^{60}\text{Ni}$ ("superfluid")

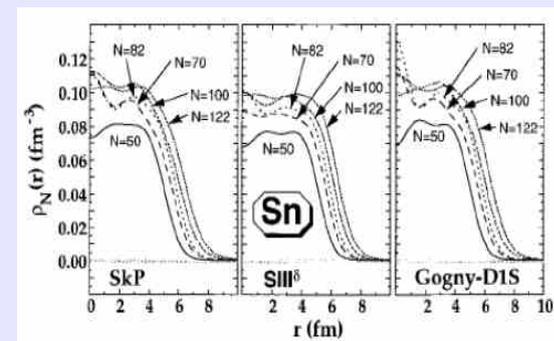


D. Montanari et al.,
PRL 113 (2014) 052501
PRC 93 (2016) 054623

$^{206}\text{Pb} + ^{118}\text{Sn}$ ("heavy")

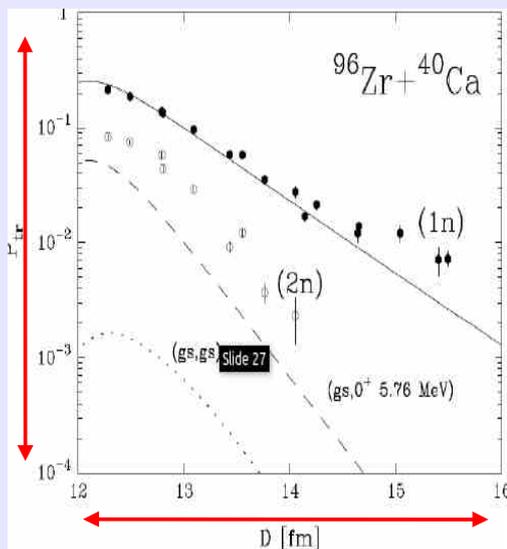


$^{132}\text{Sn} + ^{40}\text{Ca}, ^{64}\text{Ni}, ^{208}\text{Pb}$ ("neutron rich")

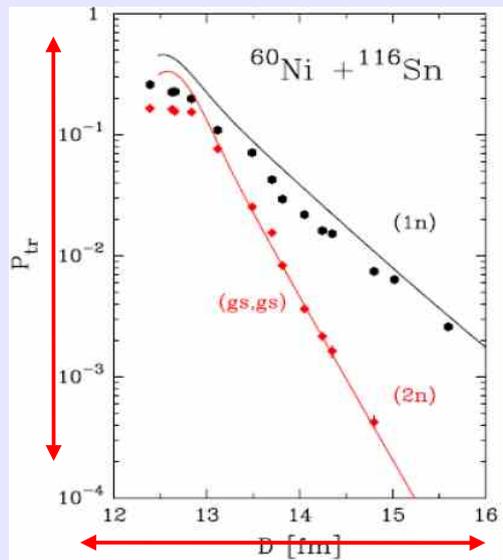


Nucleon transfer: exp. vs microscopic calculations

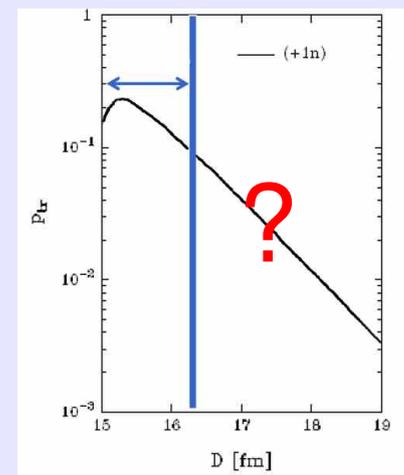
$^{96}\text{Zr} + ^{40}\text{Ca}$ ("closed shell")



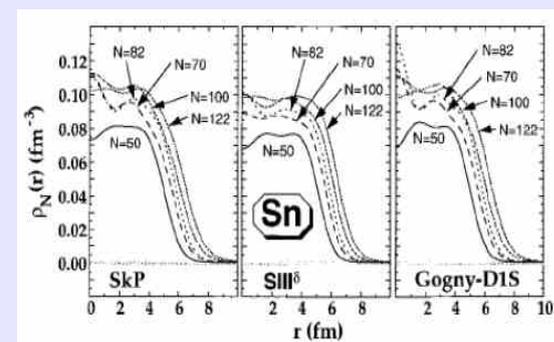
$^{116}\text{Sn} + ^{60}\text{Ni}$ ("superfluid")



$^{206}\text{Pb} + ^{118}\text{Sn}$ ("heavy")



$^{132}\text{Sn} + ^{40}\text{Ca}, ^{64}\text{Ni}, ^{208}\text{Pb}$ ("neutron rich")



informations about correlations are extracted when experimental **absolute cross sections** are compared with a **microscopic theory** which beside **correlations** includes also the coupling between relative motion (**reaction**) and intrinsic motion (**structure**).

Synthesis of heavy neutron rich nuclei in labs

Fusion by using neutron-rich radioactive beams → the intensity of the beams rather small (accelerators)

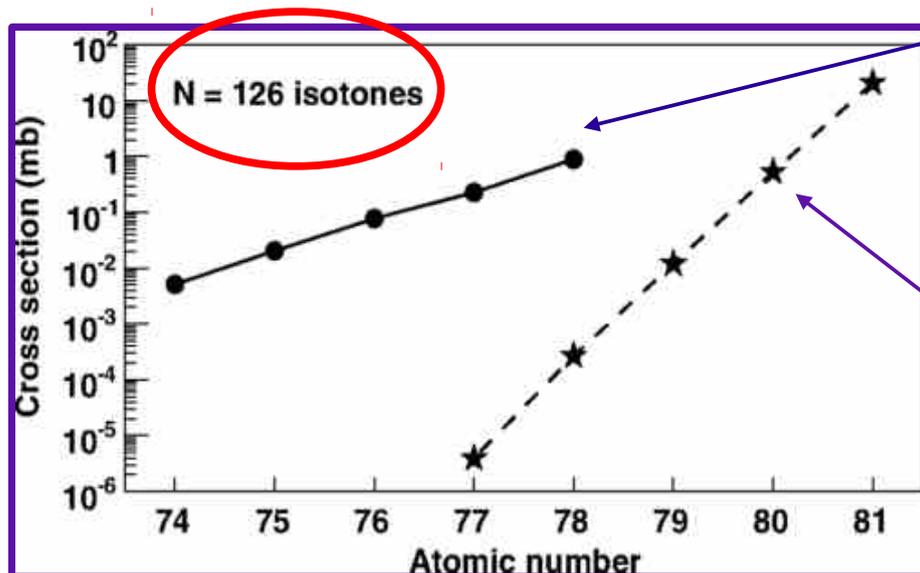
Neutron capture reaction → the intensity of the neutron beams is small (reactors)

relativistic energies : fragmentation reactions

energies close to the Coulomb barrier : multinucleon transfer reactions

→ cross sections ~ $\mu\text{b} - \text{nb}$

→ detection systems: large solid angle, large efficiency, large selectivity...

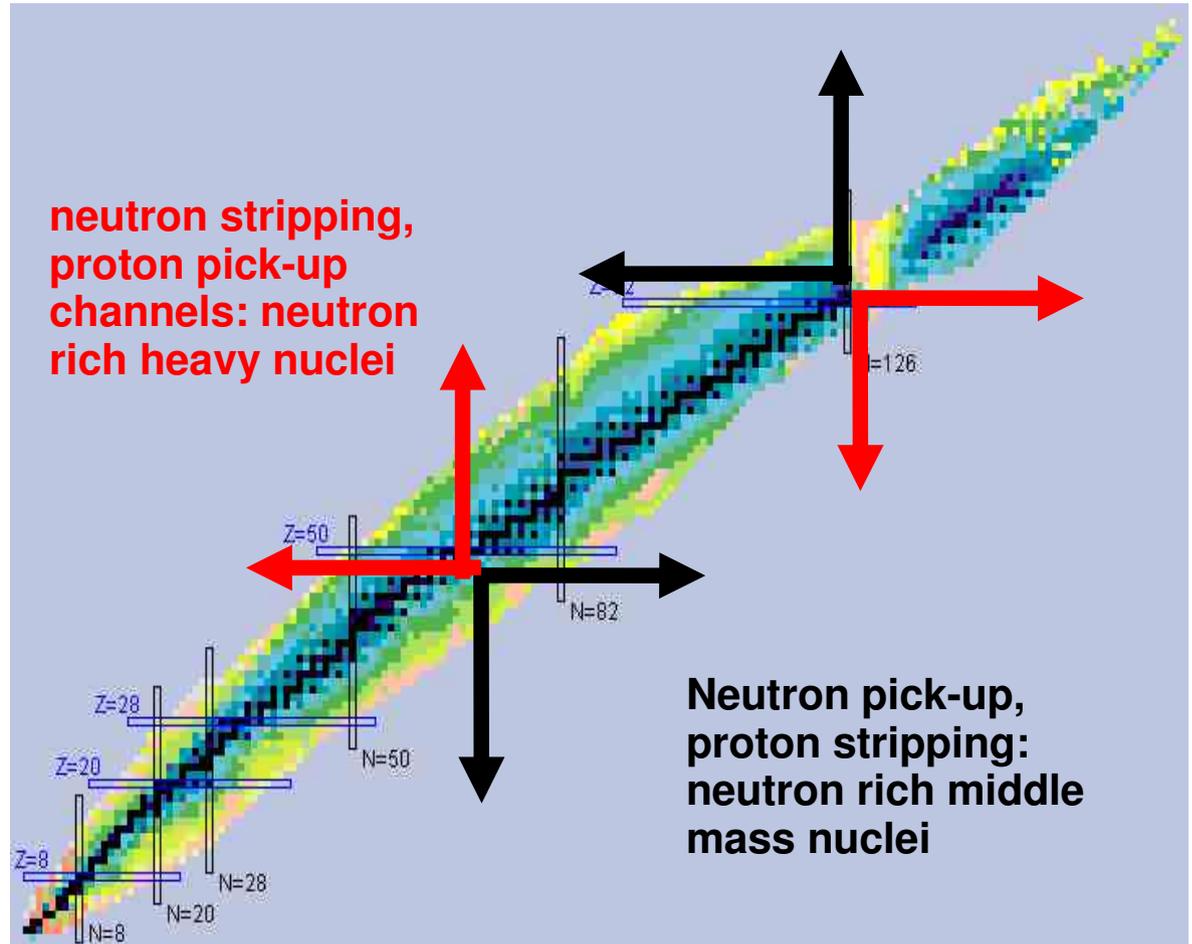
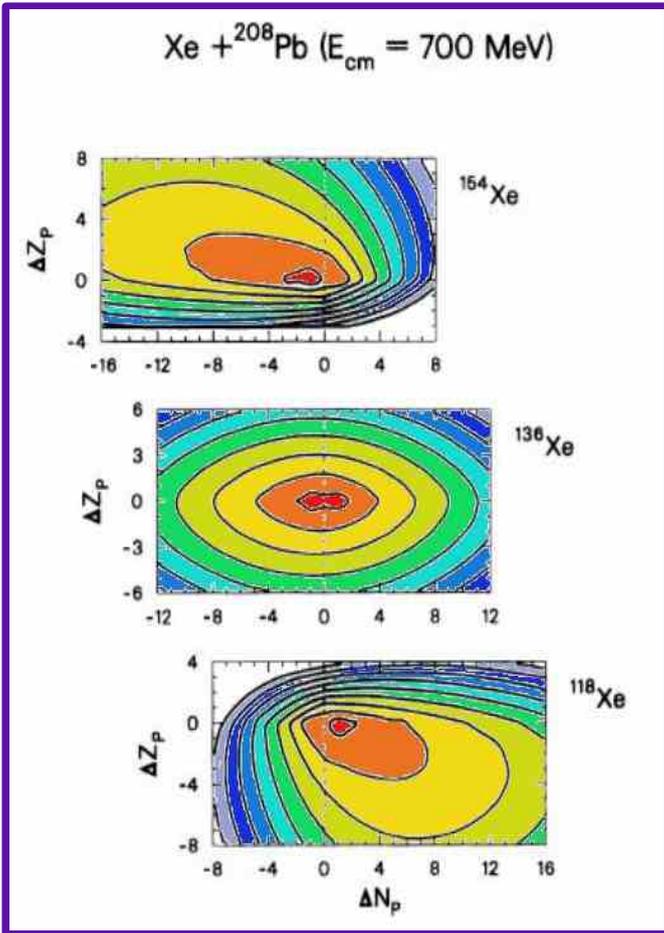


