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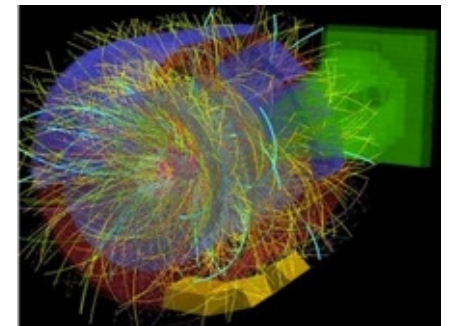
# The QGP dynamics in relativistic heavy-ion collisions

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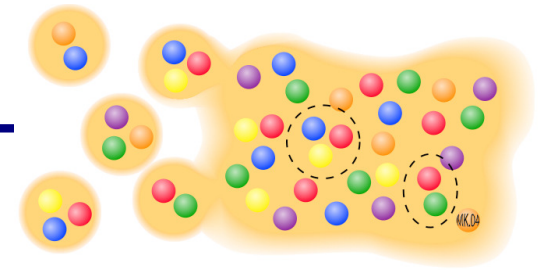


**International Workshop on Discovery Physics at the LHC  
Kruger 2012, December 3 - 7, 2012  
South Africa**





# From hadrons to partons



In order to study the **phase transition** from hadronic to partonic matter – **Quark-Gluon-Plasma** – we **need a consistent non-equilibrium (transport) model with**

- **explicit parton-parton interactions** (i.e. between quarks and gluons) beyond strings!

- **explicit phase transition** from hadronic to partonic degrees of freedom
- **IQCD EoS** for partonic phase

**Transport theory:** off-shell Kadanoff-Baym equations for the Green-functions  $S_h^<(x,p)$  in phase-space representation for the **partonic and hadronic phase**



**Parton-Hadron-String-Dynamics (PHSD)**

**QGP phase** described by

**Dynamical QuasiParticle Model (DQPM)**

W. Cassing, E. Bratkovskaya, PRC 78 (2008) 034919;  
NPA831 (2009) 215;  
W. Cassing, EPJ ST 168 (2009) 3

A. Peshier, W. Cassing, PRL 94 (2005) 172301;  
Cassing, NPA 791 (2007) 365; NPA 793 (2007)

# The Dynamical QuasiParticle Model (DQPM)

## Basic idea: Interacting quasiparticles

- massive quarks and gluons ( $g, q, q_{\text{bar}}$ ) with spectral functions :

$$\rho_i(\omega, T) = \frac{4\omega\gamma_i(T)}{(\omega^2 - \vec{p}^2 - M_i^2(T))^2 + 4\omega^2\gamma_i^2(T)} \quad (i = q, \bar{q}, g)$$

Fit from A. Peshier, PRD 70 (2004) 034016

### ■ quarks

**mass:**  $m^2(T) = \frac{N_c^2 - 1}{8N_c} g^2 \left( T^2 + \frac{\mu_q^2}{\pi^2} \right)$

**width:**  $\gamma_q(T) = \frac{N_c^2 - 1}{2N_c} \frac{g^2 T}{4\pi} \ln \frac{c}{g^2}$

### ■ gluons:

$M^2(T) = \frac{g^2}{6} \left( (N_c + \frac{1}{2}N_f) T^2 + \frac{N_c}{2} \sum_q \frac{\mu_q^2}{\pi^2} \right)$   $N_c = 3, N_f = 3$

$\gamma_g(T) = N_c \frac{g^2 T}{4\pi} \ln \frac{c}{g^2}$

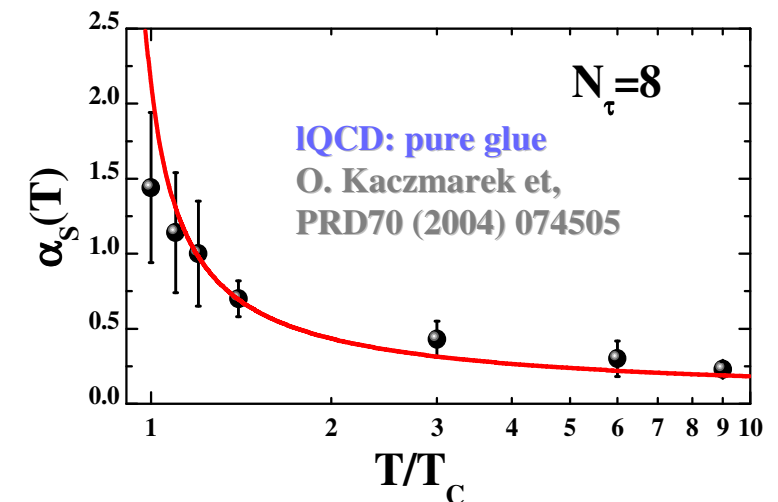
**running coupling (pure glue):**  $\alpha_s(T) = g^2(T)/(4\pi)$

$$g^2(T/T_c) = \frac{48\pi^2}{(11N_c - 2N_f) \ln(\lambda^2(T/T_c - T_s/T_c)^2)}$$

**with 3 parameters:**  $T_s/T_c = 0.46$ ;  $c = 28.8$ ;  $\lambda = 2.42$   
(for pure glue  $N_f = 0$ )

➤ **fit to lattice (IQCD) results** (e.g. entropy density)

➔ **quasiparticle properties** (mass, width)



DQPM: Peshier, Cassing, PRL 94 (2005) 172301;  
Cassing, NPA 791 (2007) 365; NPA 793 (2007)

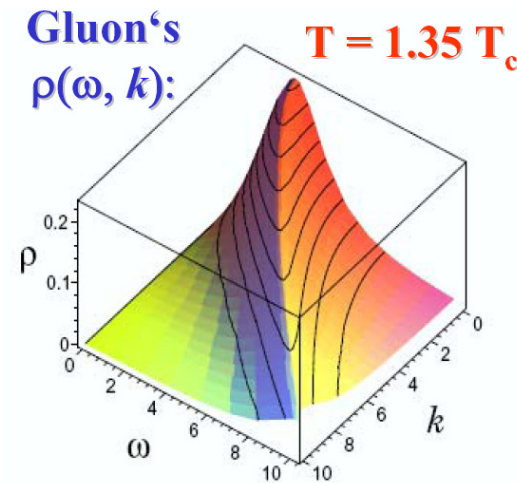
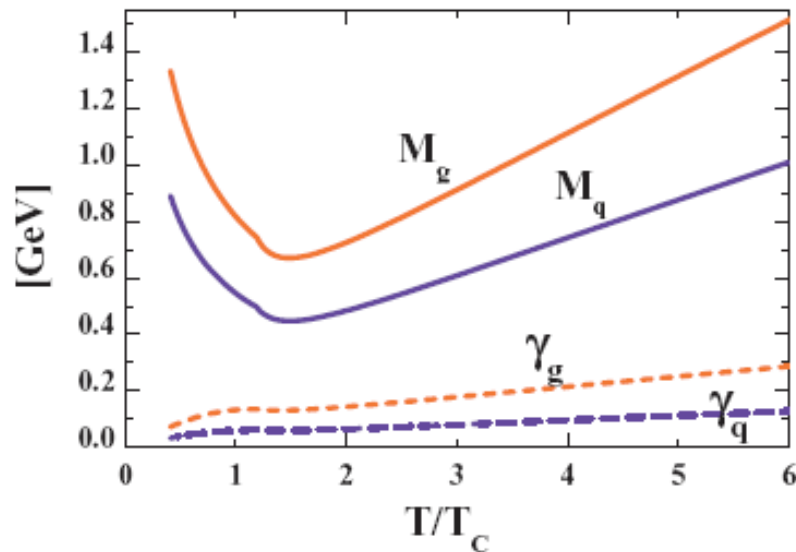
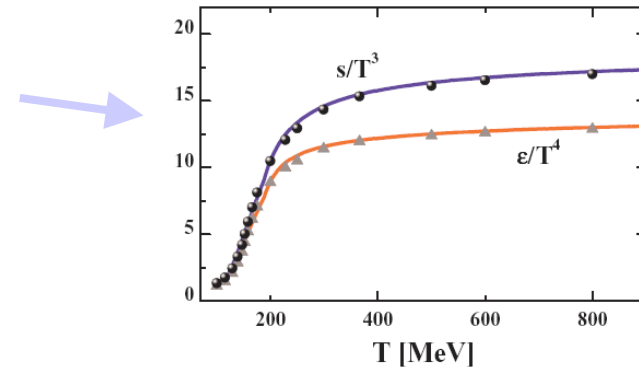
# The Dynamical QuasiParticle Model (DQPM)

➤ **fit to lattice (IQCD) results** (e.g. entropy density)

\* fit to BMW IQCD data S. Borsanyi et al., JHEP 1009 (2010) 073

➔ **Quasiparticle properties:**

■ **large width and mass for gluons and quarks**



Plot from Peshier,  
PRD 70 (2004)  
034016

- **DQPM matches well lattice QCD**
- **DQPM provides mean-fields (1PI) for gluons and quarks as well as effective 2-body interactions (2PI)**
- **DQPM gives transition rates for the formation of hadrons → PHSD**



# PHSD - basic concept

**Initial A+A collisions – HSD: string formation and decay to pre-hadrons**

**Fragmentation of pre-hadrons into quarks:** using the quark spectral functions from the **Dynamical QuasiParticle Model (DQPM)** - approximation to QCD

**Partonic phase:** quarks and gluons (= ‚dynamical quasiparticles‘) with **off-shell spectral functions** (width, mass) defined by the DQPM

**elastic and inelastic parton-parton interactions:**

using the effective cross sections from the DQPM

✓ **q + qbar (flavor neutral)  $\Leftrightarrow$  gluon (colored)**

✓ **gluon + gluon  $\Leftrightarrow$  gluon (possible due to large spectral width)**

✓ **q + qbar (color neutral)  $\Leftrightarrow$  hadron resonances**

**self-generated mean-field potential for quarks and gluons !**

**Hadronization:** based on DQPM - massive, off-shell quarks and gluons with broad spectral functions hadronize to **off-shell mesons and baryons:**

**gluons  $\rightarrow$  q + qbar; q + qbar  $\rightarrow$  meson (or string);**

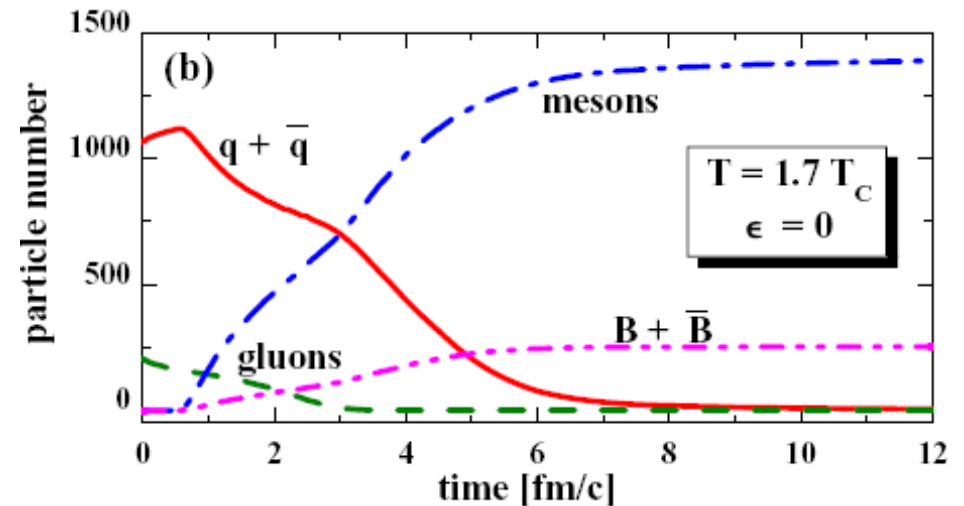
**q + q + q  $\rightarrow$  baryon (or string) (strings act as ‚doorway states‘ for hadrons)**

**Hadronic phase:** hadron-string interactions – **off-shell HSD**

W. Cassing, E. Bratkovskaya, PRC 78 (2008) 034919;  
NPA831 (2009) 215; EPJ ST 168 (2009) 3; NPA856 (2011) 162.

# PHSD: hadronization of a partonic fireball

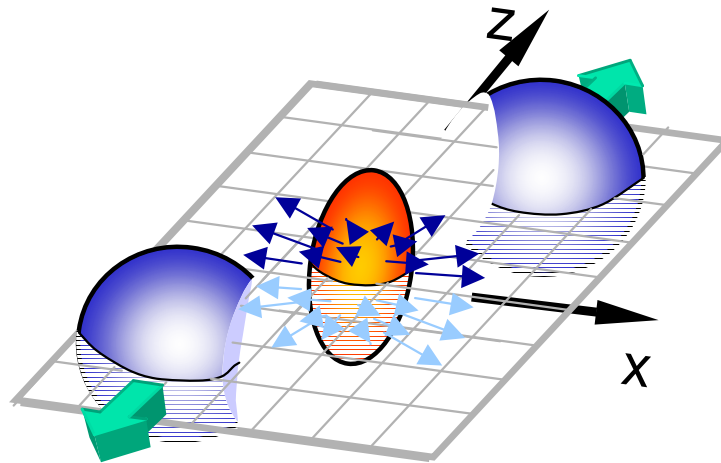
E.g. time evolution of the partonic fireball at initial temperature  $1.7 T_c$  at  $\mu_q=0$



## Consequences:

- **Hadronization:**  $q + q_{\text{bar}}$  or  $3q$  or  $3q_{\text{bar}}$  fuse to color neutral hadrons (or strings) which subsequently decay into hadrons in a microcanonical fashion, i.e. **obeying all conservation laws** (i.e. 4-momentum conservation, flavor current conservation) **in each event!**
- **Hadronization** yields **an increase in total entropy  $S$**  (i.e. more hadrons in the final state than initial partons) and not a decrease as in the simple recombination models!
- **Off-shell parton transport** roughly leads a **hydrodynamic evolution** of the partonic system

