



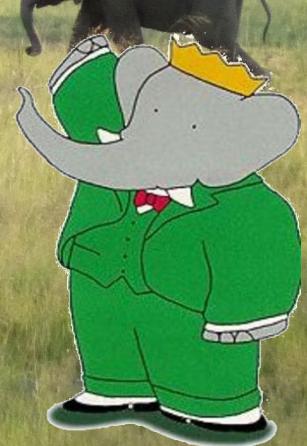
UNIVERSITÀ
DEGLI STUDI
DI PADOVA

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First Direct Observation of
Time Reversal Violation in B System
and Other CPV Measurements at BABAR

INTERNATIONAL WORKSHOP ON DISCOVERY PHYSICS AT THE LHC
KRUGER 2012
DECEMBER 3 - 7, 2012

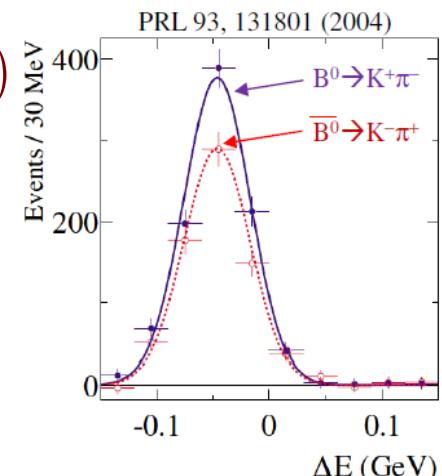


BABAR take on CP Violation

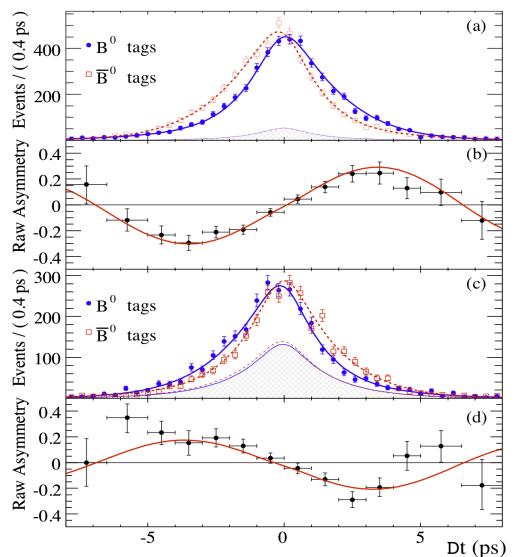
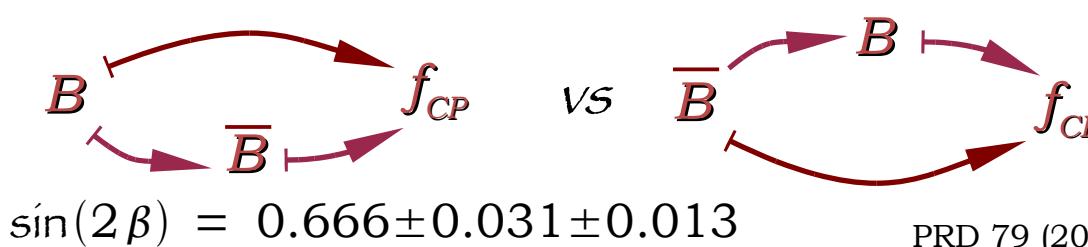
- First Observation of Direct CPV: $\Gamma(\bar{B} \rightarrow f) \neq \Gamma(B \rightarrow \bar{f})$

$$\frac{\Gamma(\bar{B}^0 \rightarrow K^- \pi^+) - \Gamma(B^0 \rightarrow K^+ \pi^-)}{\Gamma(\bar{B}^0 \rightarrow K^- \pi^+) + \Gamma(B^0 \rightarrow K^+ \pi^-)} = -0.133 \pm 0.030 \pm 0.009$$

PRL 93.131801



- CPV in interference of mixing and decay



- Not yet observed in mixing alone

$$\mathcal{A}_{ee}(B^0) = \frac{N(B^0 \bar{B}^0) - N(\bar{B}^0 \bar{B}^0)}{N(B^0 \bar{B}^0) + N(\bar{B}^0 \bar{B}^0)} = (-0.05 \pm 0.56)\%$$

B-Factories ICHEP 2012

- ➊ CPV is well established
- ➋ CPT + CPV \longmapsto T Violation
 - (1.a) Can we assert T Violation independently of CPT assumption ?
 - (1.b) Can we test CPT in the B system ?
- ➌ CP in mixing has not yet been observed
 - (2) Can we improve wrt existing measurements ?
- ➍ CP measurements provide precise value for the CKM parameter β
 - (3) What can we say for the other CKM angles ?