multinucleon transfer reactions:
 $^{136}\text{Xe} + ^{198}\text{Pt} @ E_{\text{lab}} = 8 \text{ MeV/A}$

fragmentation reactions:
 $^{208}\text{Pb} + ^9\text{Be} @ E_{\text{lab}} = 1 \text{ GeV/A}$

Y. Watanabe et al, Phys. Rev. Lett. 115 (2015) 172503, T. Kurtukian-Nieto et al., Phys. Rev. C 89 (2014) 024616.

Multinucleon transfer reactions



Xe ($Z=54$)

${}^{118}\text{Xe}$ ($T_{1/2} = 4$ min)

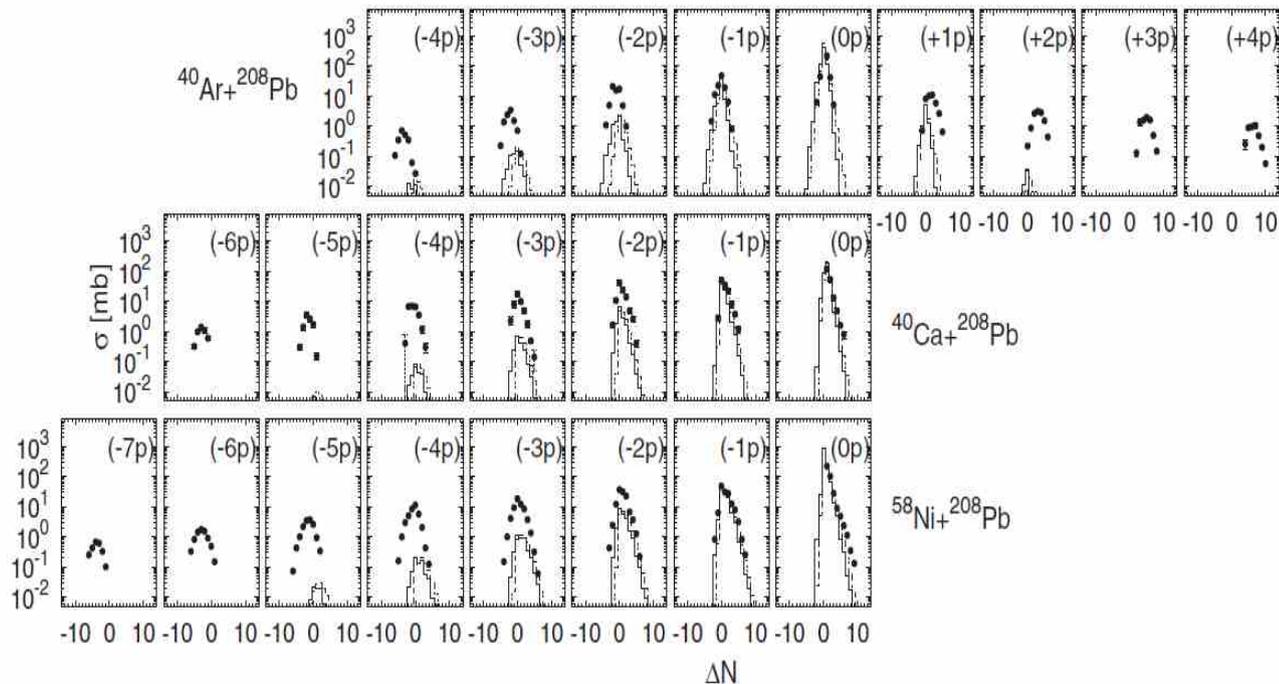
${}^{136}\text{Xe}$ (“the last” stable)

${}^{154}\text{Xe}$ (no information)

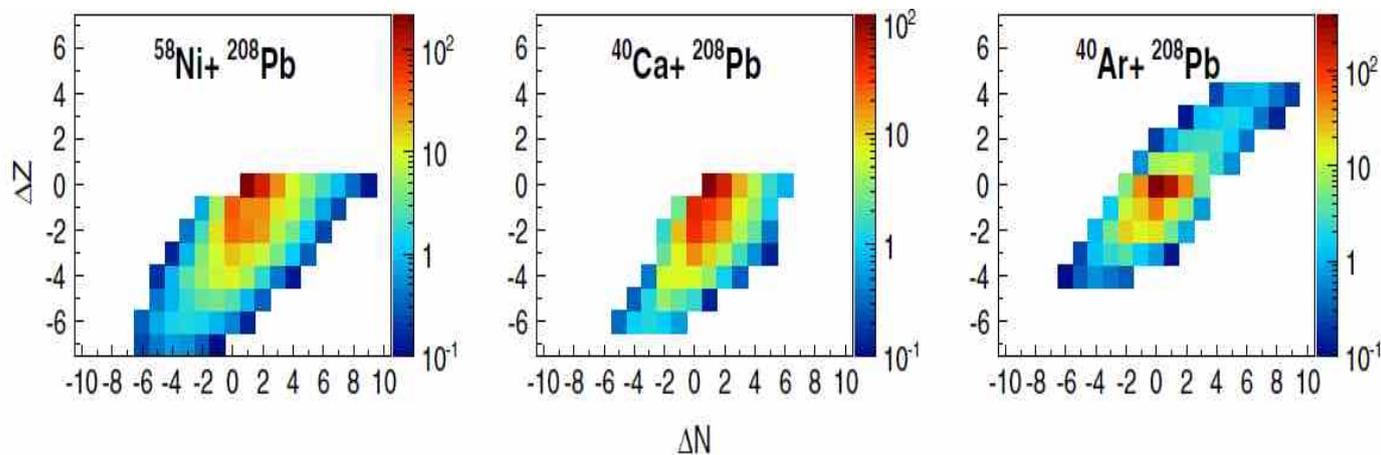
TH: C.H. Dasso, G. Pollaro and A. Winther, Phys. Rev. Lett. 73 (1994) 1907.