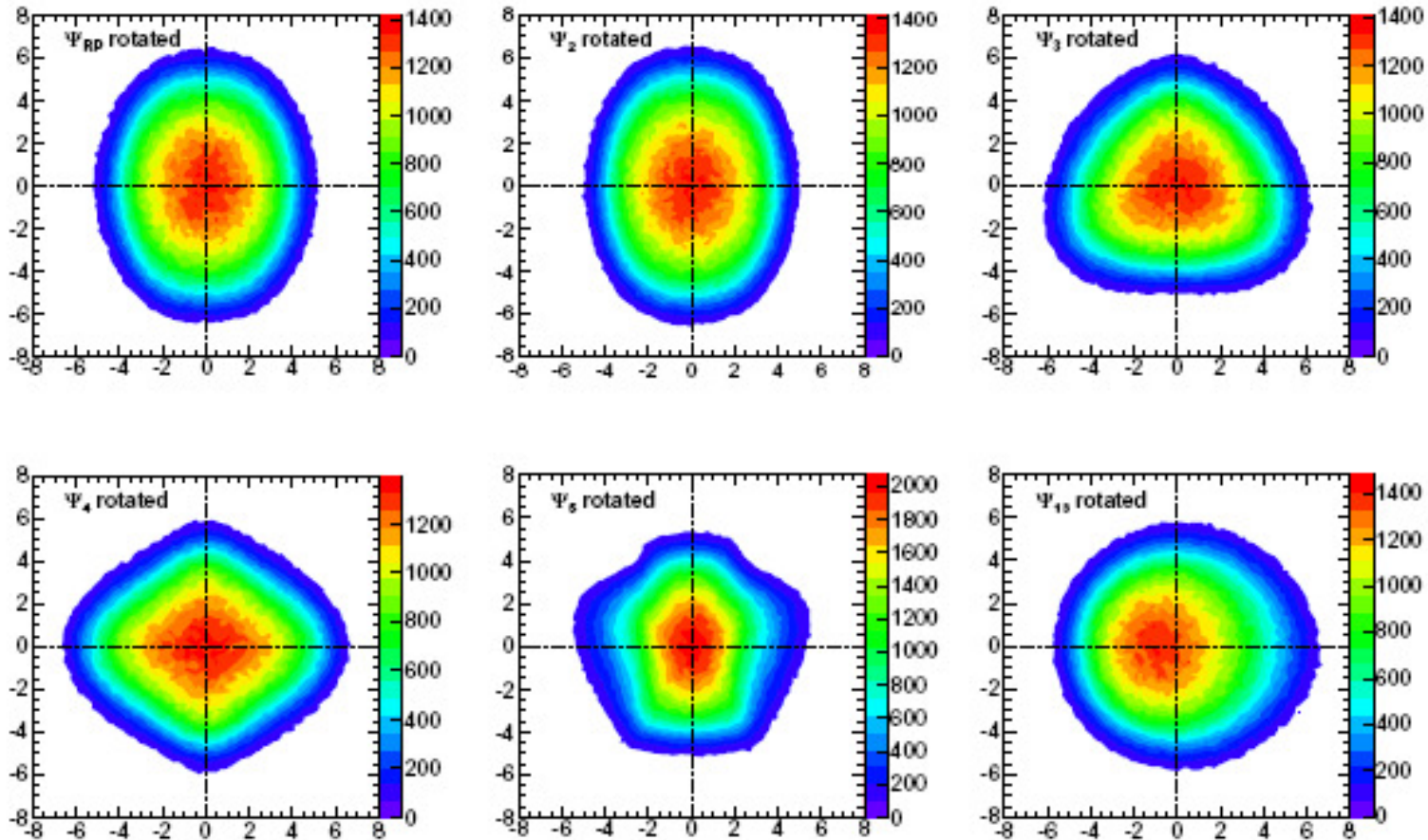
**Collective flow:  
anisotropy coefficients ( $v_1, v_2, v_3, v_4$ )  
in  $A+A$**





# Final angular distributions of hadrons

10k Au+Au collision events at  $b = 8$  fm rotated to different event planes:

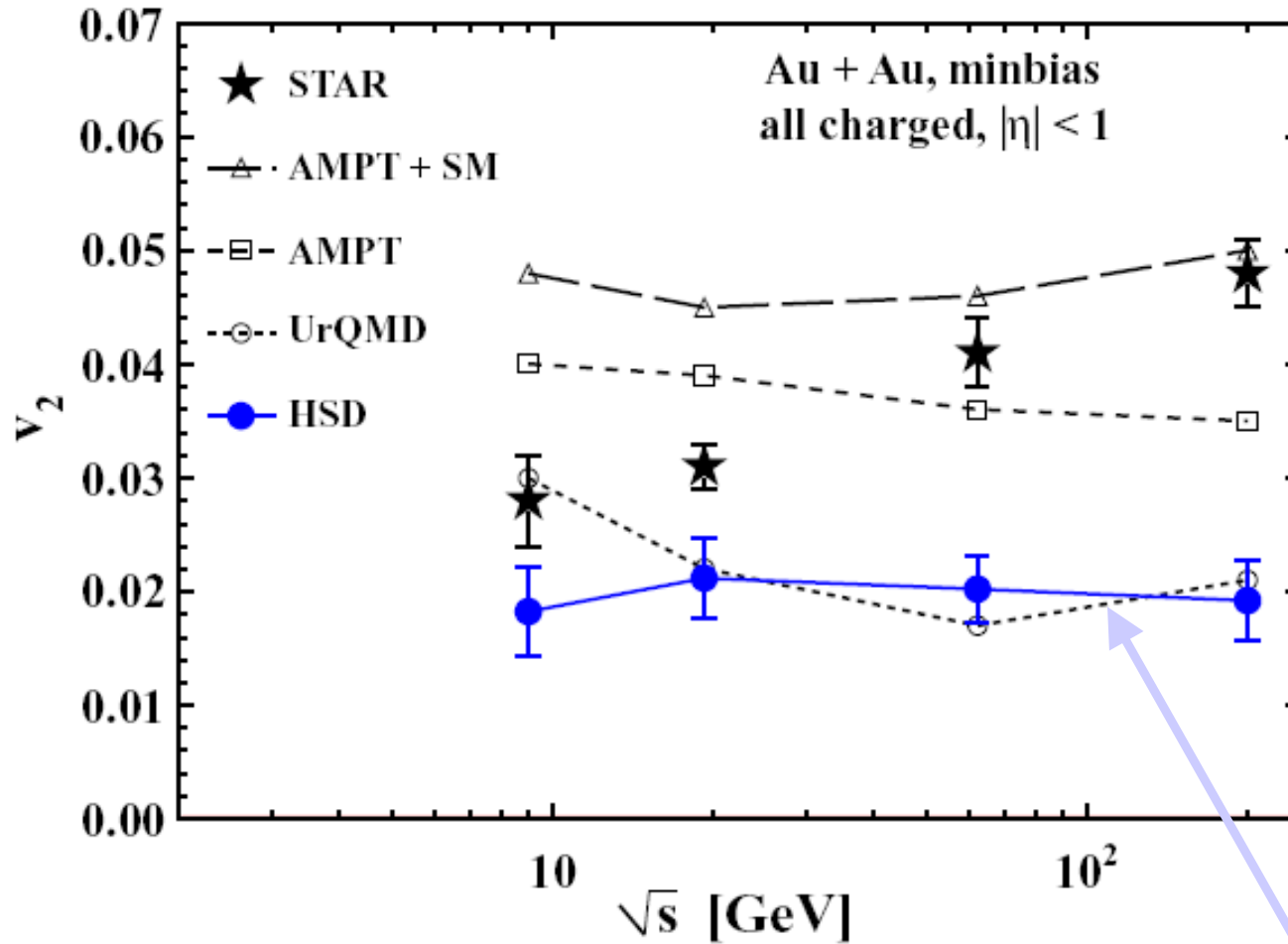


$$E \frac{d^3 N}{d^3 p} = \frac{d^2 N}{2\pi p_T dp_T dy} \left( 1 + \sum_{n=1}^{\infty} 2v_n(p_T) \cos(n(\psi - \Psi_n)) \right)$$

show higher order harmonics  $v_n$



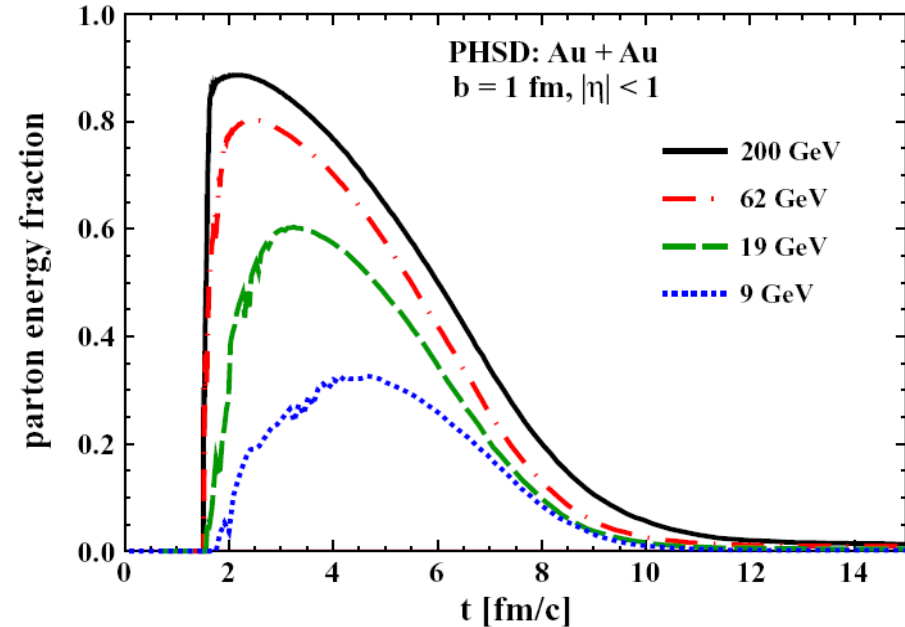
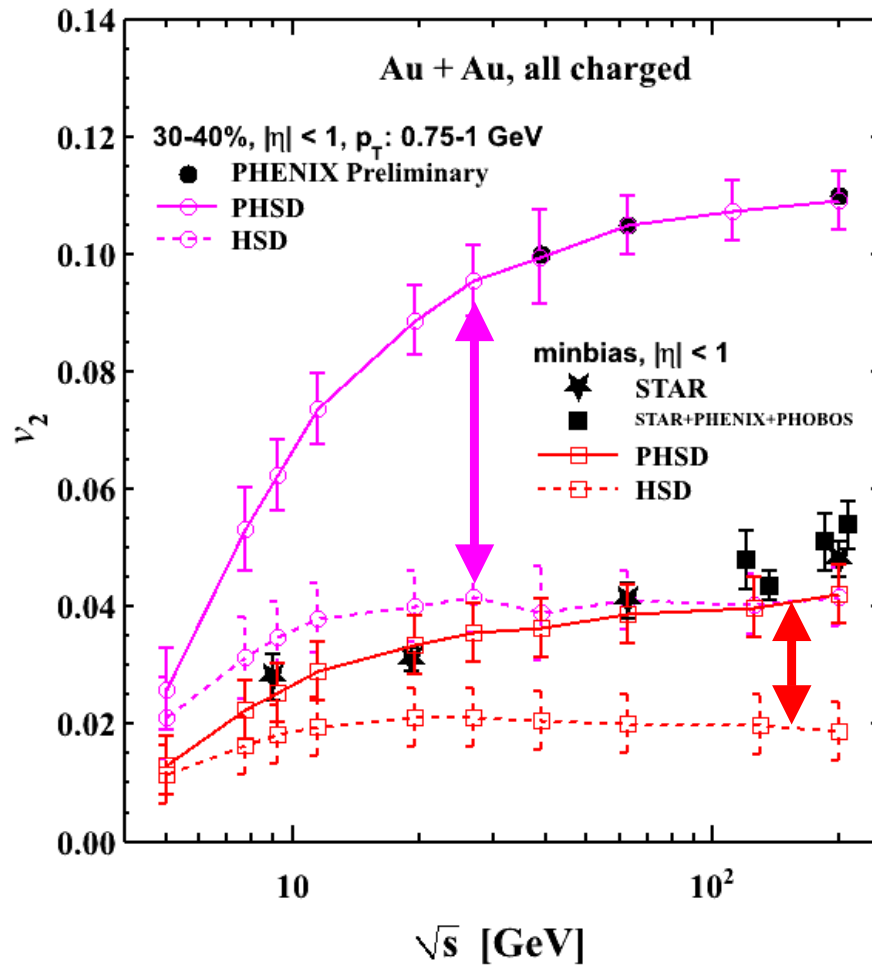
# Excitation function of elliptic flow



Excitation function of elliptic flow is not described by **hadron-string** or **purely partonic** models !



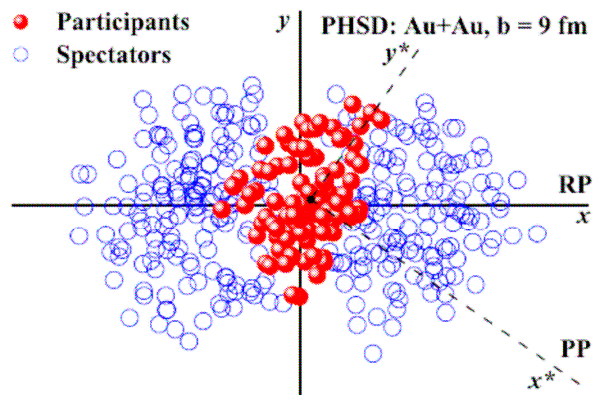
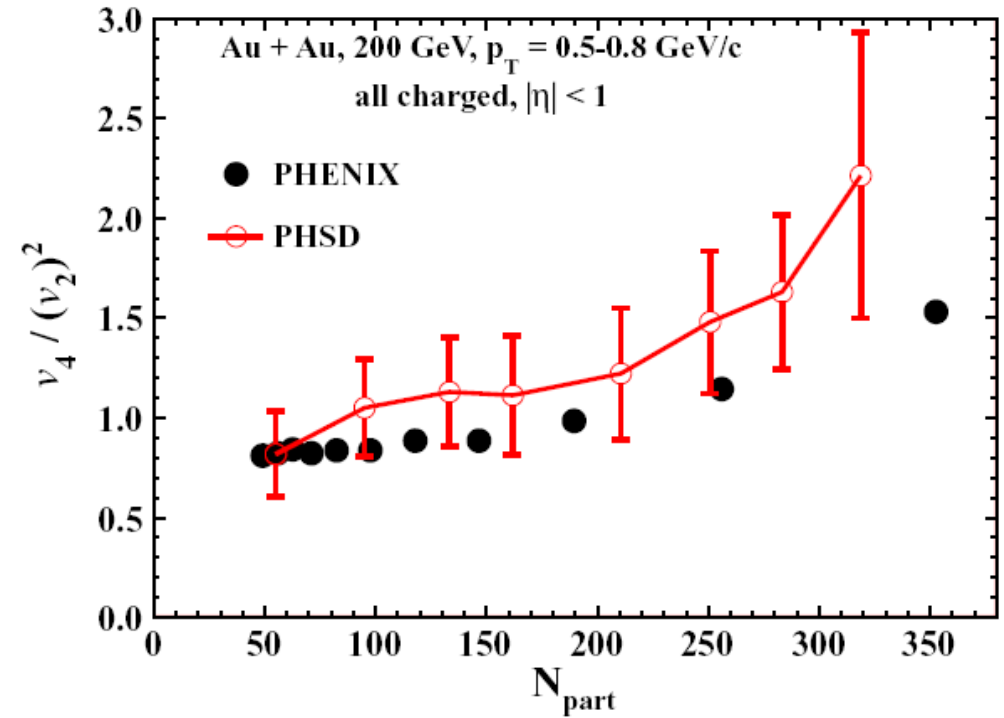
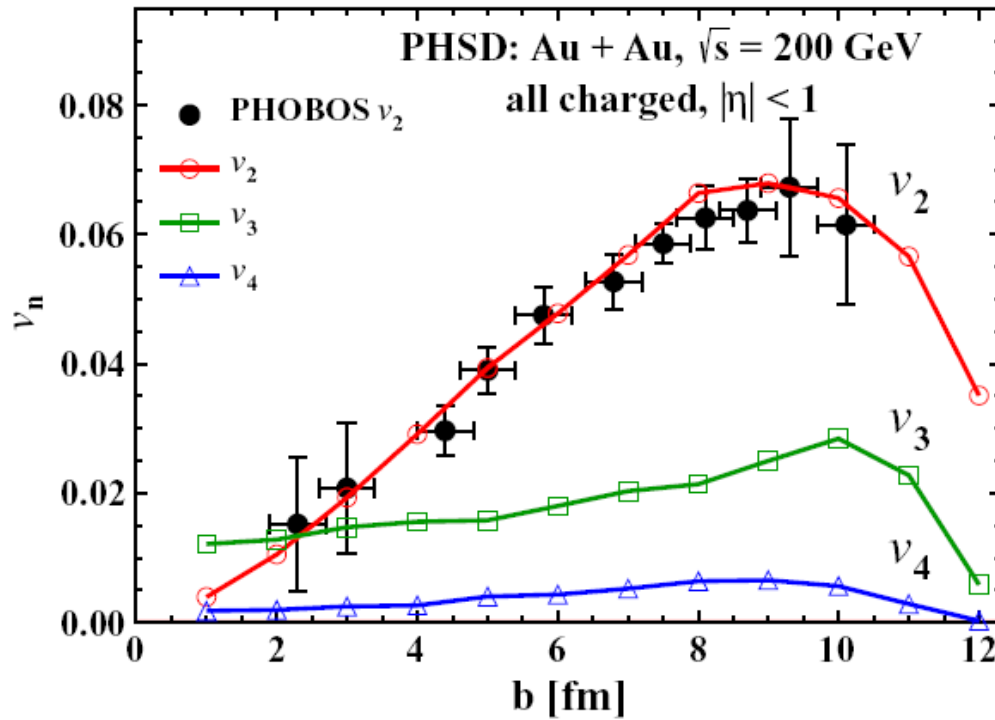
# Elliptic flow $v_2$ vs. collision energy for Au+Au