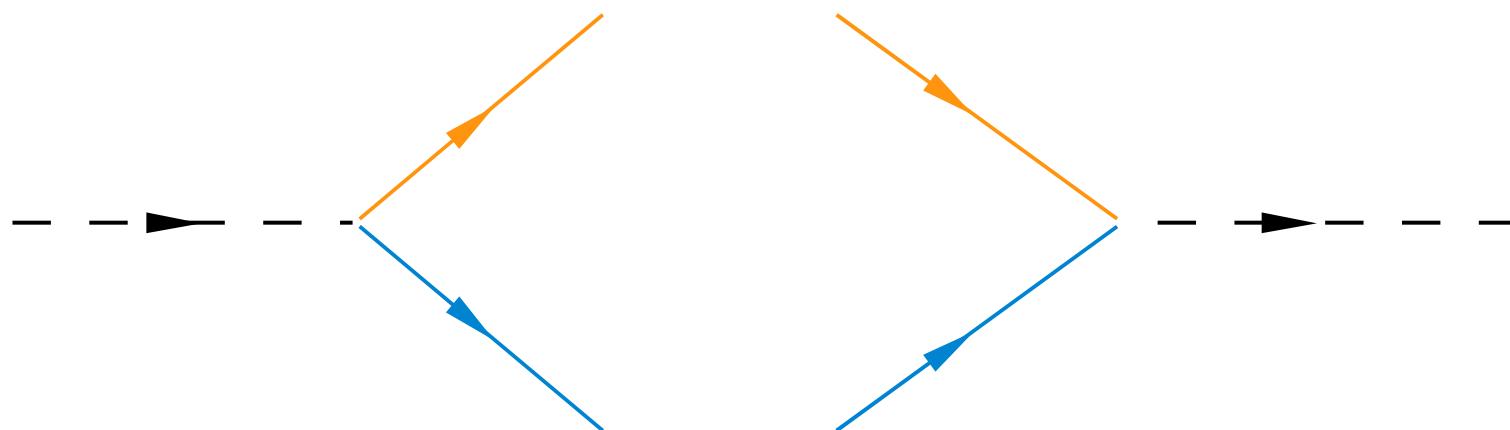
PART I

Discovering T-Violation (and testing CPT)

Direct Measurement of T Violation

- Ideally compare two time-conjugate processes

$$\mathcal{M}(B^0 \rightarrow K^+ \pi^-) \quad \text{vs} \quad \mathcal{M}(K^+ \pi^- \rightarrow B^0)$$



- Unfeasible:

- tiny effects
- swamped by strong interactions

- In practice, exploit EPR entanglement in $B\bar{B}$ production at $Y(4S)$

$$e^+ e^- \rightarrow Y(4S) \rightarrow b\bar{b}$$

$$J^{PC} = 1^{--}$$

Direct Measurement of T Violation

- In practice, exploit EPR entanglement in $B\bar{B}$ production at $Y(4S)$

$$e^+ e^- \rightarrow Y(4S) \rightarrow b\bar{b}$$

$$J^{PC} = 1^{--}$$

$$\rightarrow \frac{1}{\sqrt{2}}(\mathbb{B}^0(t_1)\overline{\mathbb{B}^0}(t_2) - \mathbb{B}^0(t_2)\overline{\mathbb{B}^0}(t_1))$$