EXP: L. Corradi, G. Pollaro, S. Szilner, J. Phys. G 36 (2009) 113101 (Special Topic)

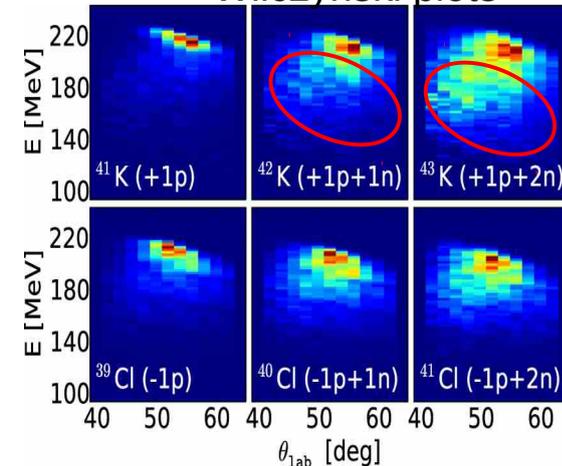
$^{40}\text{Ar}+^{208}\text{Pb}$, $^{40}\text{Ca}+^{208}\text{Pb}$, and $^{58}\text{Ni}+^{208}\text{Pb}$



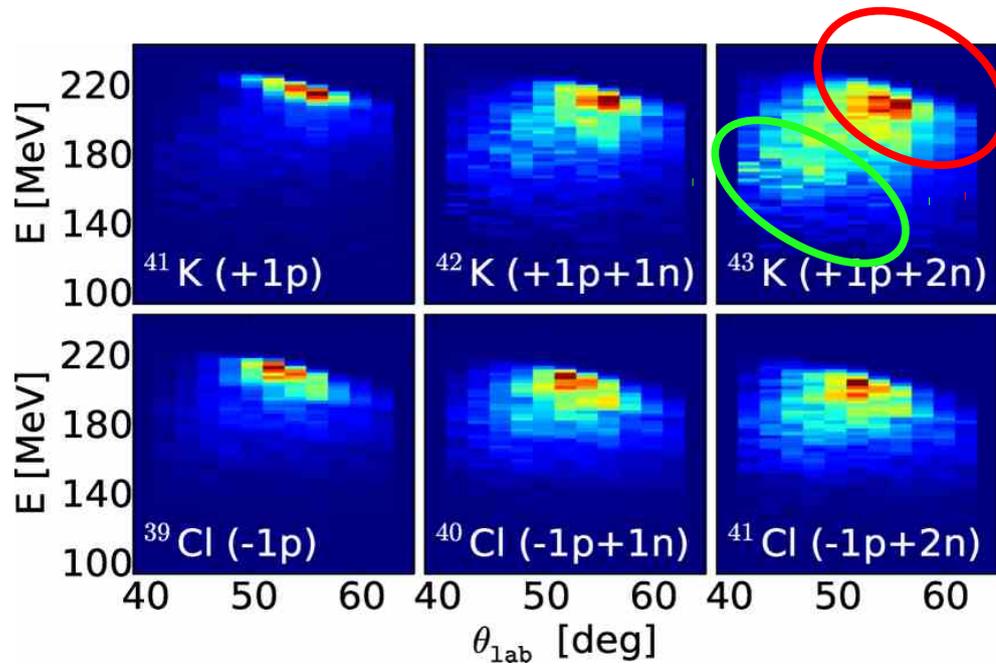
Above the barrier:
 → many open channels, transfer of 5-10 protons and neutrons governed by optimum Q-value
 → large TKEL, onset of **DIC** components
 → secondary processes: evaporation, transfer induced fission



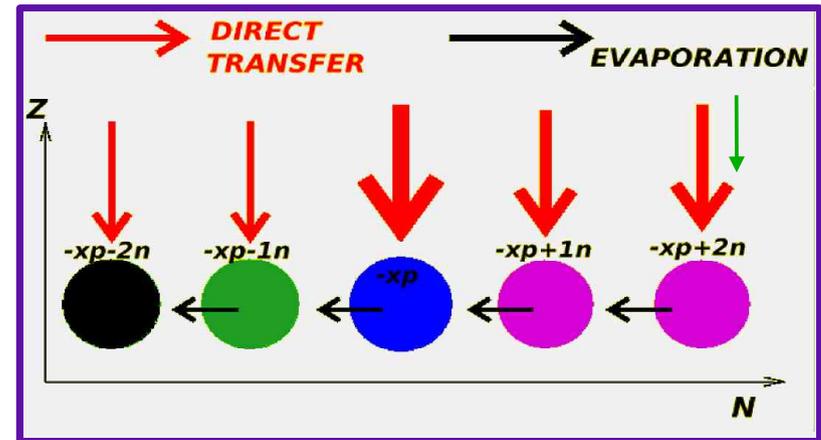
Wilczynski plots



$^{40}\text{Ar} + ^{208}\text{Pb}$



Wilczynski plots

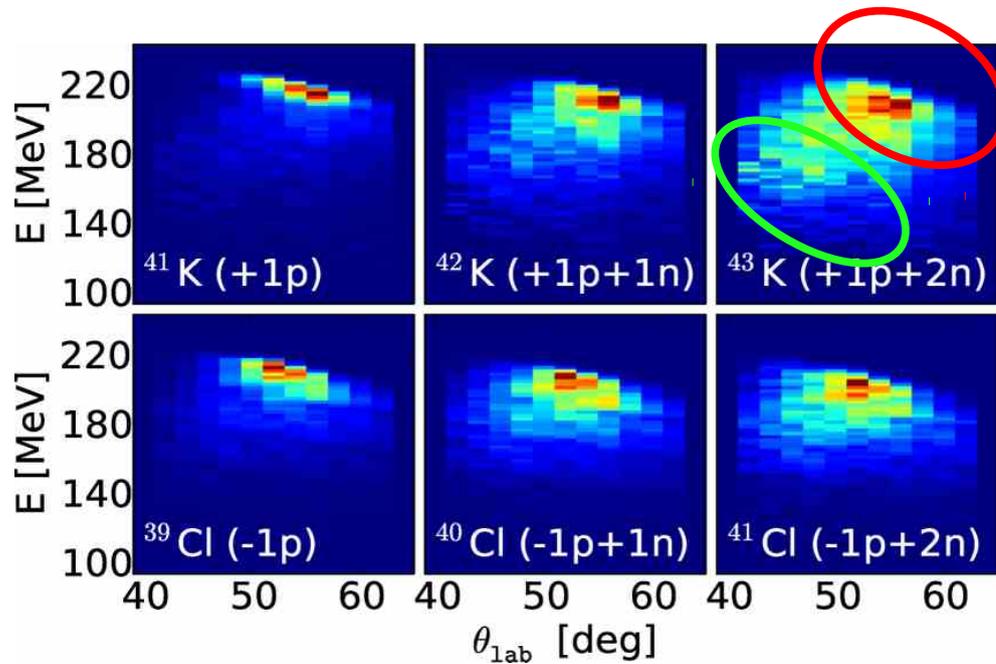


- ✓ Reaction develops from quasi-elastic to deep inelastic
- ✓ Secondary processes are important (fission, evaporation of neutrons may strongly modify the final cross sections) → survival probability of the heavy binary partner

+2n channel: $^{40}\text{Ar} + ^{208}\text{Pb} \rightarrow ^{42}\text{Ar} + ^{206}\text{Pb}$

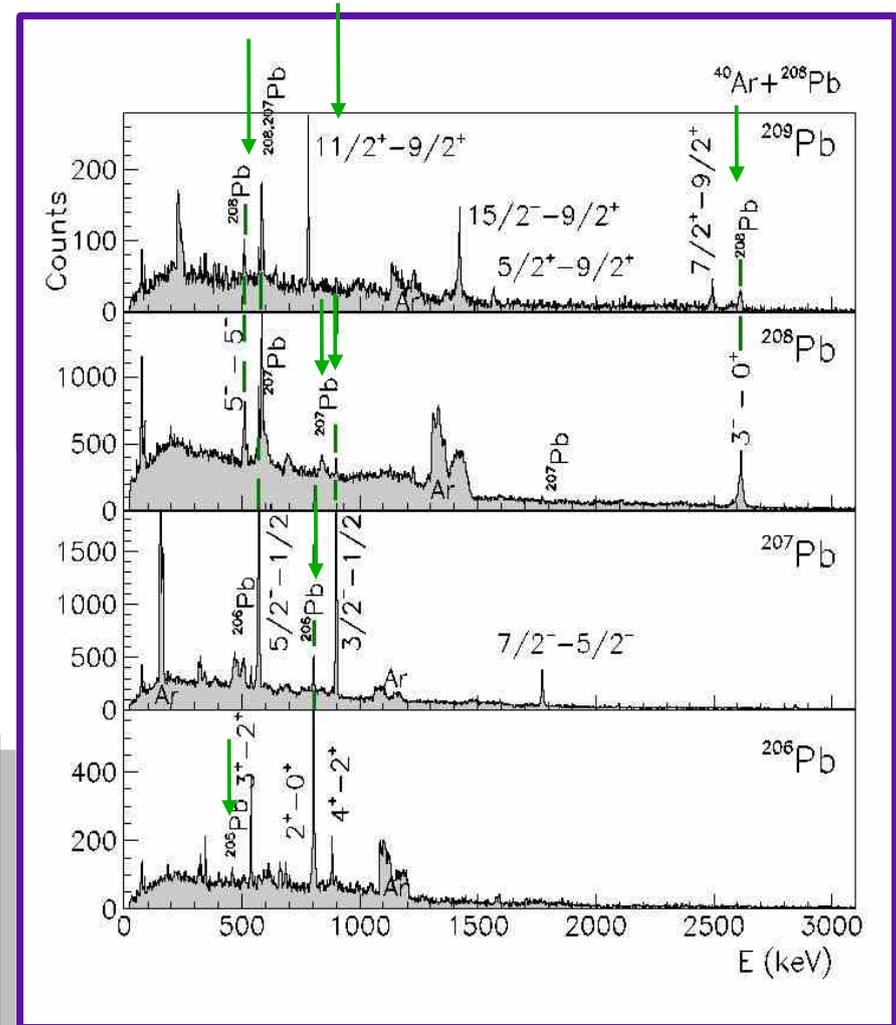
~90% of the yield corresponds to the true binary partner (^{206}Pb)