- $v_2$  in PHSD is larger than in HSD due to the repulsive scalar mean-field potential  $U_s(\rho)$  for partons
- $v_2$  grows with bombarding energy due to the increase of the parton fraction



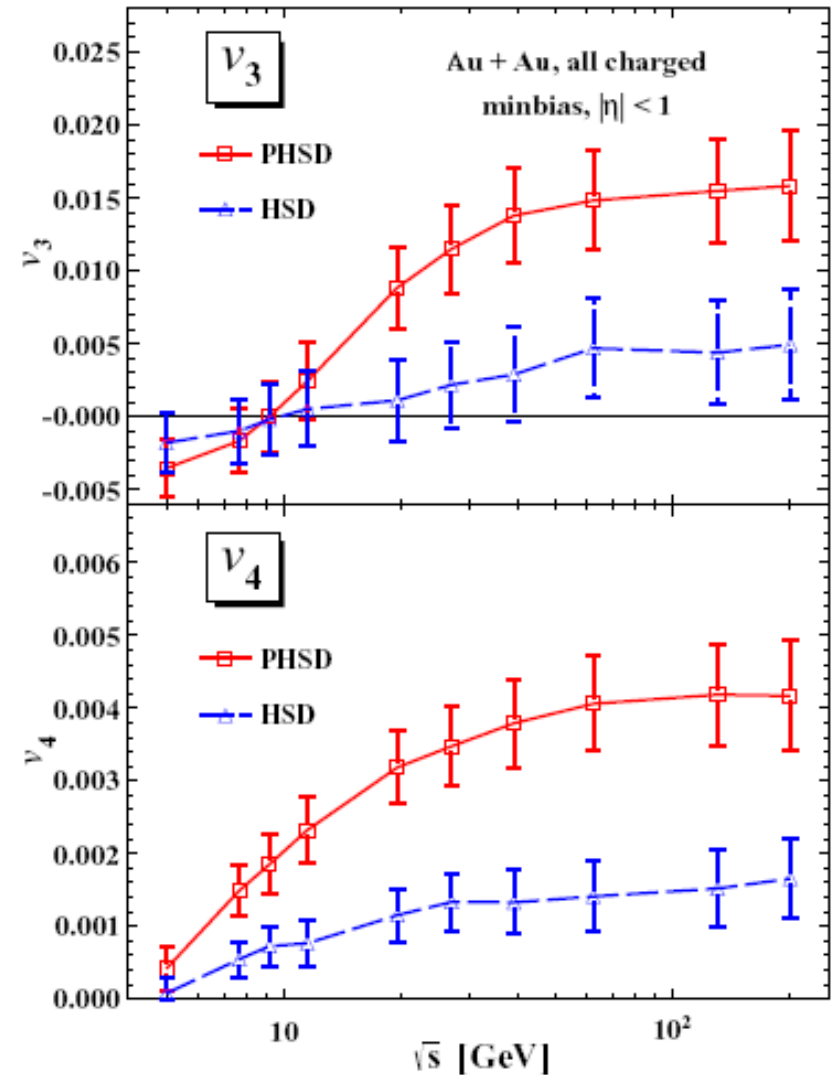
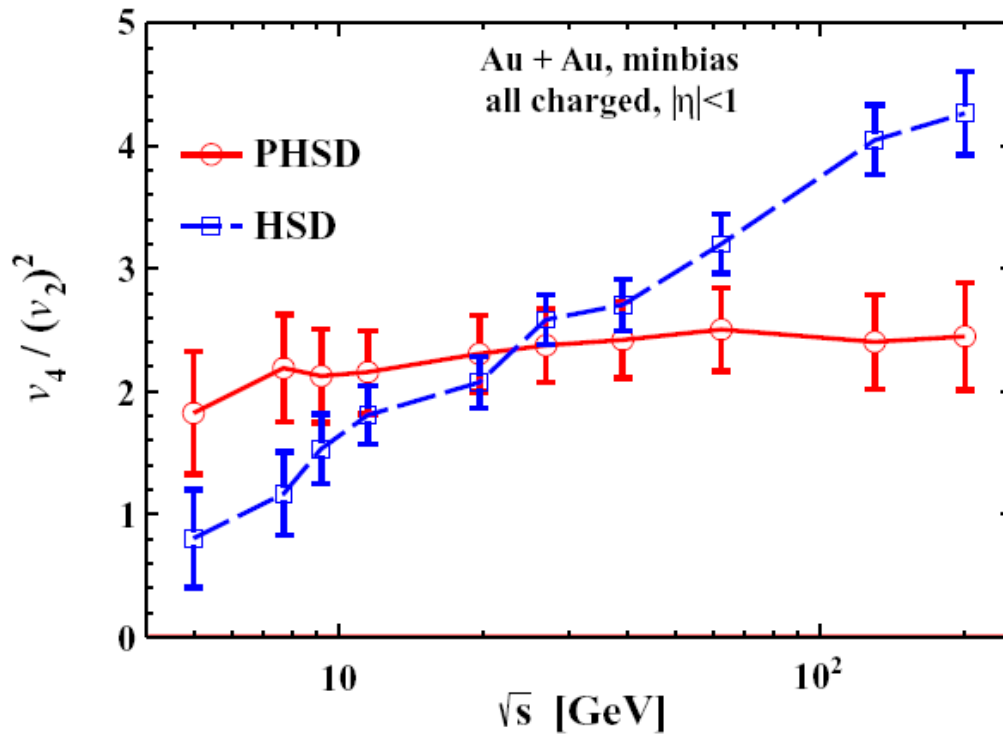
# Flow coefficients versus centrality at RHIC



□ increase of  $v_2$  with impact parameter but flat  $v_3$  and  $v_4$



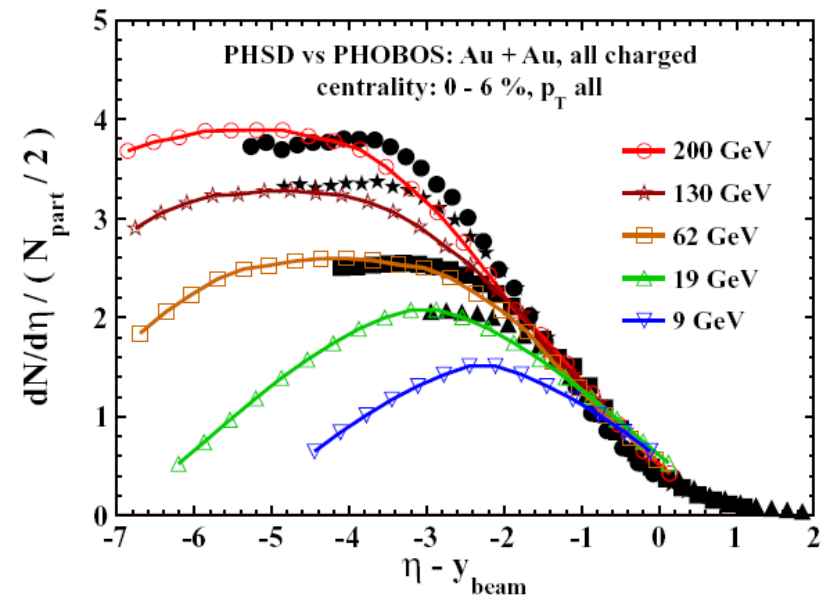
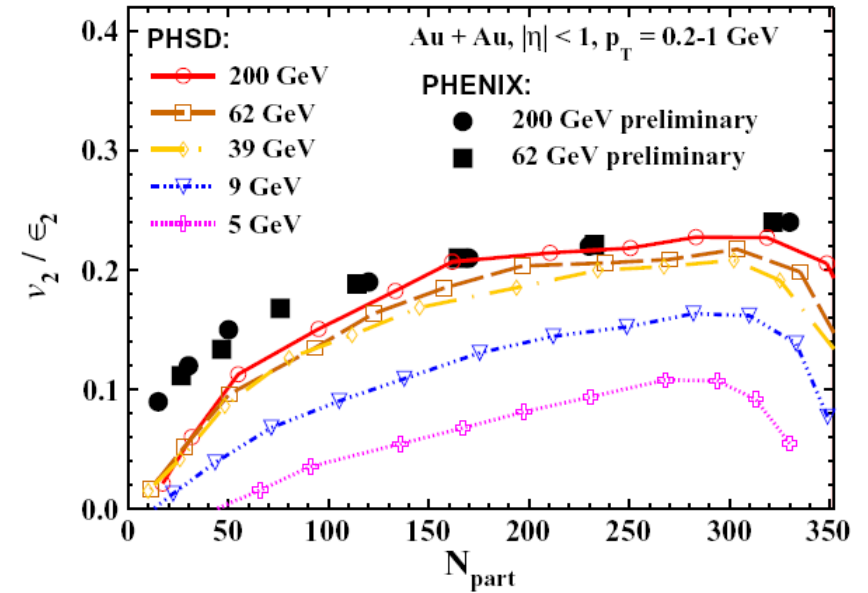
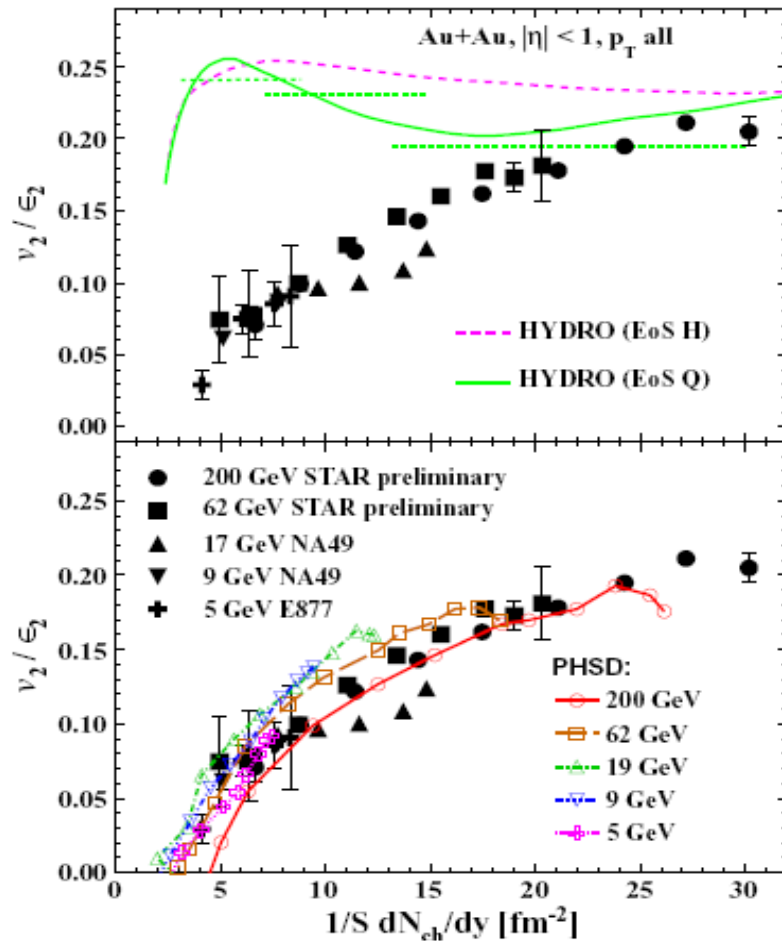
# $v_4/(v_2)^2$ , $v_3$ , $v_4$ excitation functions at RHIC



- $v_3, v_4$  from PHSD are systematically larger than those from HSD
- very low  $v_3$  and  $v_4$  at FAIR/NICA energies
- almost constant  $v_4/(v_2)^2$  for PHSD



# Scaling properties

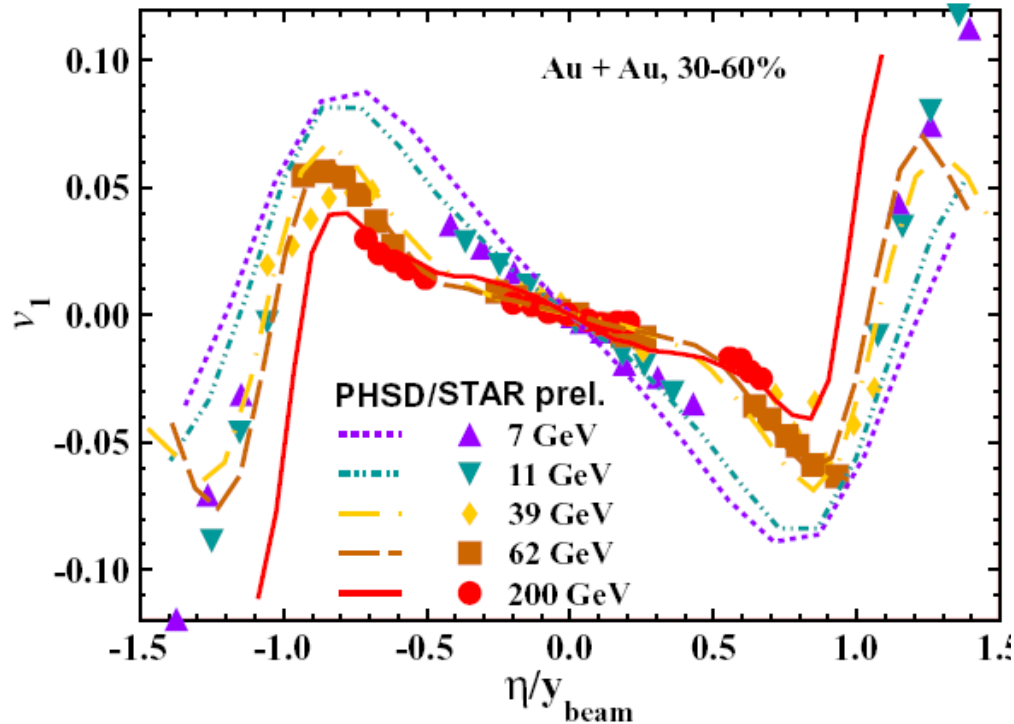


■ PHSD:  $v_2/\epsilon$  vs. centrality follows an approximate scaling with energy in line with experimental data