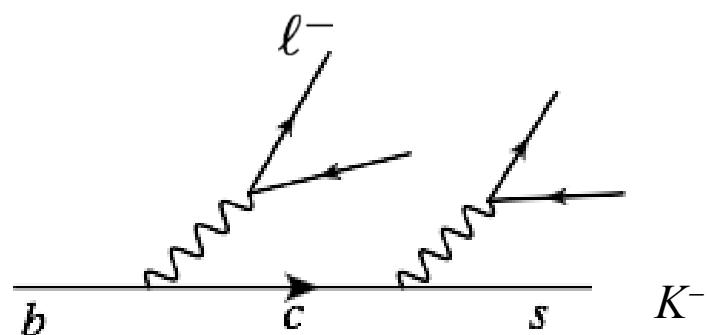
flavor eigenstate: $\mathbb{B}^0 = \begin{pmatrix} b \\ d \end{pmatrix}$

- Flavor tagged by same means as CP analyses :

$$\overline{\mathbb{B}^0} \rightarrow \ell^- X$$

$$\overline{\mathbb{B}^0} \rightarrow K^- X$$

$$\overline{\mathbb{B}^0} \rightarrow \pi_{\text{soft}}^+ X, \dots$$



- In practice, exploit EPR entanglement in $B\bar{B}$ production at $Y(4S)$

$$e^+ e^- \rightarrow Y(4S) \rightarrow b\bar{b}$$

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$$\rightarrow \frac{1}{\sqrt{2}}(\mathbb{I}\mathcal{B}^0(t_1)\overline{\mathcal{B}^0}(t_2) - \mathbb{I}\mathcal{B}^0(t_2)\overline{\mathcal{B}^0}(t_1))$$

flavor eigenstate: $\mathcal{B}^0 = \begin{pmatrix} b \\ d \end{pmatrix}$

$$\rightarrow \frac{1}{\sqrt{2}}(\mathbb{I}\mathcal{B}_+(t_1)\mathcal{B}_-(t_2) - \mathbb{I}\mathcal{B}_+(t_2)\mathcal{B}_-(t_1))$$

CP eigenstate: $CP|\mathcal{B}_\pm\rangle = \pm |\mathcal{B}_\pm\rangle$

- $B_{+,-}$ decay to CP eigenstates

$$\mathcal{B}_+ \rightarrow J/\psi K_L$$

$$\mathcal{B}_- \rightarrow (c\bar{c})K_S$$



- In practice, exploit EPR entanglement in $B\bar{B}$ production at $Y(4S)$

$$e^+ e^- \rightarrow Y(4S) \rightarrow b\bar{b}$$

$$J^{PC} = 1^{--}$$

$$\rightarrow \frac{1}{\sqrt{2}}(\mathbb{I}\mathcal{B}^0(t_1)\overline{\mathcal{B}^0}(t_2) - \mathbb{I}\mathcal{B}^0(t_2)\overline{\mathcal{B}^0}(t_1))$$

flavor eigenstate: $\mathcal{B}^0 = \begin{pmatrix} b \\ d \end{pmatrix}$

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CP eigenstate: $CP|\mathcal{B}_\pm\rangle = \pm |\mathcal{B}_\pm\rangle$

- Perform 4 complementary tests:

$$\mathcal{B}_+ \rightarrow \mathcal{B}^0 \quad \text{vs} \quad \mathcal{B}^0 \rightarrow \mathcal{B}_+$$

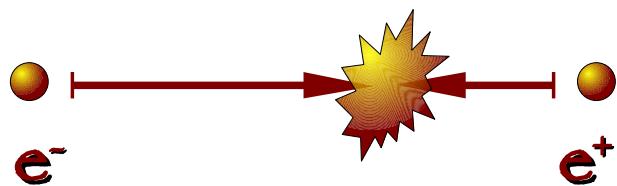
$$\mathcal{B}_- \rightarrow \mathcal{B}^0 \quad \text{vs} \quad \mathcal{B}^0 \rightarrow \mathcal{B}_-$$

$$\mathcal{B}_- \rightarrow \overline{\mathcal{B}^0} \quad \text{vs} \quad \overline{\mathcal{B}^0} \rightarrow \mathcal{B}_-$$