$^{40}\text{Ar} + ^{208}\text{Pb}$



Wilczynski plots

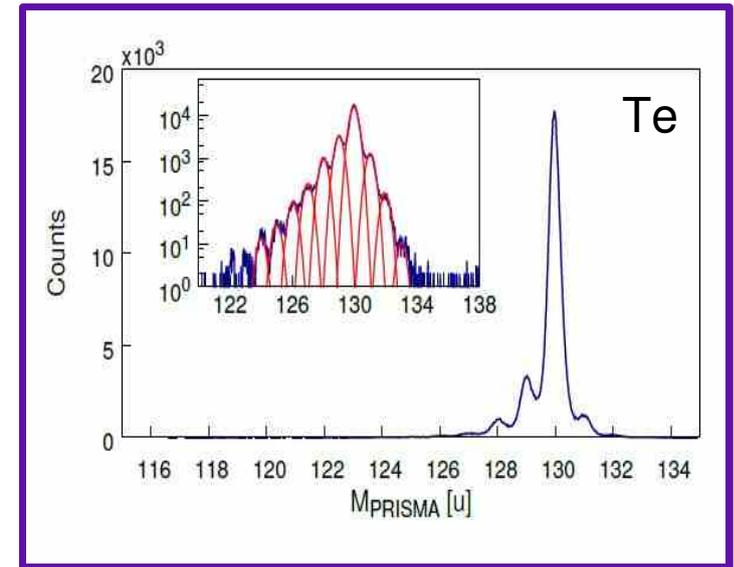
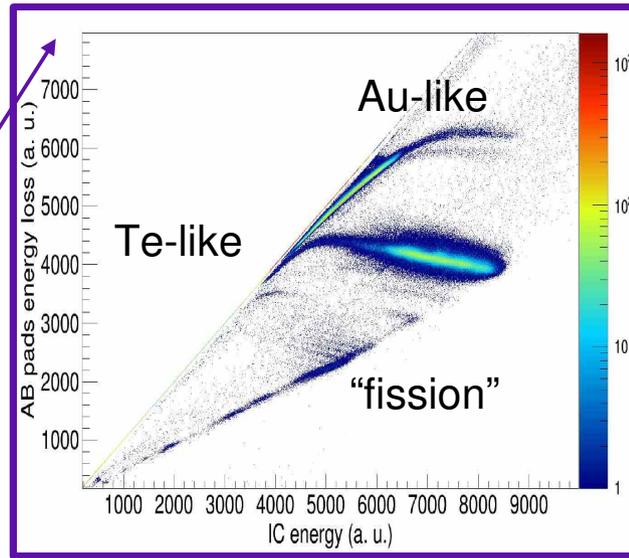
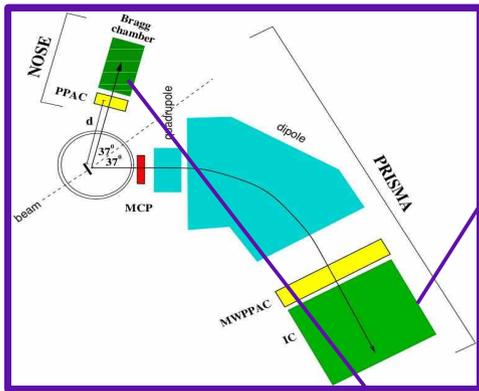
- ✓ Reaction develops from quasi-elastic to deep inelastic
- ✓ Secondary processes are important (fission, evaporation of neutrons may strongly modify the final cross sections) → survival probability of the heavy binary partner



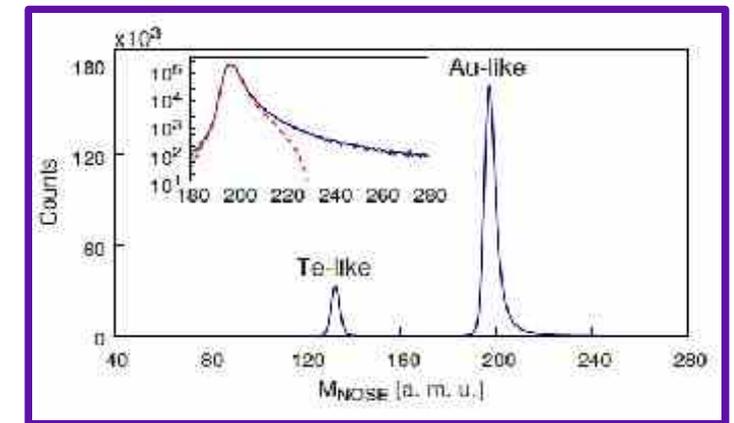
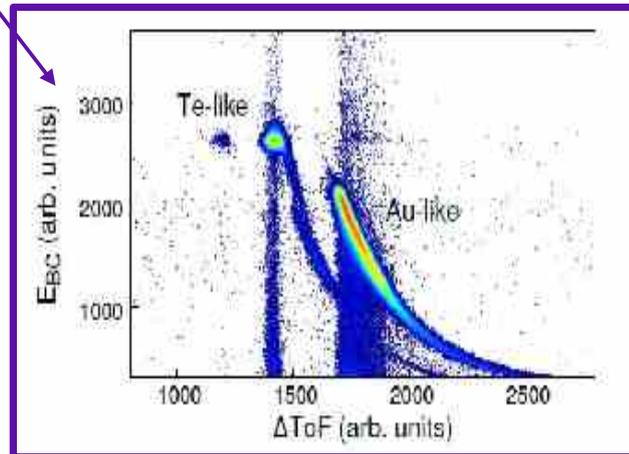
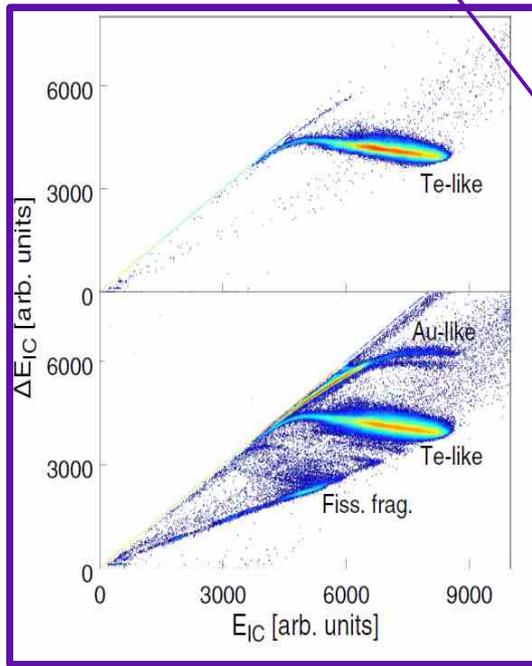
+2n channel: $^{40}\text{Ar} + ^{208}\text{Pb} \rightarrow ^{42}\text{Ar} + ^{206}\text{Pb}$

~90% of the yield corresponds to the true binary partner (^{206}Pb)

$^{197}\text{Au}+^{130}\text{Te}$: coincident detection of binary partners



PRISMA



NOSE

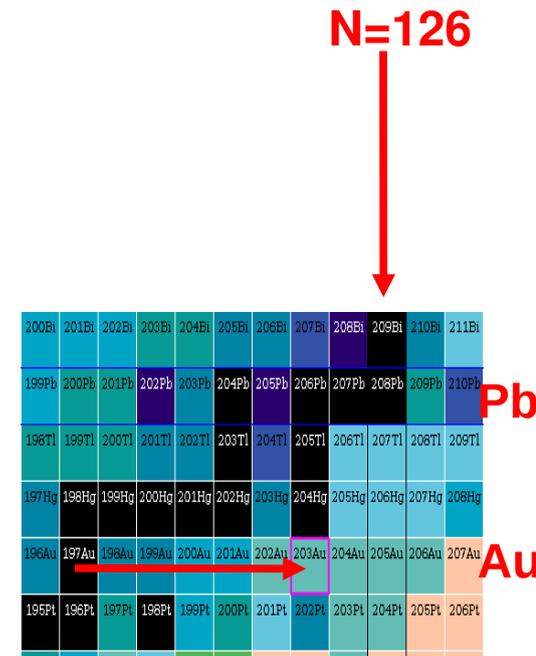
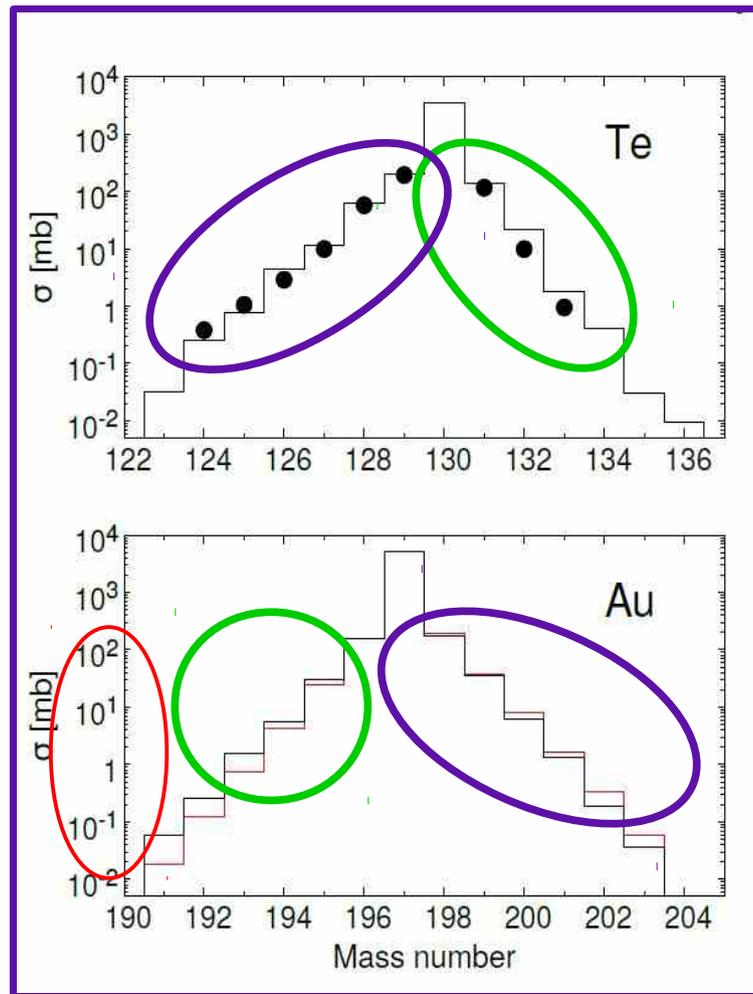
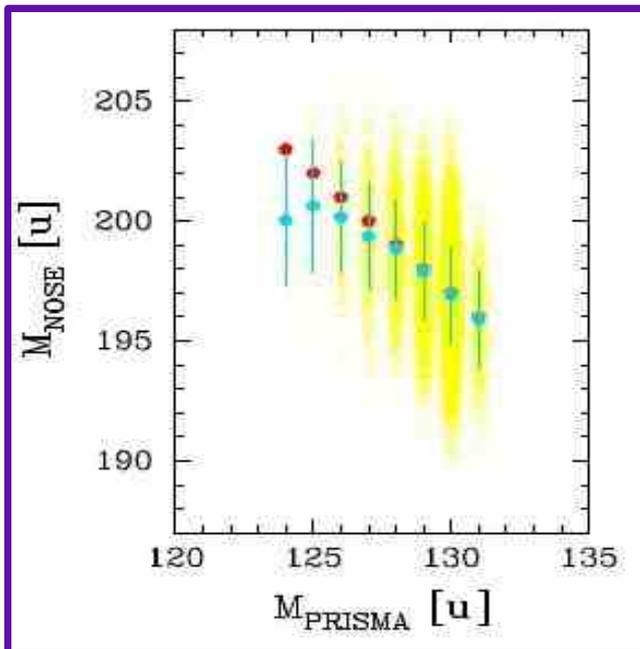
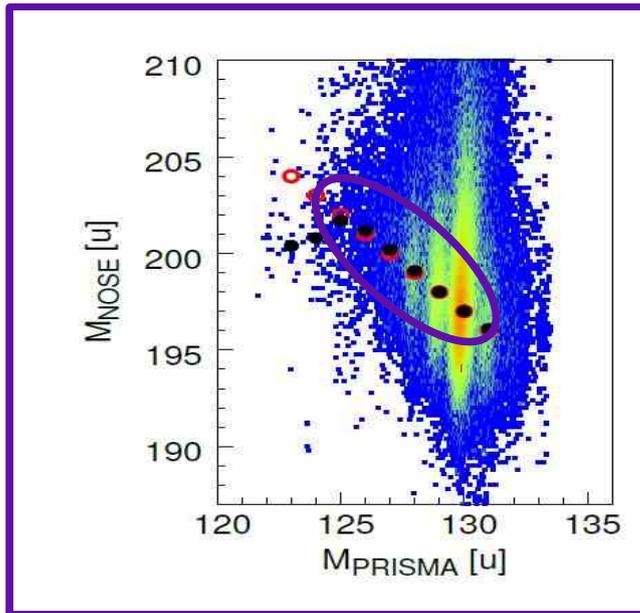
F. Galtarossa et al., Phys. Rev. C 97 (2018) 054606