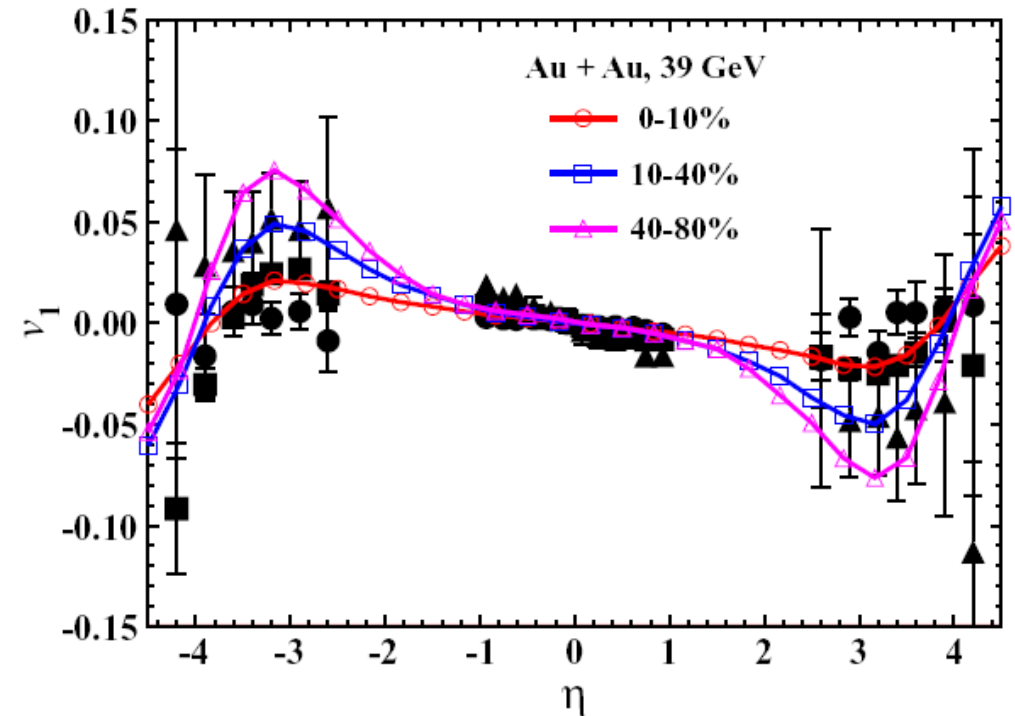


# In-plane flow $v_1$ at RHIC

versus beam energy



versus centrality

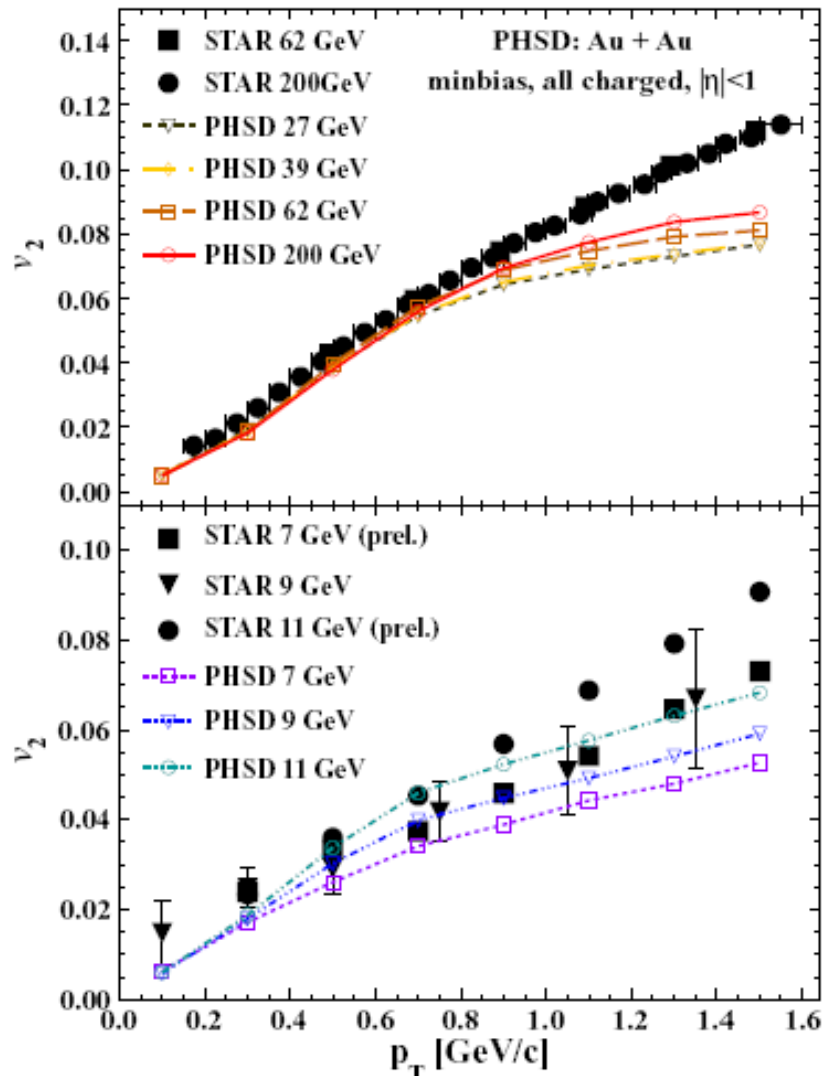


- **PHSD:  $v_1$  vs. pseudo-rapidity** follows an **approximate scaling** for high invariant energies  $s^{1/2}=39, 62, 200$  GeV - in line with experimental data – whereas at low energies the scaling is violated!

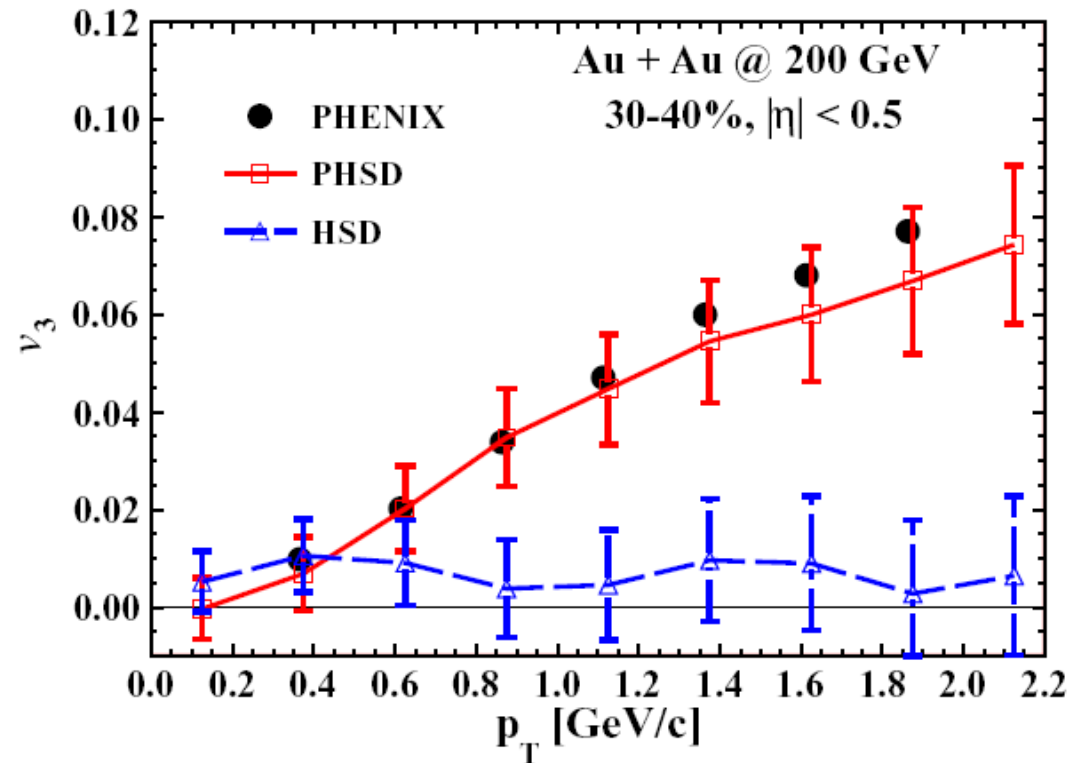


# Transverse momentum dependence at RHIC

## elliptic flow



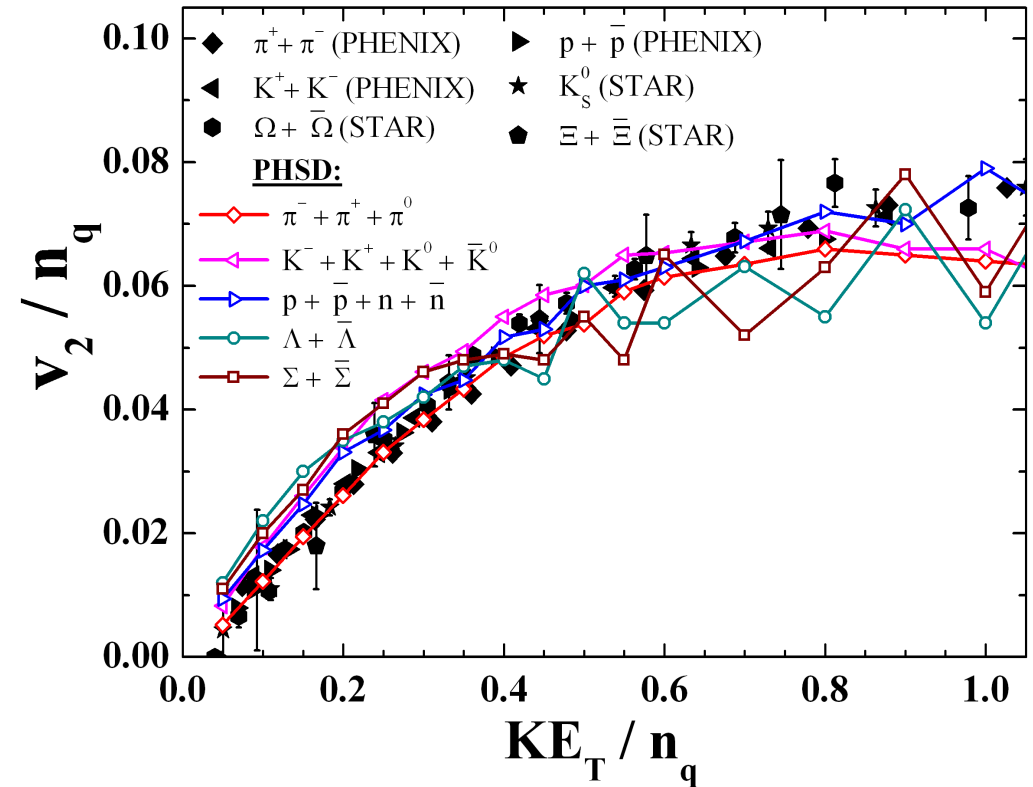
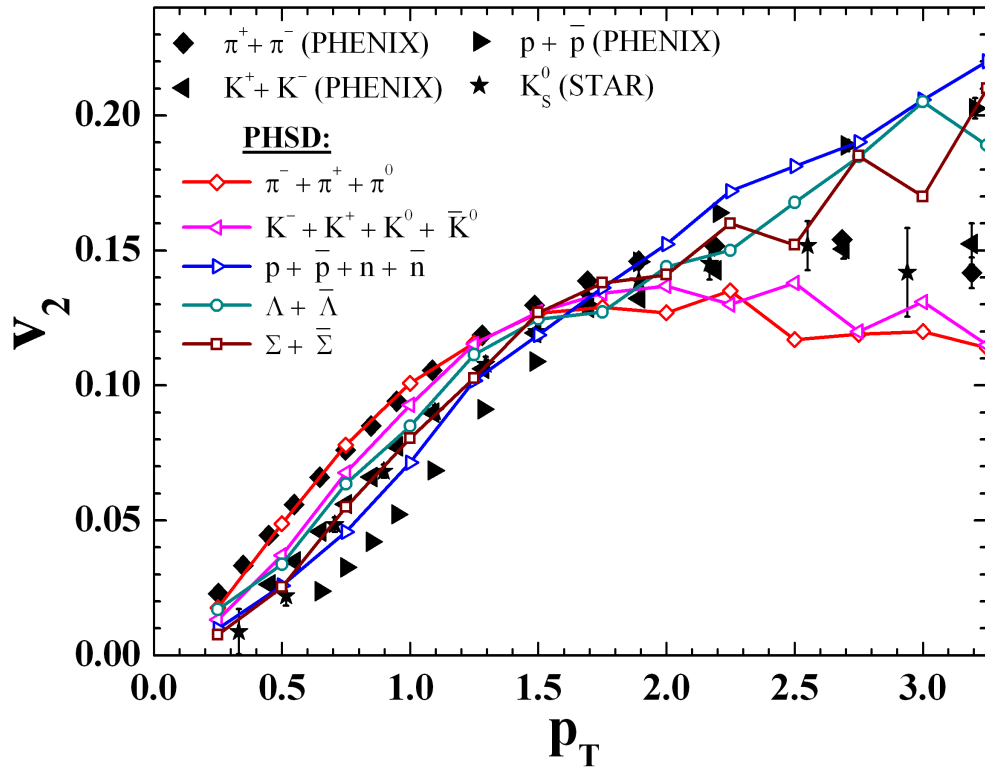
## triangular flow



- $v_2$  vs.  $p_T$  follows an **approximate scaling** for high invariant energies  $s^{1/2}=27, 39, 62, 200$  GeV
- $v_3$  : **needs partonic degrees-of-freedom !**