E. Fioretto et al. Nucl. Inst. and Meth. A 899 (2018) 73

A gas detection system for fragment identification in low-energy heavy-ion collisions

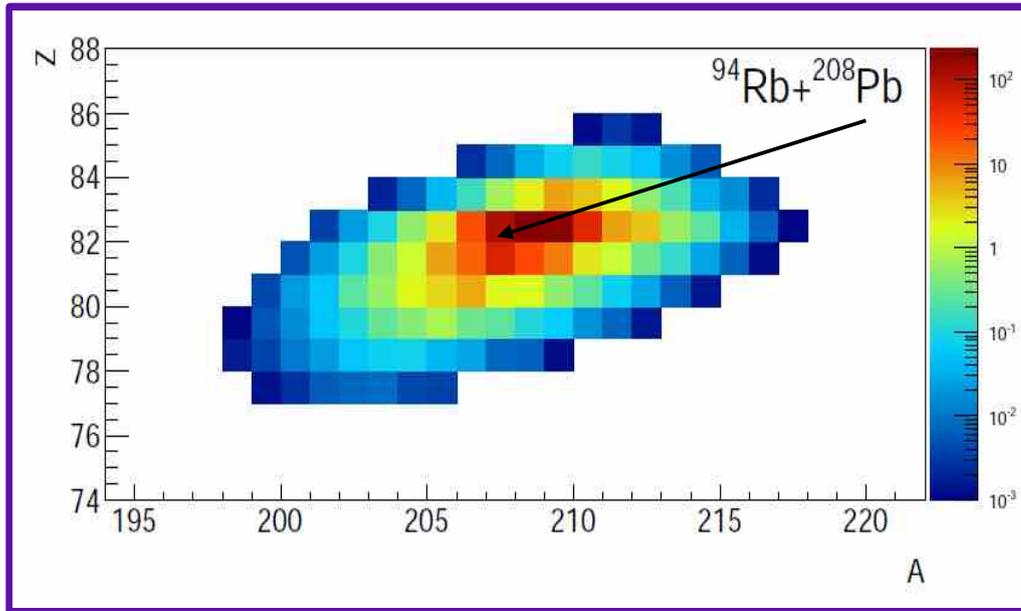
$^{197}\text{Au}+^{130}\text{Te}$

$^{197}\text{Au} + ^{130}\text{Te}$: coincident detection of binary partners

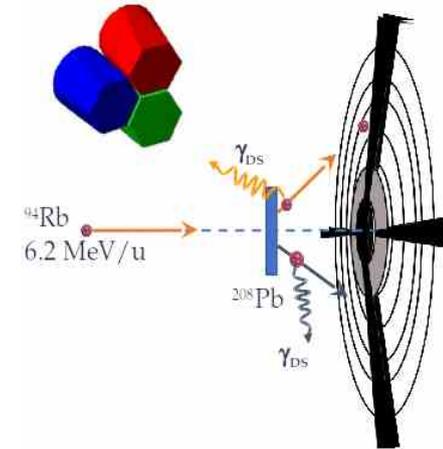


Multinucleon transfer reactions are a suitable tool for the production of heavy neutron-rich nuclei
 Te isotopes with “more” neutrons than in ^{130}Te
 Au isotopes with “more” neutrons than in ^{197}Au