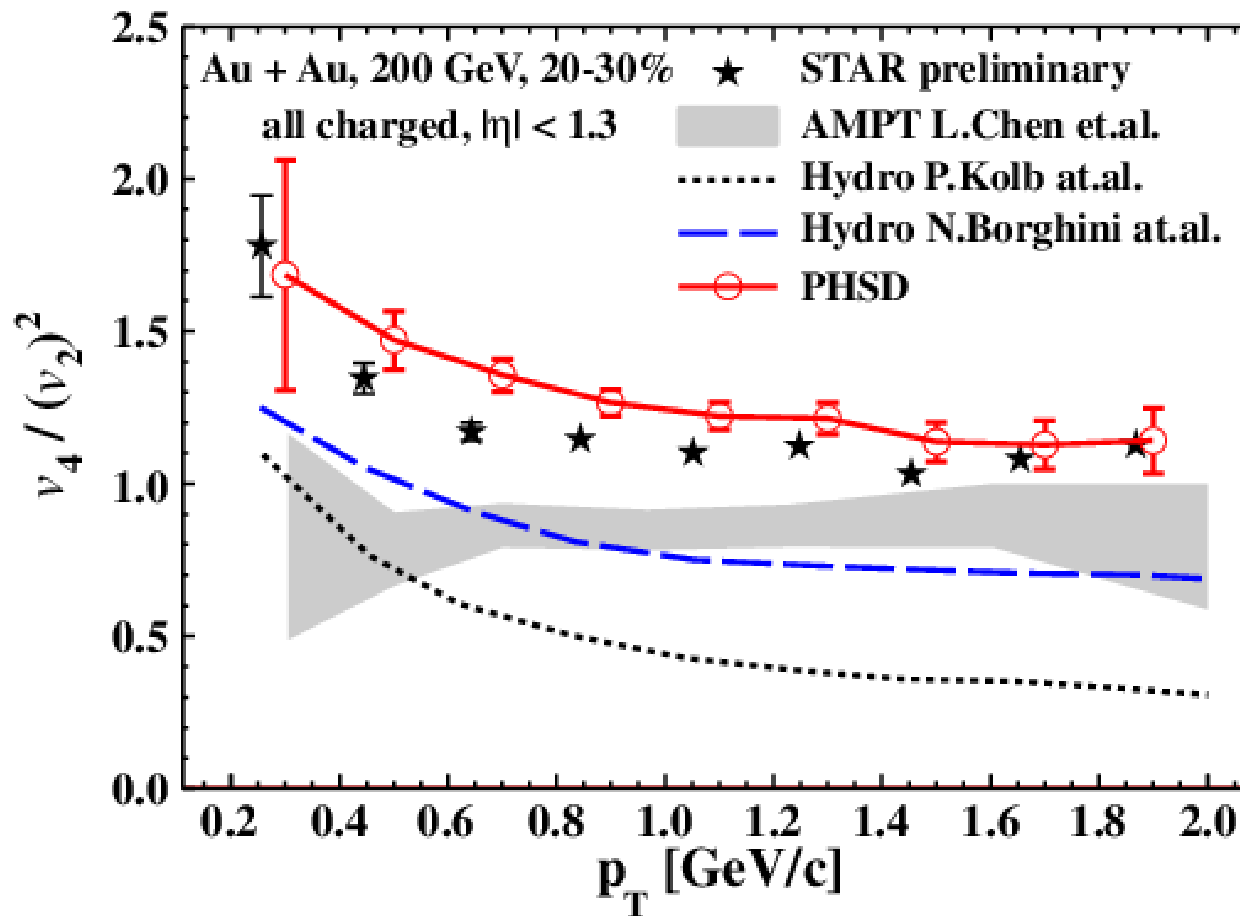
# Elliptic flow scaling at RHIC



- The mass splitting at low  $p_T$  is approximately reproduced as well as the meson-baryon splitting for  $p_T > 2 \text{ GeV}/c$  !
- The scaling of  $v_2$  with the number of constituent quarks  $n_q$  is roughly in line with the data .



# Ratio $v_4/(v_2)^2$ vs. $p_T$ at RHIC

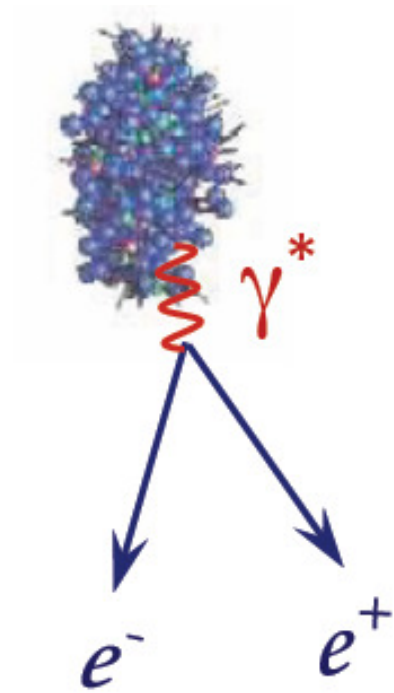


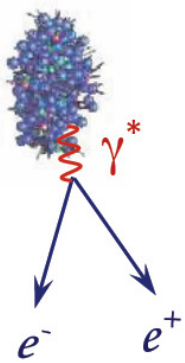
The ratio  $v_4/(v_2)^2$  :

□ is very sensitive to the microscopic dynamics

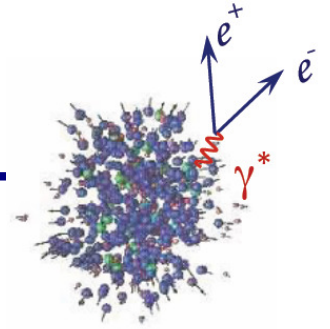
□ PHSD: ratio grows at low  $p_T$  - in line with exp. data

# Dileptons





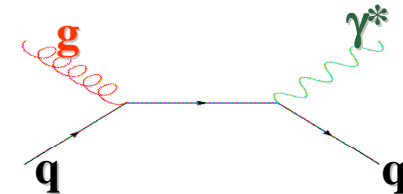
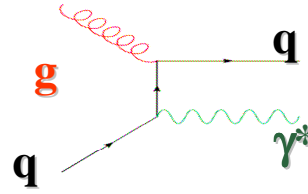
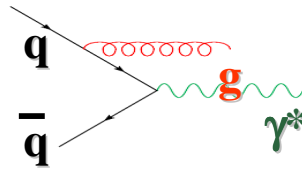
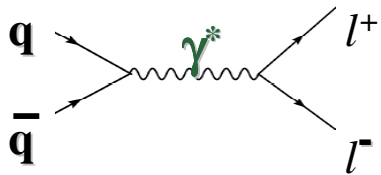
# Electromagnetic probes: dileptons and photons



➤ Dileptons are emitted from different stages of the reaction and not much effected by final-state interactions

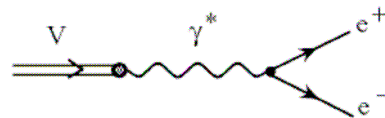
## Dilepton sources:

■ from the QGP via partonic (q,qbar, g) interactions:

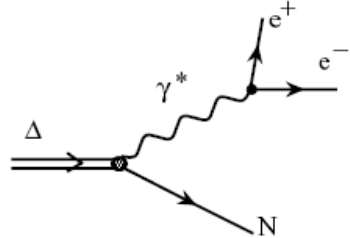


■ from hadronic sources:

• direct decay of vector mesons ( $\rho, \omega, \phi, J/\Psi, \Psi'$ )



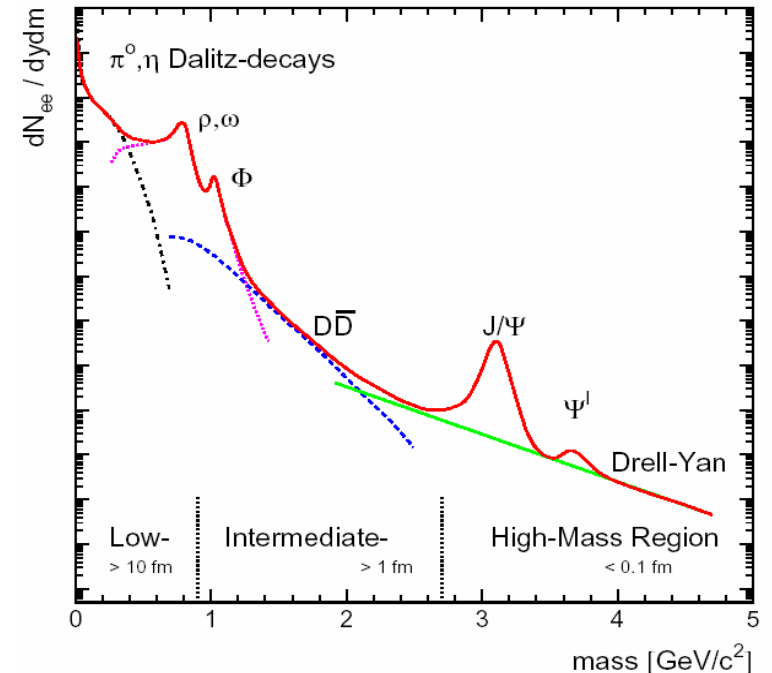
• Dalitz decay of mesons and baryons ( $\pi^0, \eta, \Delta, \dots$ )



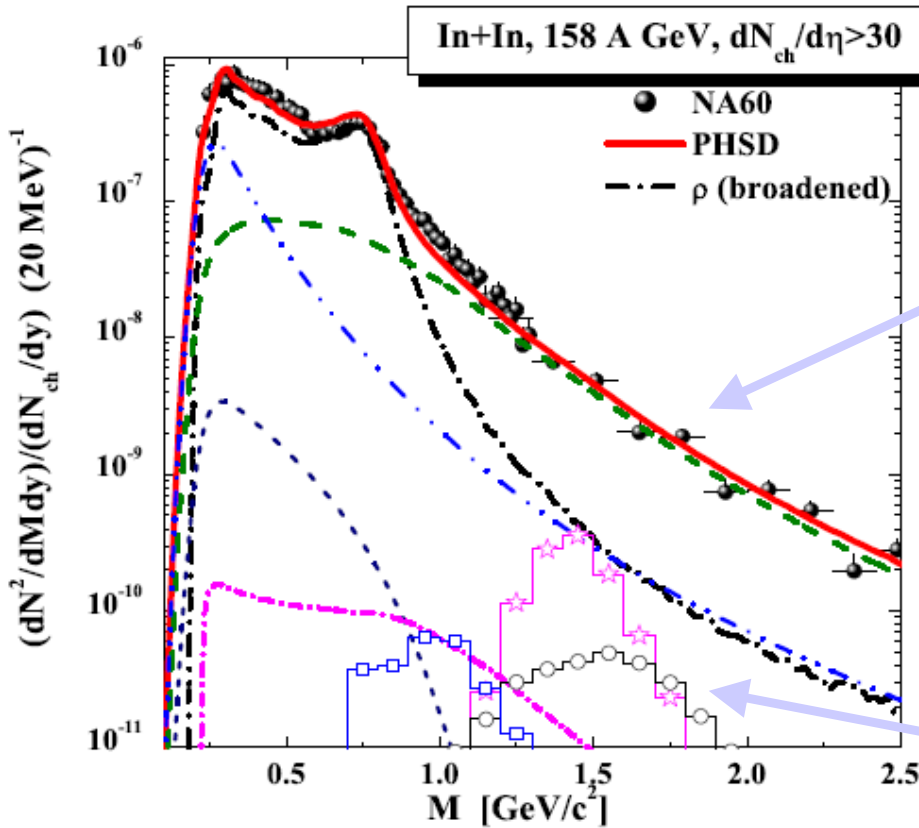
• correlated D+Dbar pairs

• radiation from multi-meson reactions ( $\pi+\pi, \pi+\rho, \pi+\omega, \rho+\rho, \pi+a_1$ ) - ,4π'

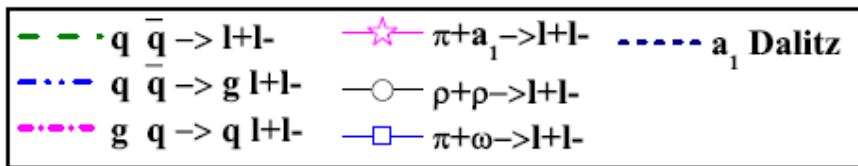
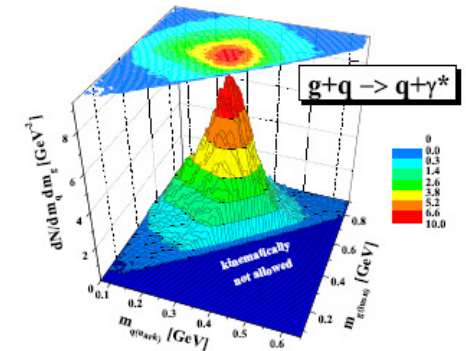
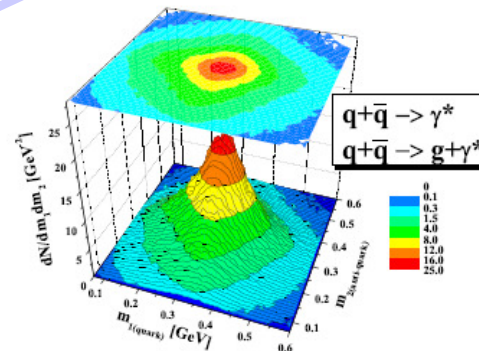
➔ Dileptons are an ideal probe to study the properties of the hot and dense medium



## Acceptance corrected NA60 data



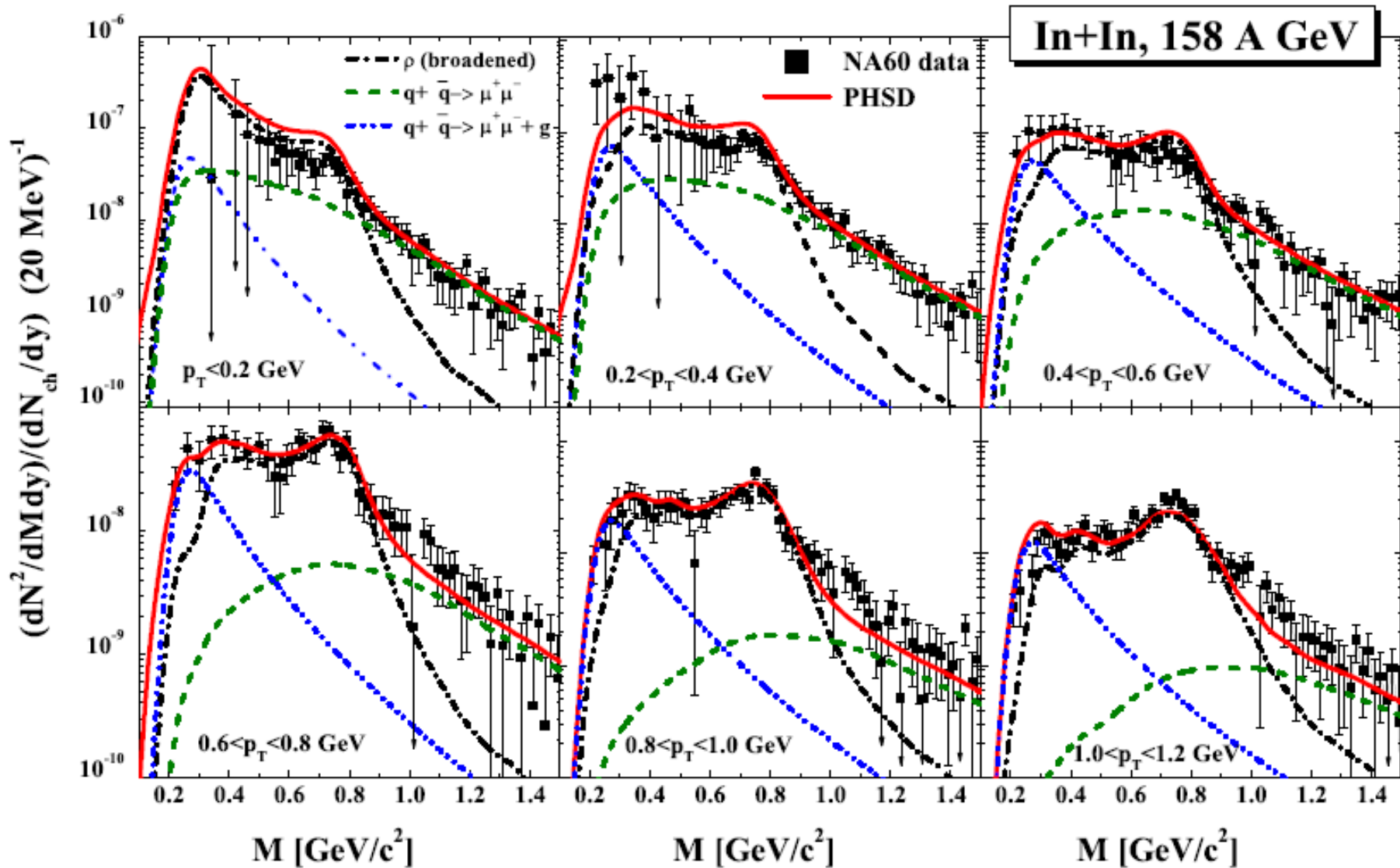
■ Mass region above 1 GeV is dominated by **partonic radiation** !