$^{94}\text{Rb} + ^{208}\text{Pb}$: MNT with neutron-rich beam

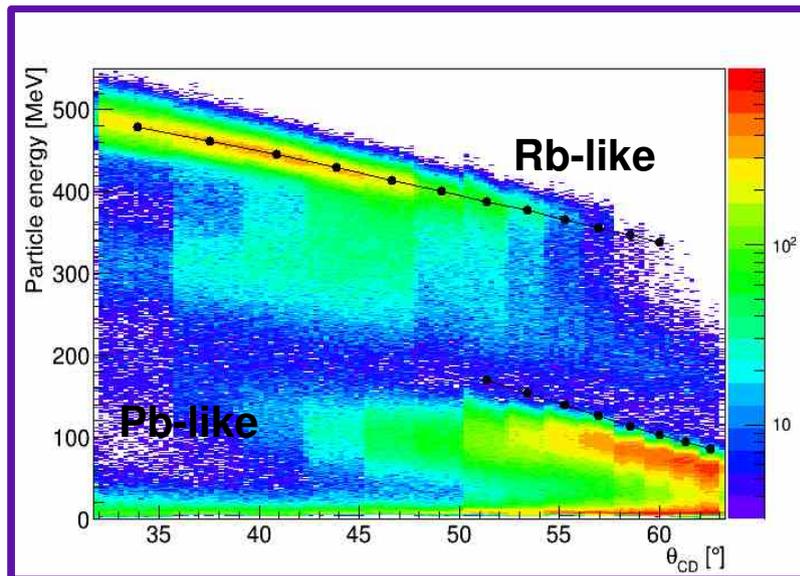


ISOLDE



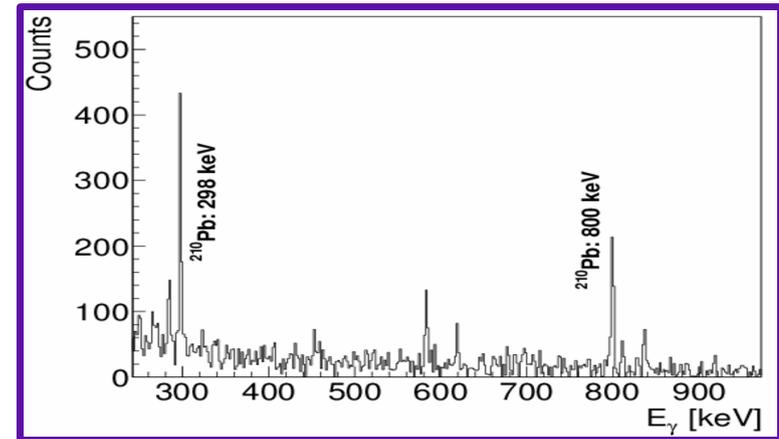
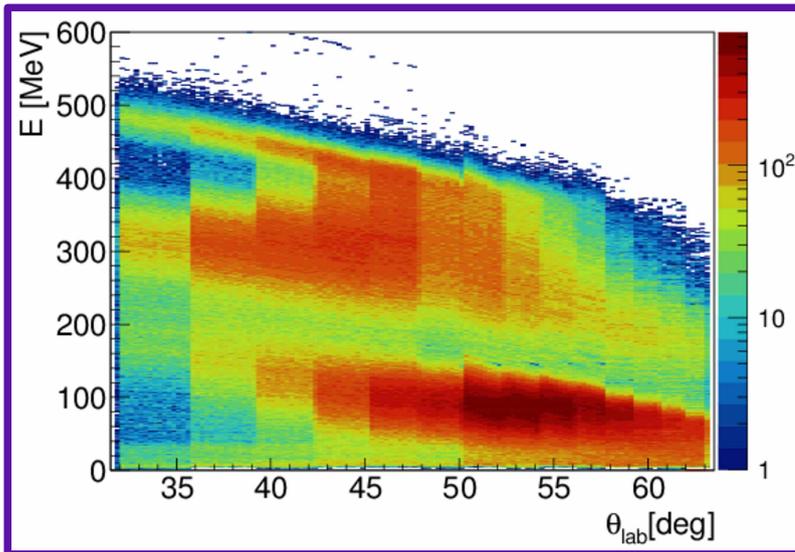
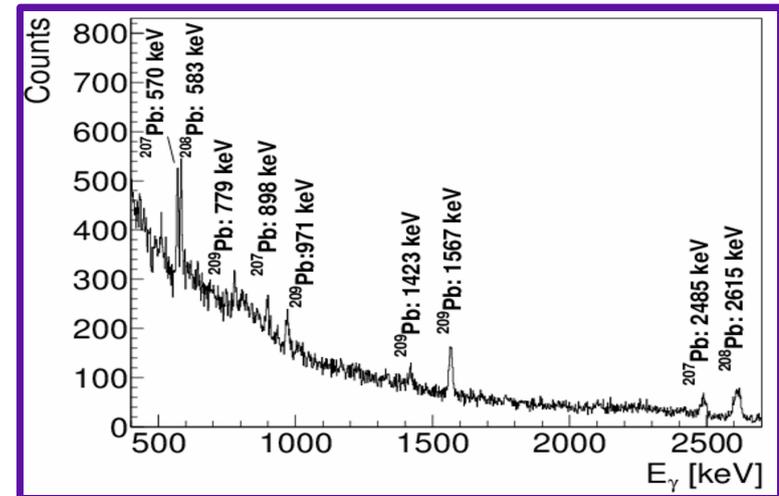
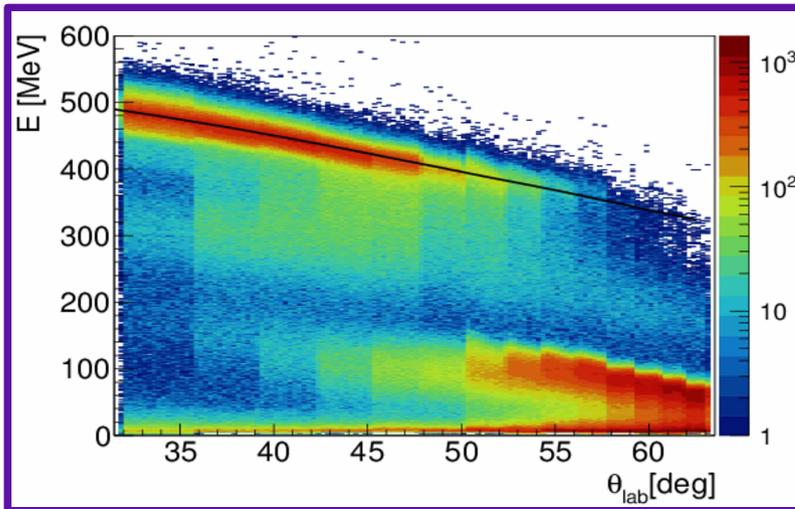
ISOLDE – CERN: MINIBALL + CD particle detector \rightarrow fragment-gamma(-gamma) coincidences

P. Čolović et al. PRC 102 (2020) 054609
Population of lead isotopes in binary reactions using a ^{94}Rb radioactive beam



ISOLDE EXP IS572, spokespersons:
J.J. Valiente Dobon and S. Szilner

$^{94}\text{Rb} + ^{208}\text{Pb}$: MNT with neutron-rich beam

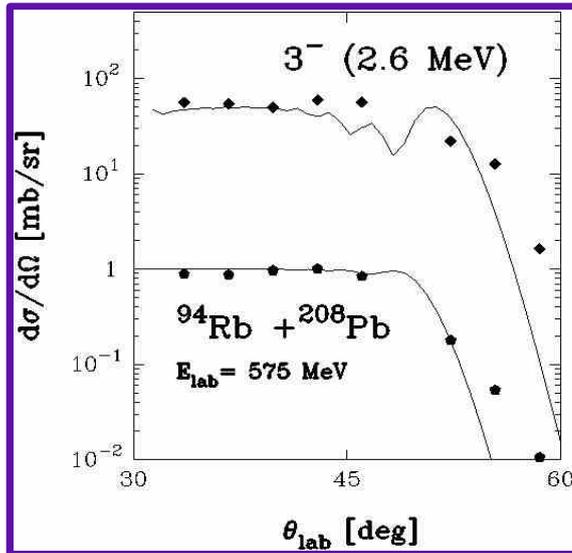


Matrix of total kinetic energy vs angle
→ fragments (top) and fragments-
gamma coincidences (bottom)

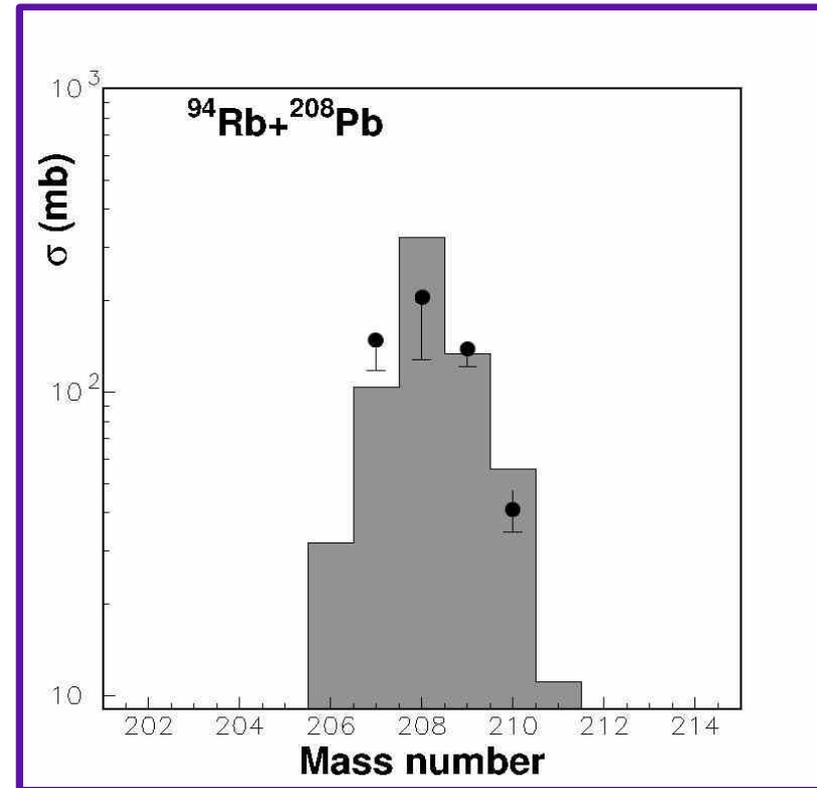
Prompt, up to 200 ns (top), and
delayed, up to $2\mu\text{s}$ (bottom) γ -ray
spectra taken in coincidence with the
Rb-like detected in CD detector

$^{94}\text{Rb} + ^{208}\text{Pb}$: MNT with neutron-rich beam

^{208}Pb



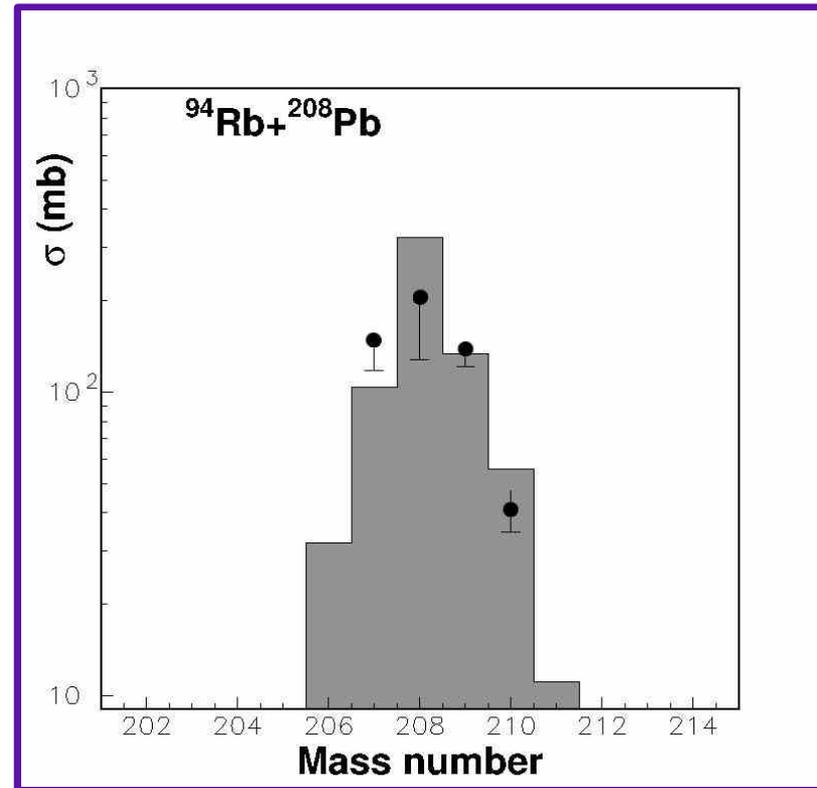
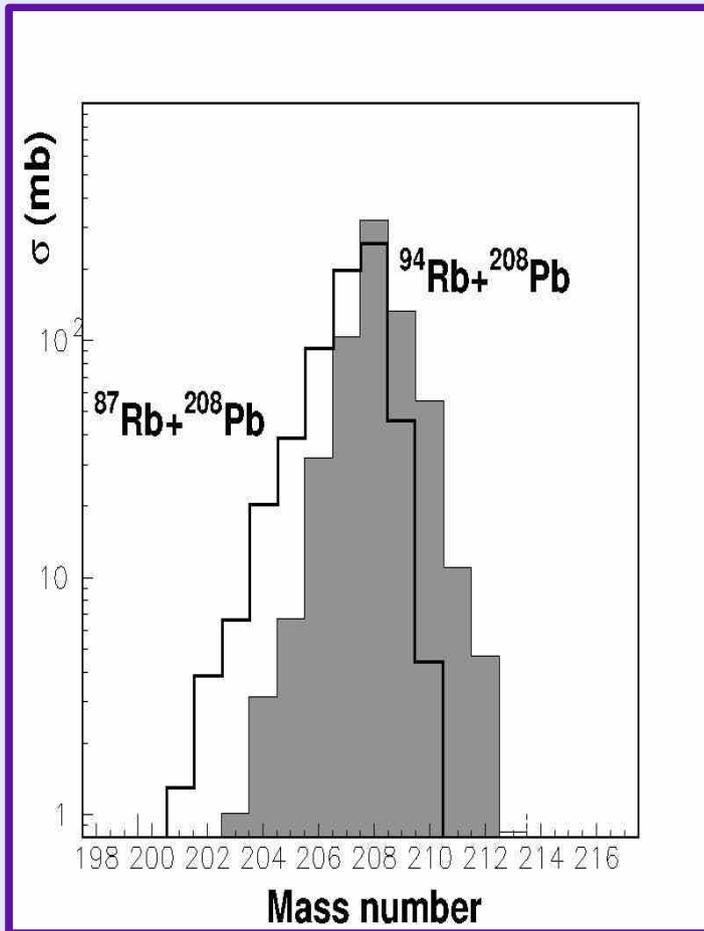
Differential cross sections for the inelastic scattering of the 3^- state in ^{208}Pb . Data have been normalized at forward angles to the DWBA calculation. Experimental quasi-elastic cross sections and theoretical elastic scattering, divided by Rutherford cross section.



Total cross sections of Pb isotopes compared with the GRAZING calculations. The measured cross sections are indicated as lower limits, while those which include the estimated values for the ground states are indicated with full points.

$^{94}\text{Rb}+^{208}\text{Pb}$: MNT with neutron-rich beam

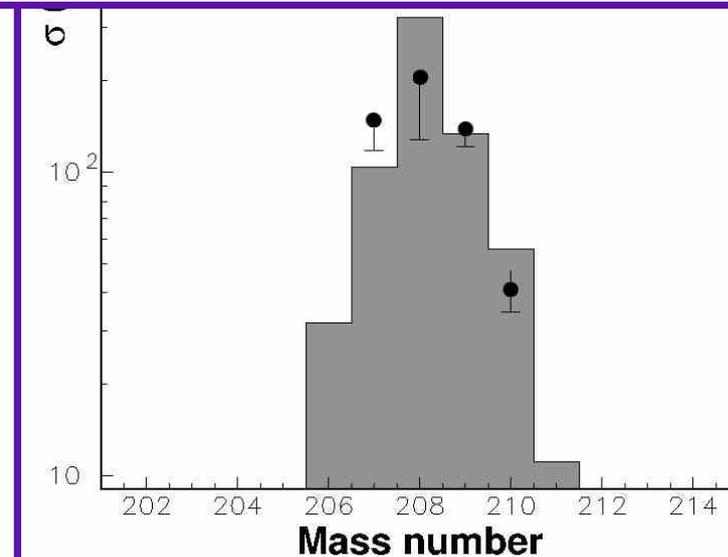
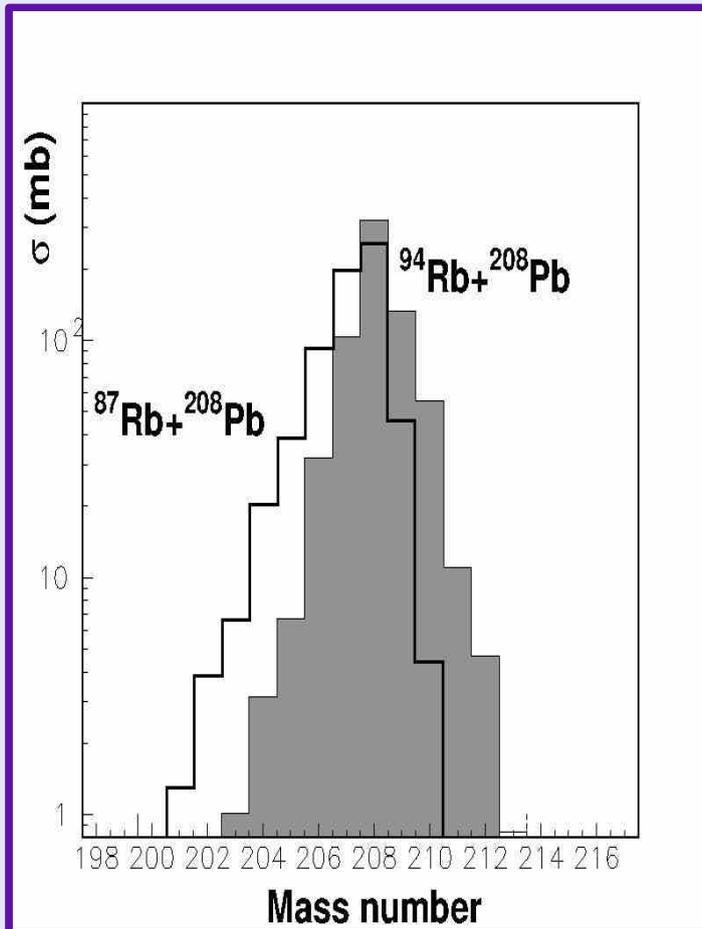
GRAZING calculated total cross sections for Pb isotopes in $^{94}\text{Rb}+^{208}\text{Pb}$ and $^{87}\text{Rb}+^{208}\text{Pb}$ reactions



Total cross sections of Pb isotopes compared with the GRAZING calculations. The measured cross sections are indicated as lower limits, while those which include the estimated values for the ground states are indicated with full points.

What new directions could stable ion beams and novel instrumentation bring to further our understanding of dynamics through gamma-ray spectroscopy?

$$N_{\text{detected}} = j_{\text{beam}} \cdot N_{\text{target}} \cdot \frac{d\sigma}{d\Omega} \cdot \Delta\Omega \cdot \epsilon_{\text{eff}}$$



Total cross sections of Pb isotopes compared with the GRAZING calculations. The measured cross sections are indicated as lower limits, while those which include the estimated values for the ground states are indicated with full points.

What new directions could stable ion beams and novel instrumentation bring to further our understanding of dynamics through gamma-ray spectroscopy?

Excited states in yttrium isotopes

transfer reactions:
 $^{90}\text{Zr} + ^{208}\text{Pb}$, fragment –
gamma coincidences
(PRISMA + CLARA)



fragment – gamma coincidences: new
gammas uniquely attributed to the specific
isotope, the isotopic chain populated in the
same reaction, relatively high spin states

M. Varga Pajtler et al, Phys. Scr. 96 (2021) 035305
and Ph.D. Thesis University of Zagreb (2014)

fission of ^{238}U accelerated
in inverse kinematic on
 ^9Be , fragment – gamma
coincidences (VAMOS +
AGATA + EXOGAM)



fragment - gamma - gamma coincidences:
the larger efficiency of arrays for mutual
gamma coincidences

J.H. Kim et al, Eur. Phys. J. A 53 (2017) 162

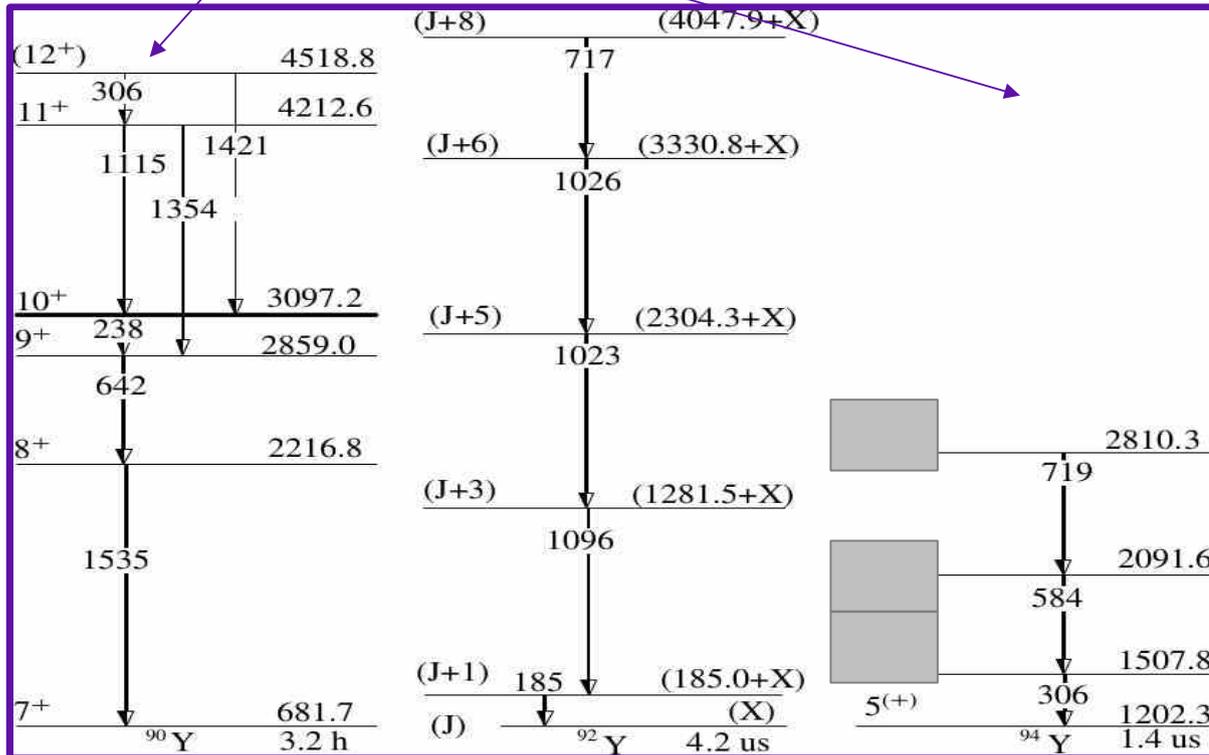
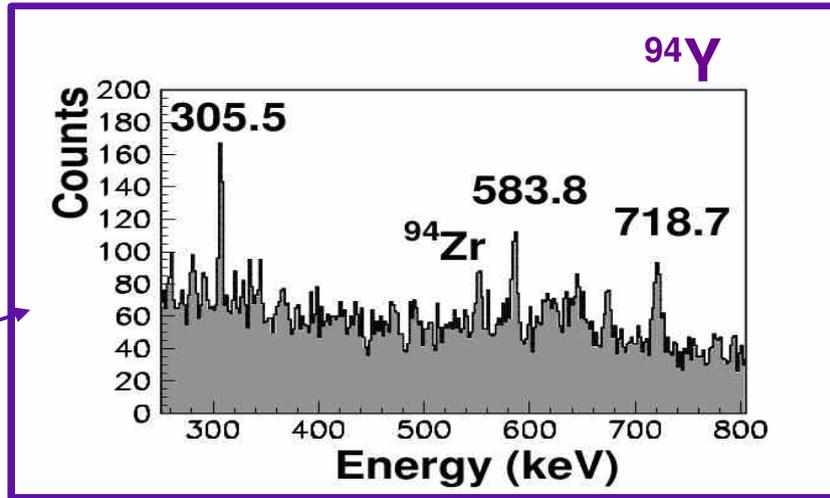
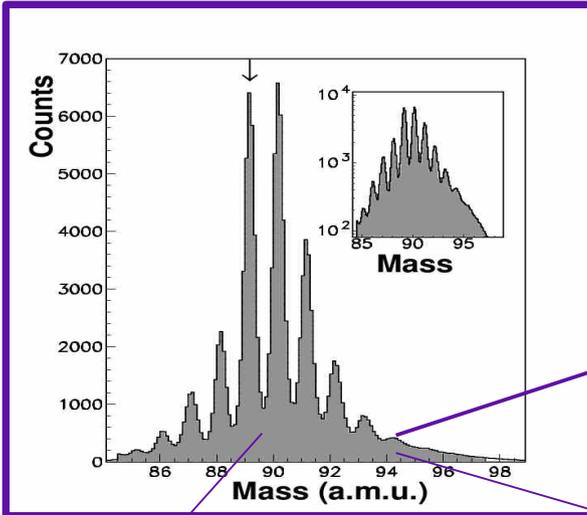
fission of ^{235}U induced by
cold neutrons, gamma
coincidences (EXILL
gamma spectrometer)