■ Contributions of **“4π”** channels (radiation from multi-meson reactions) are **small**



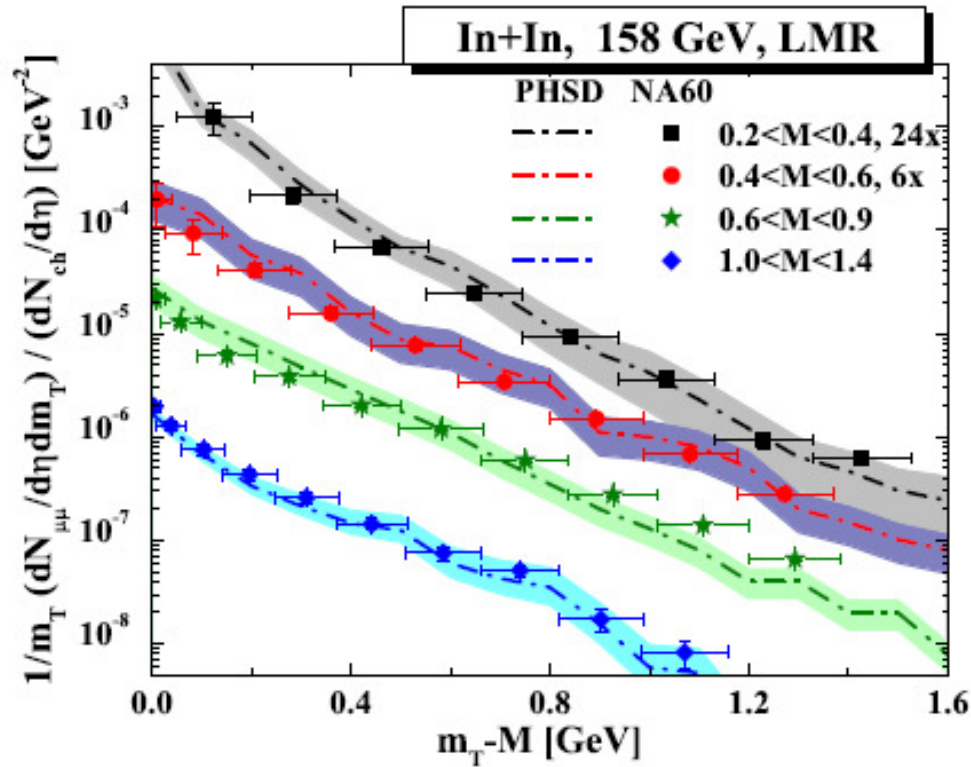
# Dileptons at SPS: NA60



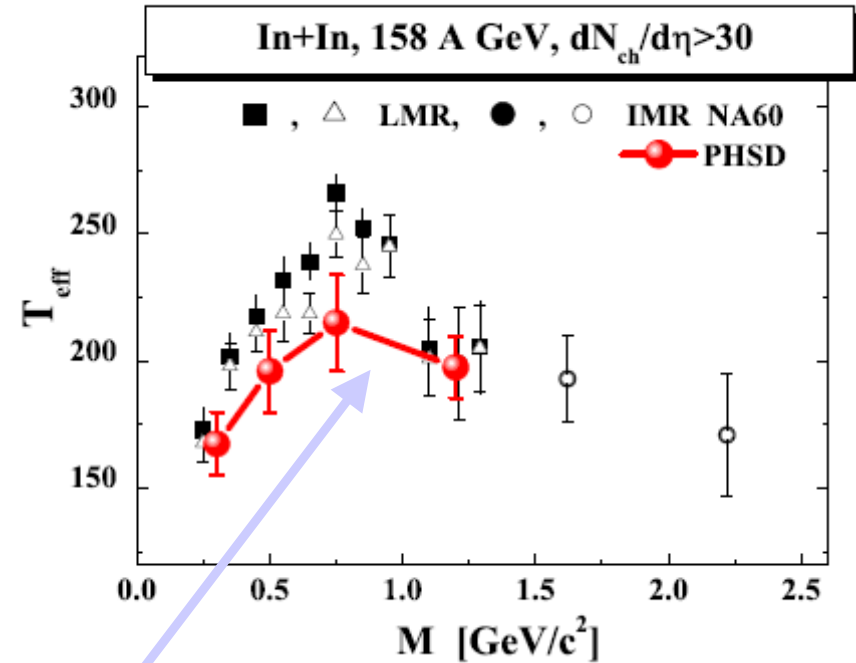
O. Linnyk, E.B., V. Ozvenchuk, W. Cassing  
and C.-M. Ko, PRC 84 (2011) 054917



# NA60: $m_T$ spectra



- Inverse slope parameter  $T_{\text{eff}}$  for dilepton spectra vs NA60 data

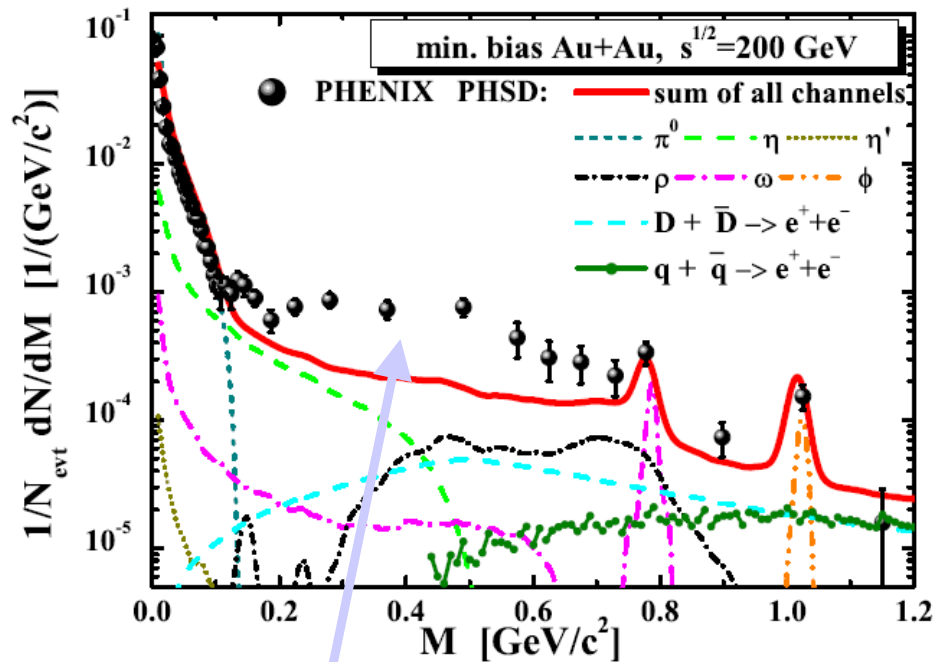


## Conjecture:

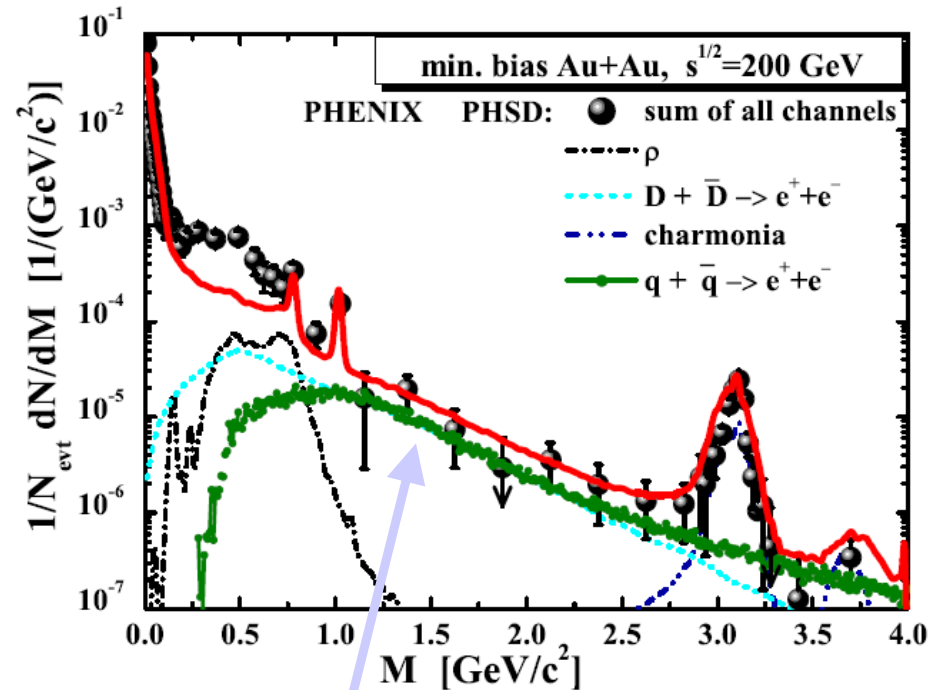
- spectrum from sQGP is softer than from hadronic phase since quark-antiquark annihilation occurs dominantly before the collective radial flow has developed (cf. NA60)



# PHENIX: dileptons from partonic channels



- The **excess** over the considered mesonic sources for  $M=0.15-0.6$  GeV is not explained by the QGP radiation as incorporated presently in PHSD

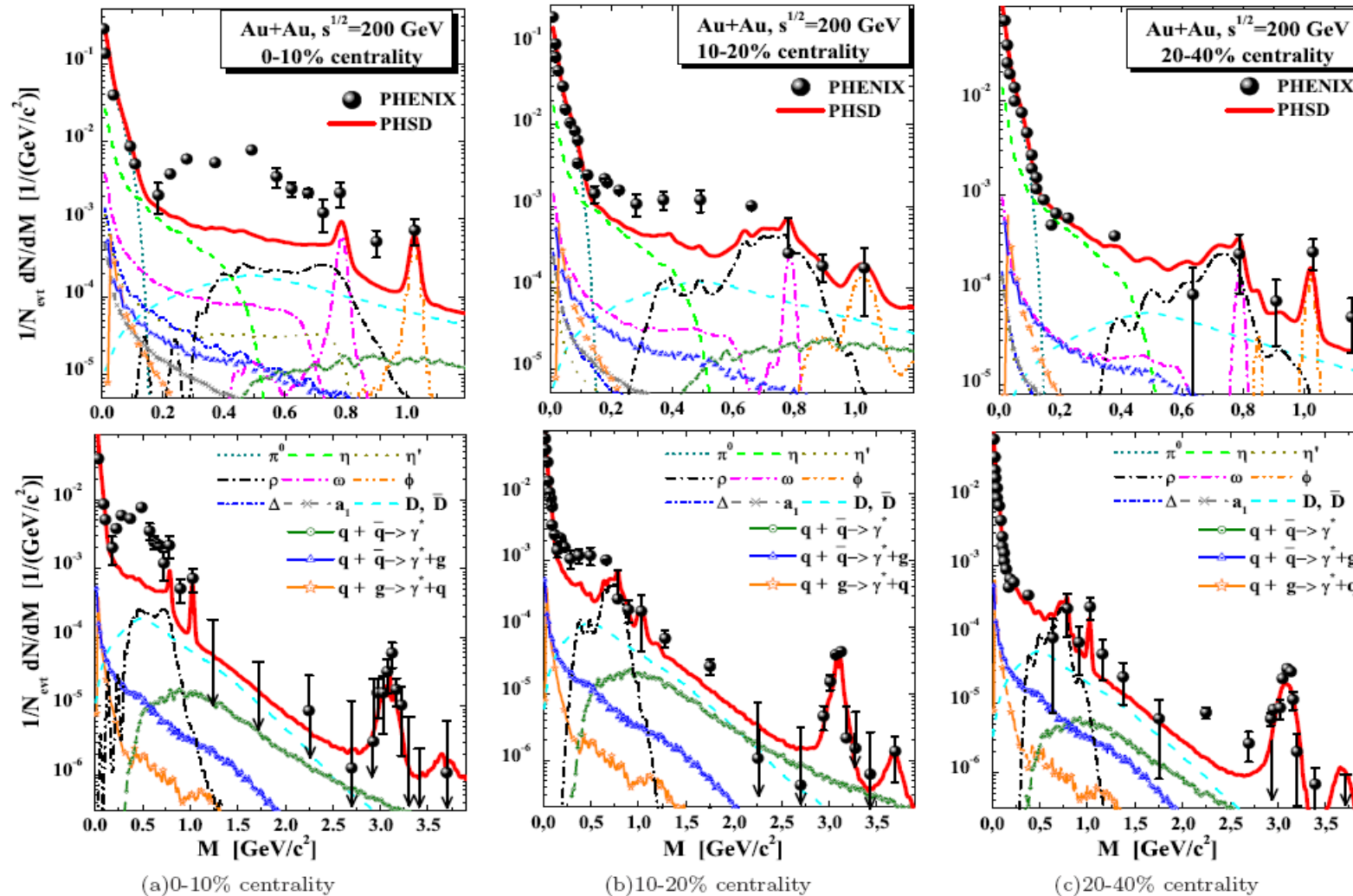


- The **partonic channels** fill up the discrepancy between the hadronic contributions and the data for  $M > 1$  GeV