prompt and delayed gammas, spins
suggested by the gamma angular
correlation analysis

W. Iskra et al, Phys. Scr. 92 (2017) 104001

Excited states in yttrium isotopes



transfer reactions:
 $^{90}\text{Zr} + ^{208}\text{Pb}$, fragment –
 gamma coincidences
 (PRISMA + CLARA)

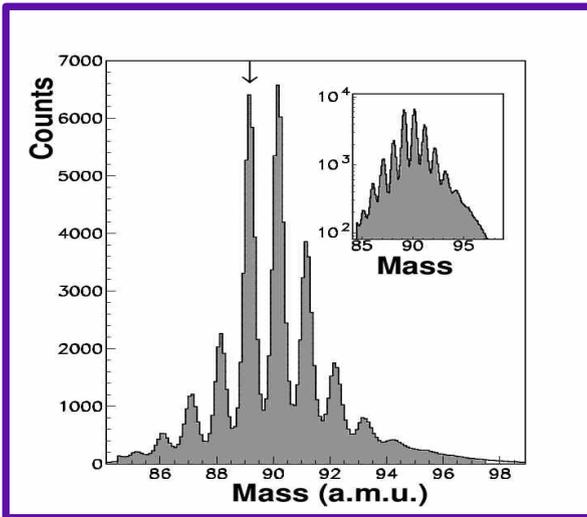
fission of ^{238}U accelerated
 on ^9Be , fragment –
 gamma - gamma
 coincidences (VAMOS +
 AGATA + EXOGAM)

90Y

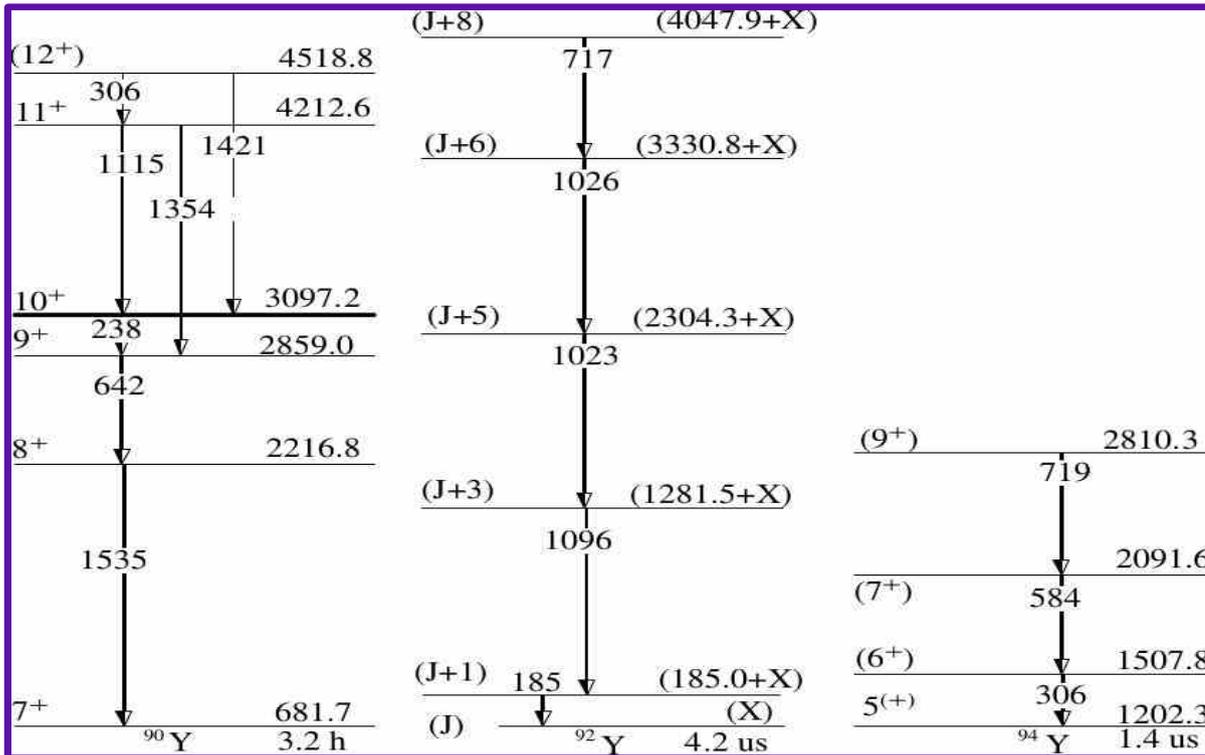
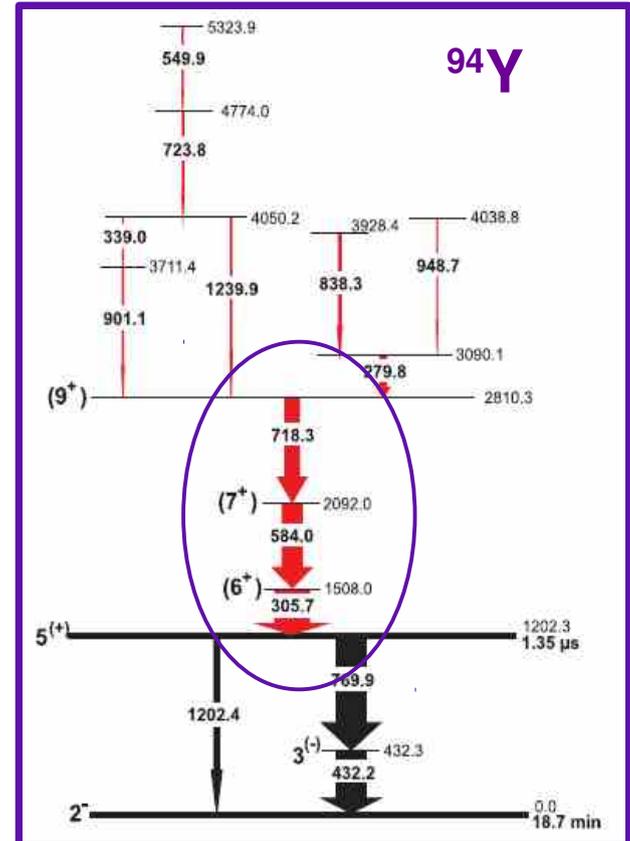
92Y

94Y

Excited states in yttrium isotopes



transfer reactions:
 $^{90}\text{Zr} + ^{208}\text{Pb}$, fragment
 – gamma
 coincidences
 (PRISMA + CLARA)



fission of ^{235}U : mutual
 coincidences, prompt and
 delayed gammas, spins
 suggested by the gamma
 angular correlation analysis
 (EXILL gamma spectrometer)

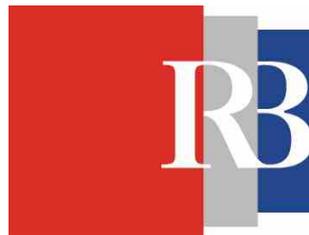
^{90}Y

^{92}Y

^{94}Y

L. Corradi, G. Pollarolo, J. Diklić, T. Mijatović, F. Galtarossa, P. Čolović, A. Goasduff, D. Montanari, E. Fioretto, A.M. Stefanini, G. Montagnoli, G. Coucci, F. Scarlassara, J.J. Valiente-Dobon, D. Mengoni, D. Jelavić Malenica, N. Soić, N. Vukman, M. Milin, D. Nurkić and CLARA-AGATA collaboration

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INFN and Università di Torino, Italy
INFN and Università di Padova, Padova, Italy
University of Zagreb, Croatia
ISOLDE, CERN*



Kokopelli: links distant and diverse communities together.



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