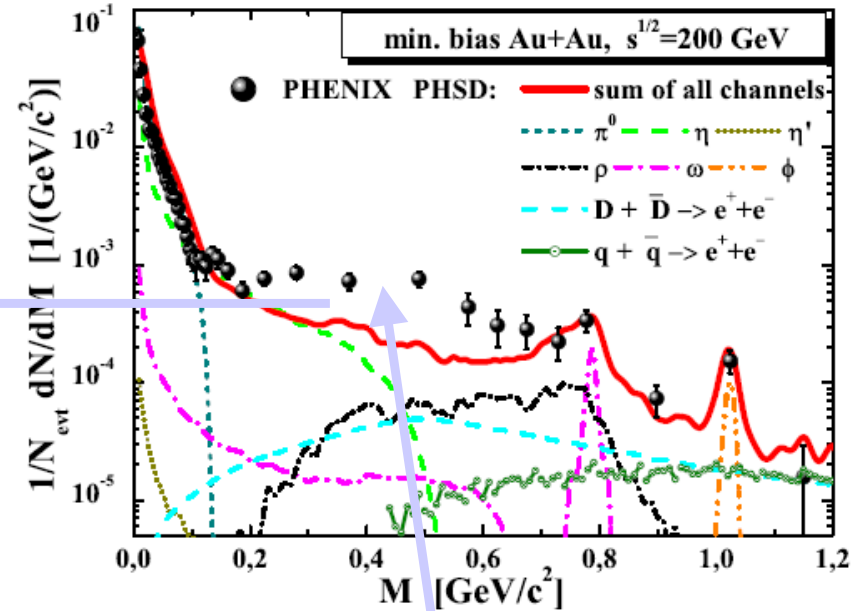
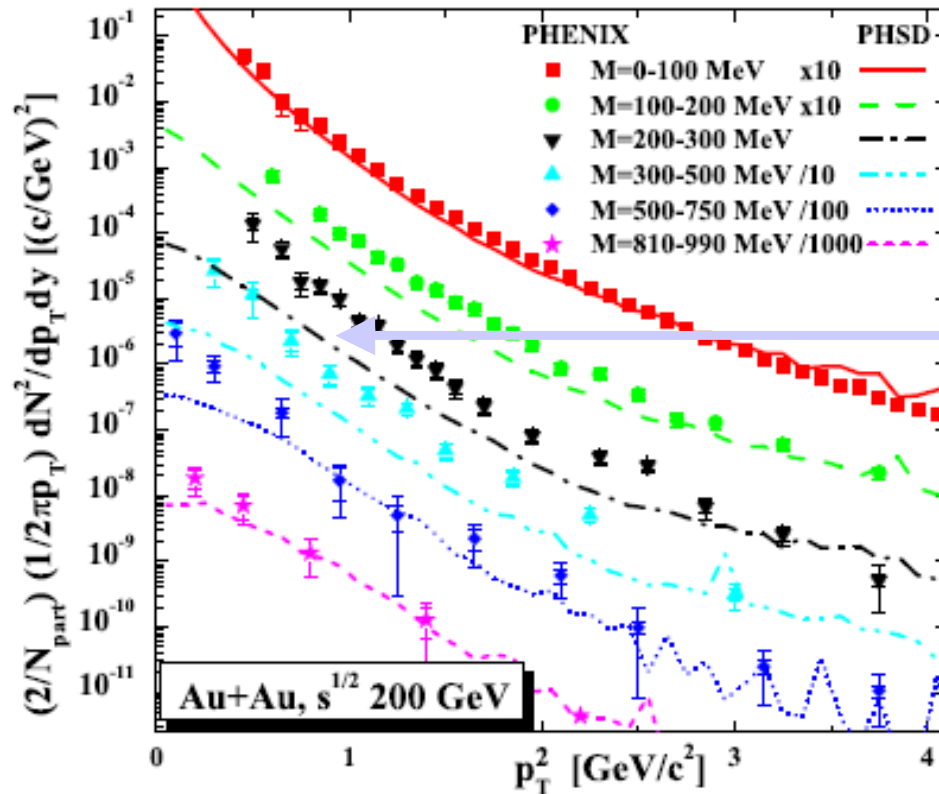
# PHENIX: mass spectra



- Peripheral collisions (and pp) are well described, however, central fail!



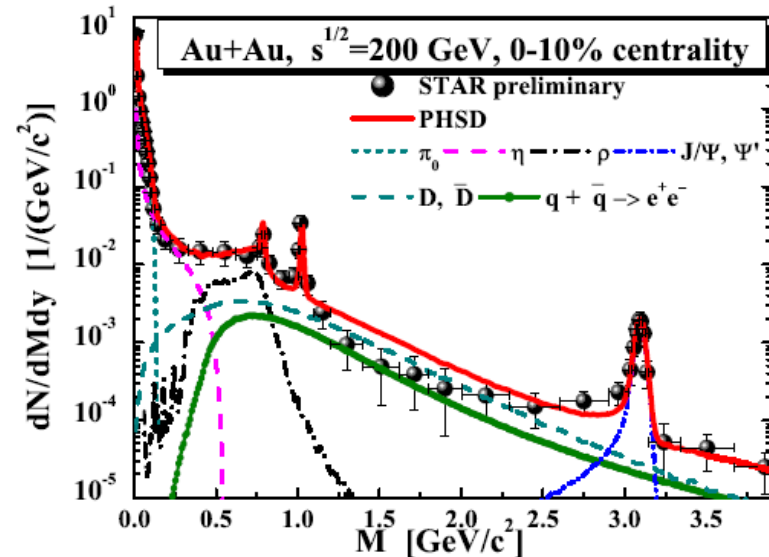
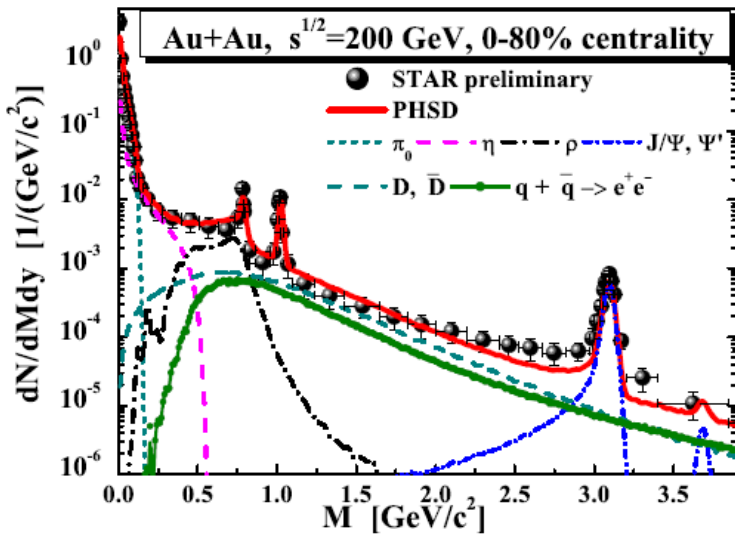
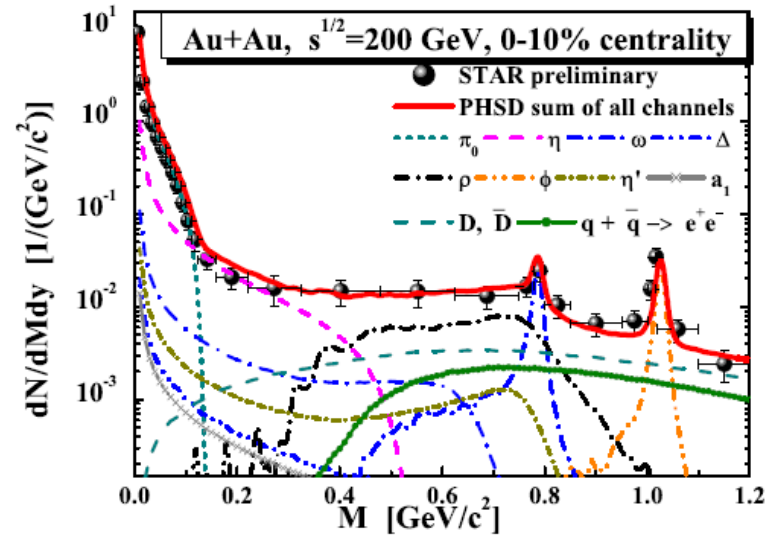
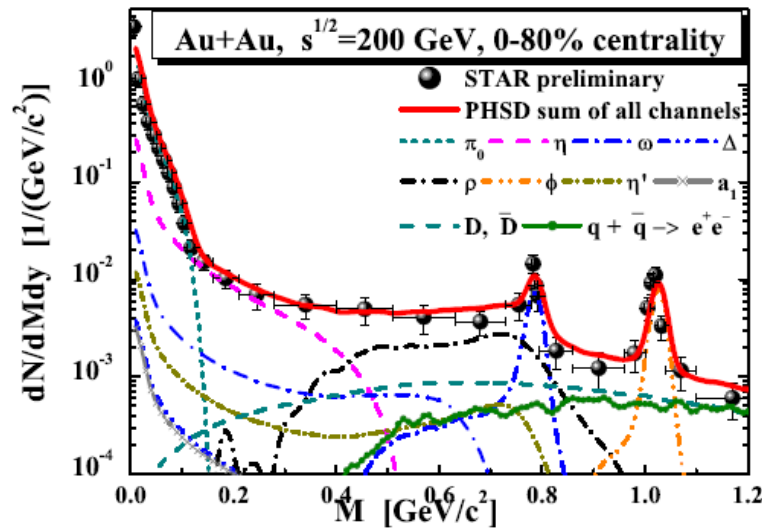
# PHENIX: $p_T$ spectra



- The lowest and highest mass bins are described very well
- Underestimation of  $p_T$  data for  $100 < M < 750$  MeV bins consistent with  $dN/dM$
- The ‘missing source’(?) is located at low  $p_T$  !



# STAR: mass spectra

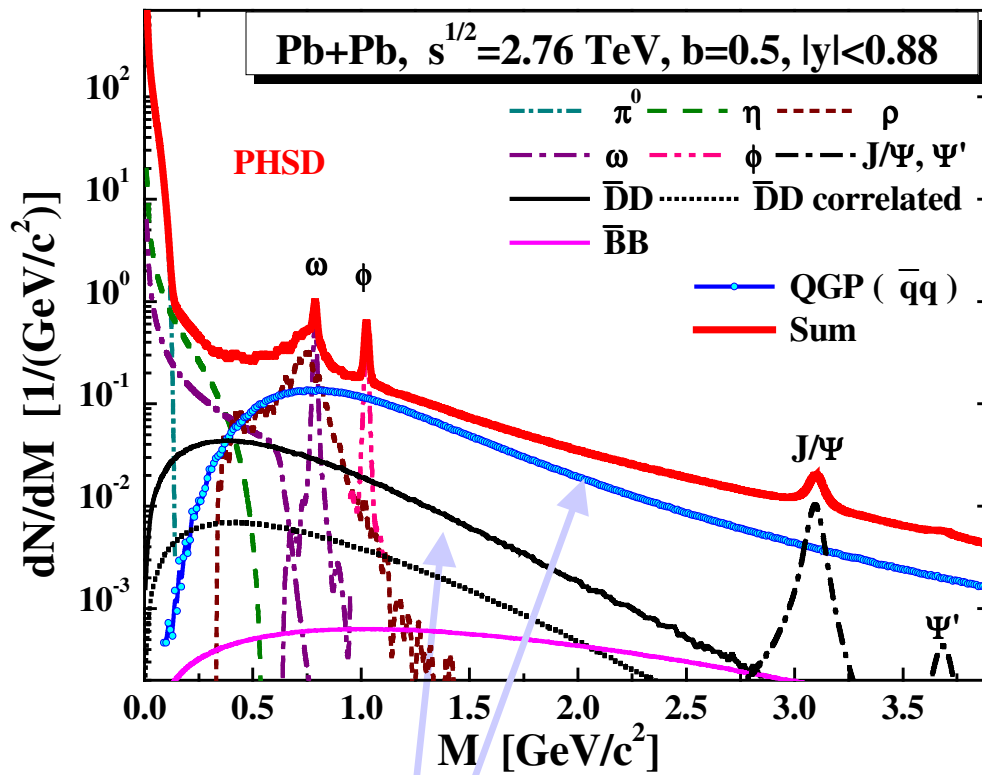


■ STAR data are well described!

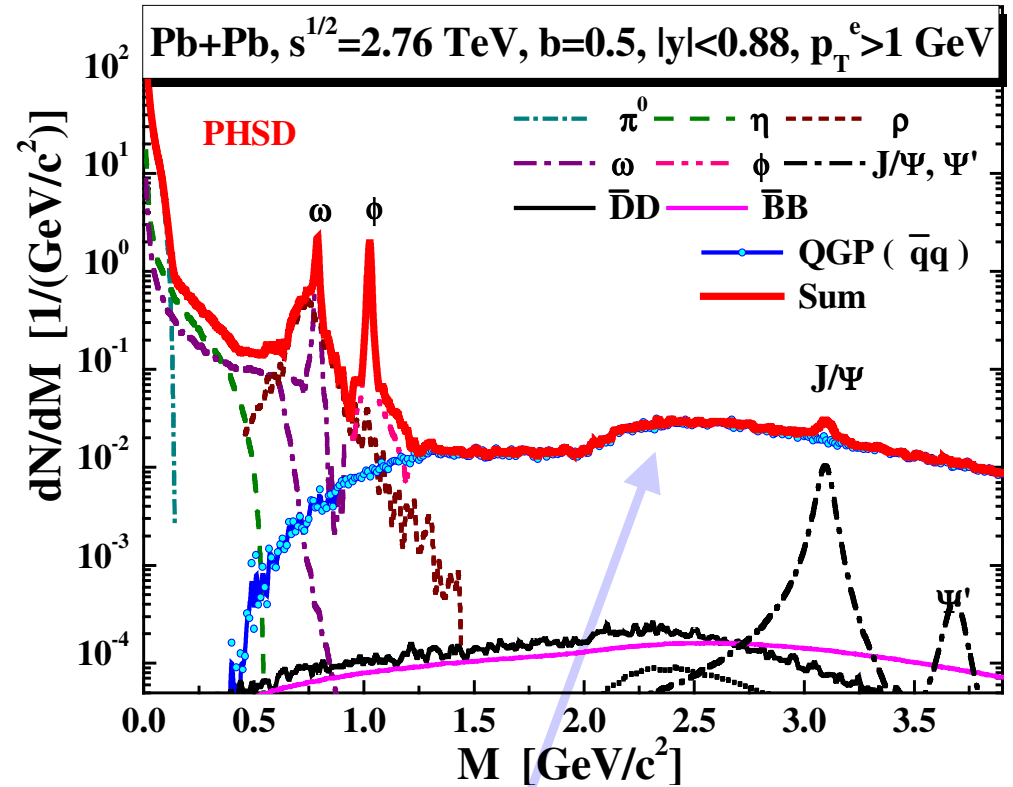
O. Linnyk, W. Cassing, J. Manninen, E.B. and C.-M. Ko,  
PRC 85 (2012) 024910



# Predictions for LHC



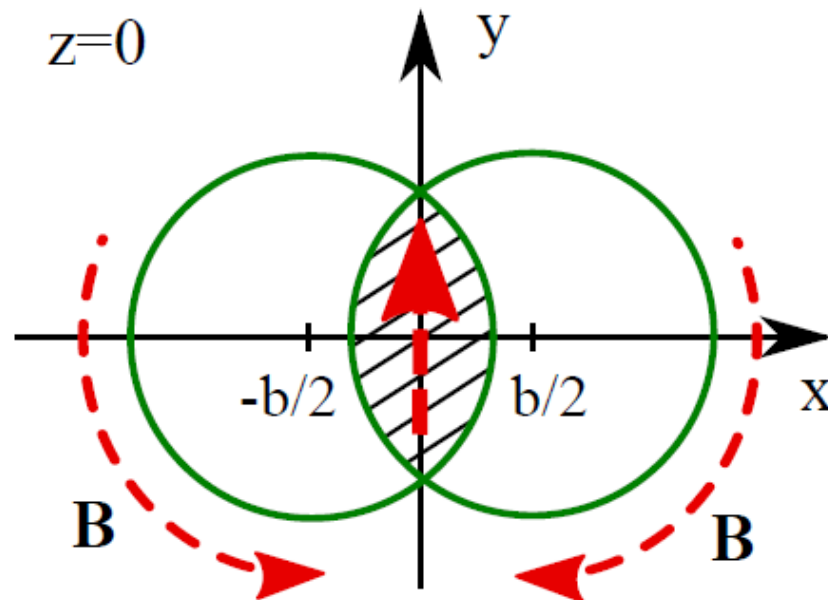
QGP( $\bar{q}q$ ) dominates at  $M > 1.2$  GeV



$p_T$  cut enhances the signal of QGP( $\bar{q}q$ )

- D-, B-mesons energy loss from Pol-Bernard Gossiaux and Jörg Aichelin
- J/ $\Psi$  and  $\Psi'$  nuclear modification from Che-Ming Ko and Taesoo Song

# Chiral magnetic effect and evolution of the electromagnetic field in relativistic heavy-ion collisions



# PHSD - transport model with electromagnetic fields

Generalized transport equations in the presence of electromagnetic fields :

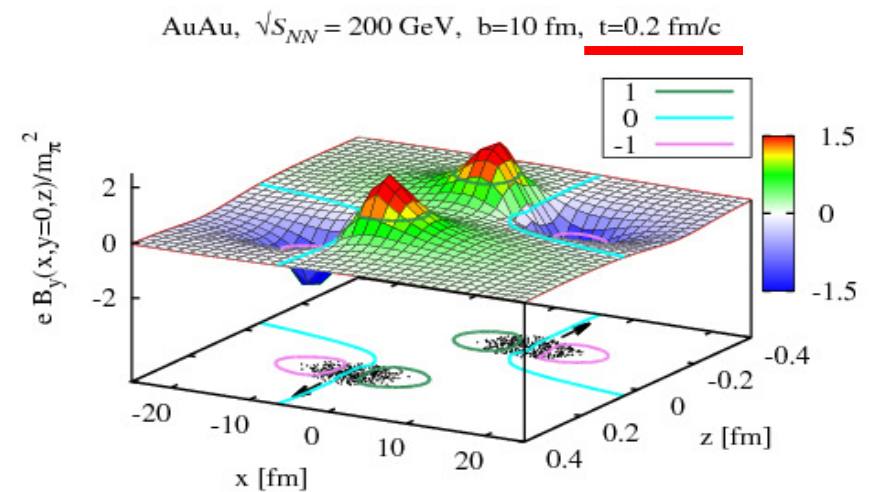
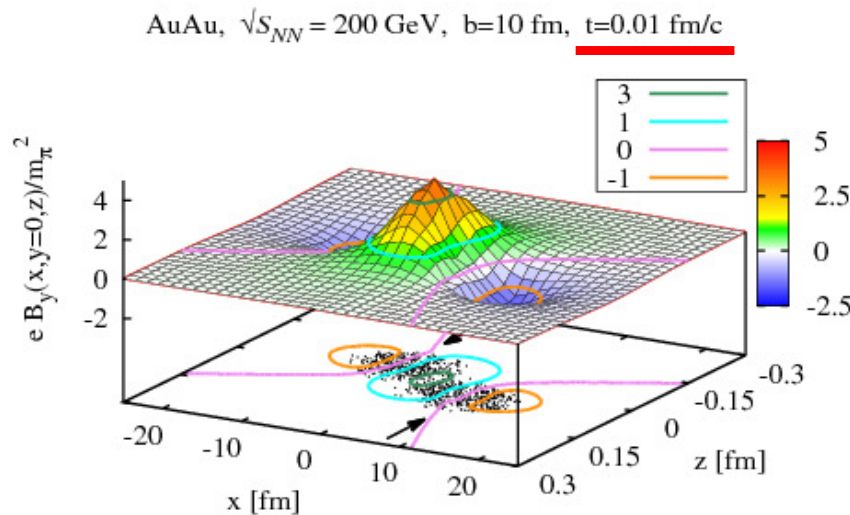
$$\left\{ \begin{array}{l} \dot{\vec{r}} \rightarrow \frac{\vec{p}}{p_0} + \vec{\nabla}_p U, \quad U \sim \text{Re}(\Sigma^{\text{ret}})/2p_0 \\ \dot{\vec{p}} \rightarrow -\vec{\nabla}_r U + e\vec{E} + e\vec{v} \times \vec{B} \end{array} \right.$$

$$\left\{ \begin{array}{l} \vec{B} = \vec{\nabla} \times \vec{A} \\ \vec{E} = -\vec{\nabla} \Phi - \frac{\partial \vec{A}}{\partial t} \end{array} \right.$$

$$\vec{A}(\vec{r}, t) = \frac{1}{4\pi} \int \frac{\vec{j}(\vec{r}', t') \delta(t - t' - |\vec{r} - \vec{r}'|/c)}{|\vec{r} - \vec{r}'|} d^3r' dt'$$

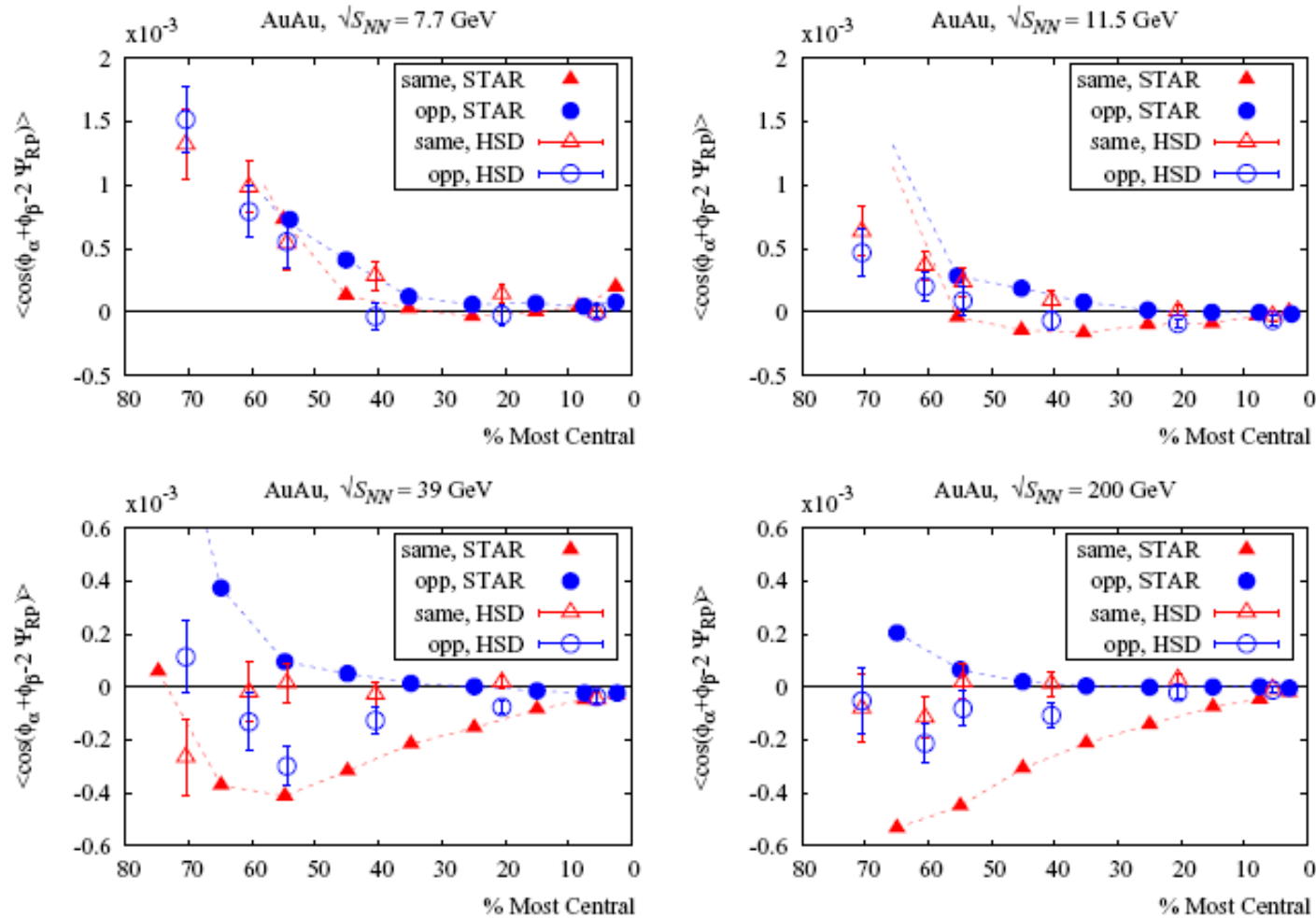
$$\Phi(\vec{r}, t) = \frac{1}{4\pi} \int \frac{\rho(\vec{r}', t') \delta(t - t' - |\vec{r} - \vec{r}'|/c)}{|\vec{r} - \vec{r}'|} d^3r' dt'$$

## ■ Magnetic field evolution in HSD/PHSD :



# Angular correlation wrt. reaction plane

$$\langle \cos(\psi_\alpha + \psi_\beta - 2\Psi_{RP}) \rangle$$

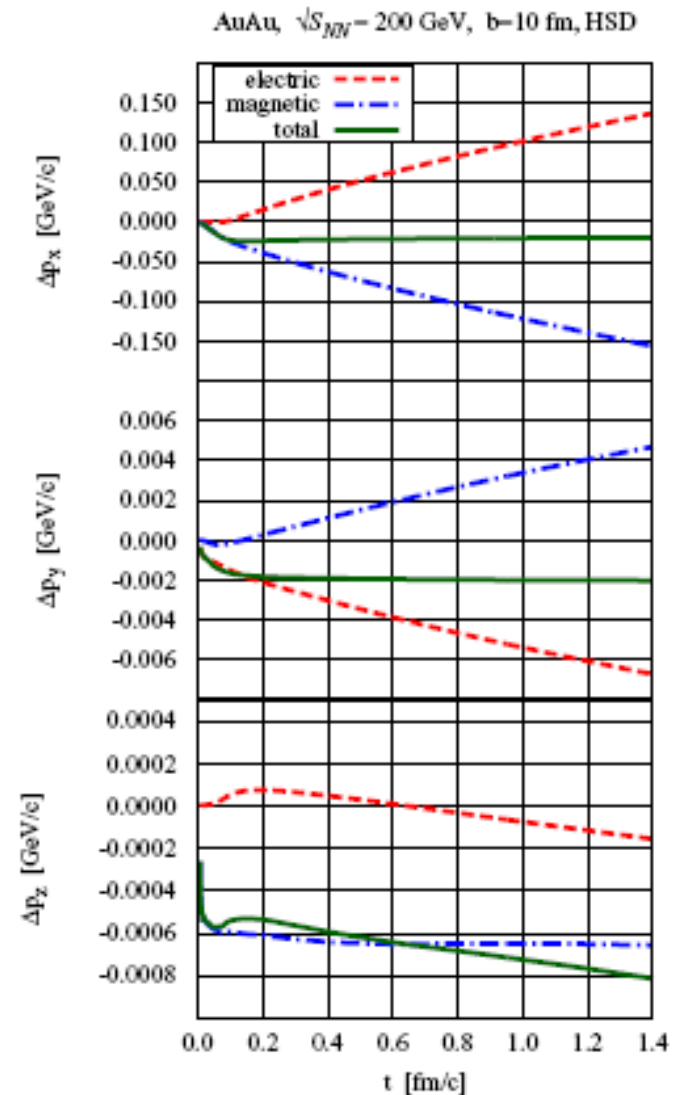
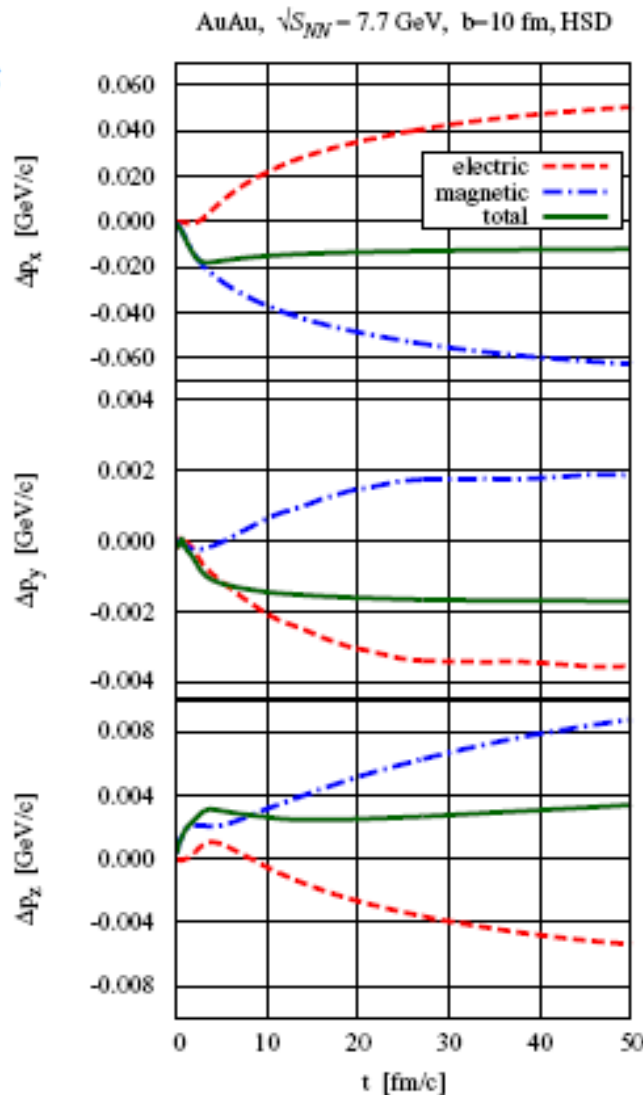


Angular correlation is of hadronic origin up to  $\sqrt{s} = 11$  GeV !

# Compensation of magnetic and electric forces

## Forces

$$\dot{\vec{p}} \rightarrow e\vec{E} + e\vec{v} \times \vec{B}$$



There are not only strong magnetic forces but also strong electric forces which compensate each other!





# Summary

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- **PHSD** provides a consistent description of **off-shell parton dynamics** in line with the **lattice QCD equation of state** (from the BMW collaboration)

- **PHSD** versus **experimental observables**:

  - enhancement of meson  $m_T$  slopes (at top SPS and RHIC)

  - strange antibaryon enhancement (at SPS)

  - partonic emission of high mass dileptons at SPS and RHIC

  - enhancement of collective flow  $v_2$  with increasing energy

  - quark number scaling of  $v_2$  (at RHIC)

  - jet suppression

  - ...

⇒ **evidence for strong nonhadronic interactions in the early phase of relativistic heavy-ion reactions**

⇒ **formation of the sQGP**



# PHSD group

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