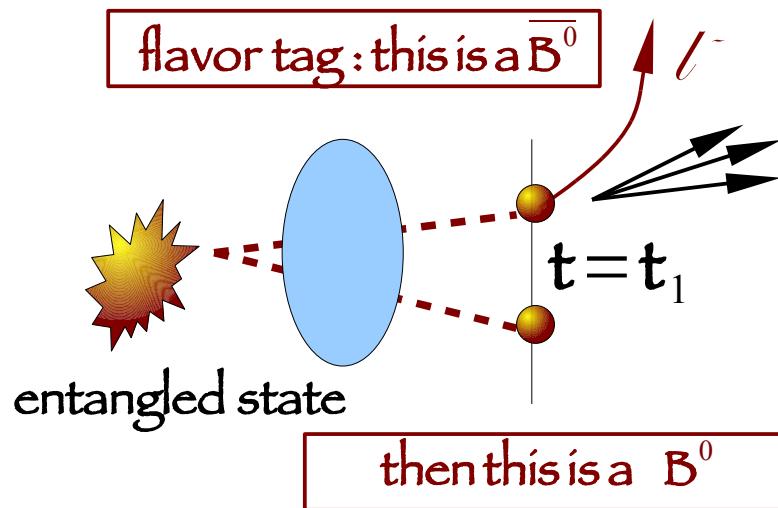
$$\mathcal{B}_+ \rightarrow \overline{\mathcal{B}^0} \quad \text{vs} \quad \overline{\mathcal{B}^0} \rightarrow \mathcal{B}_+$$

- ... plus tests of CPT and CP

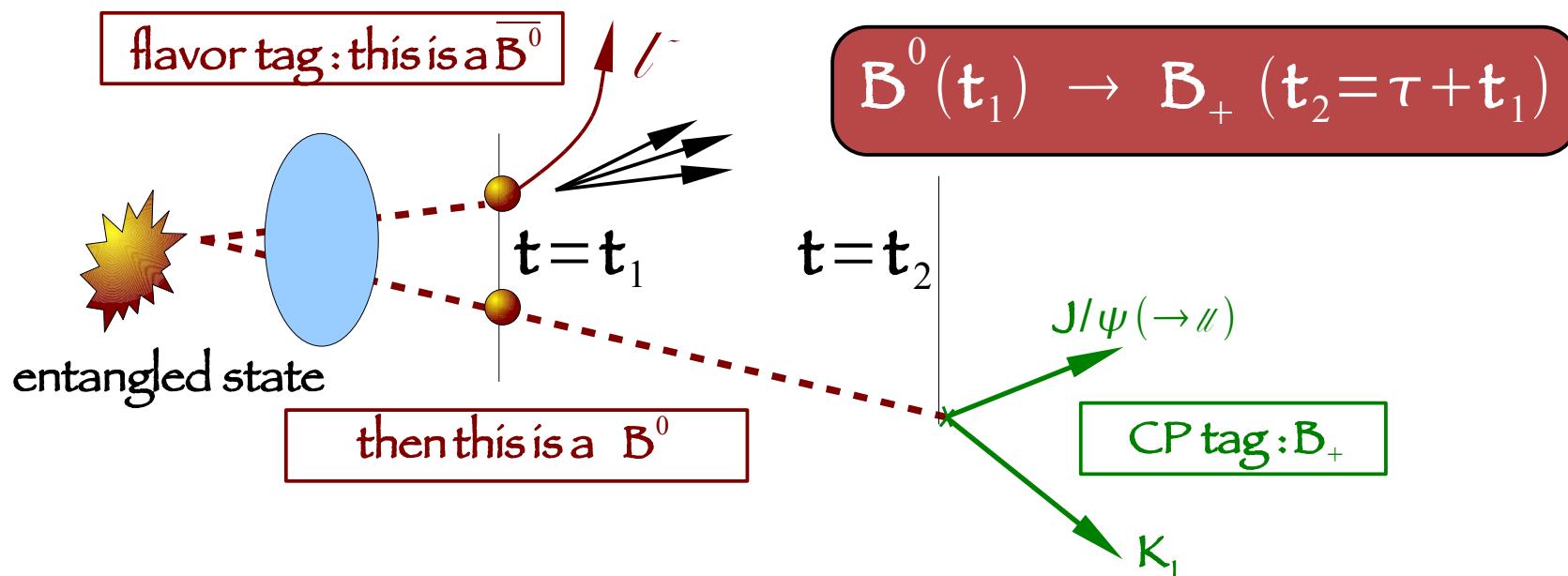
boosted $\Upsilon(4S)$ ($\beta\gamma \approx 0.56$)



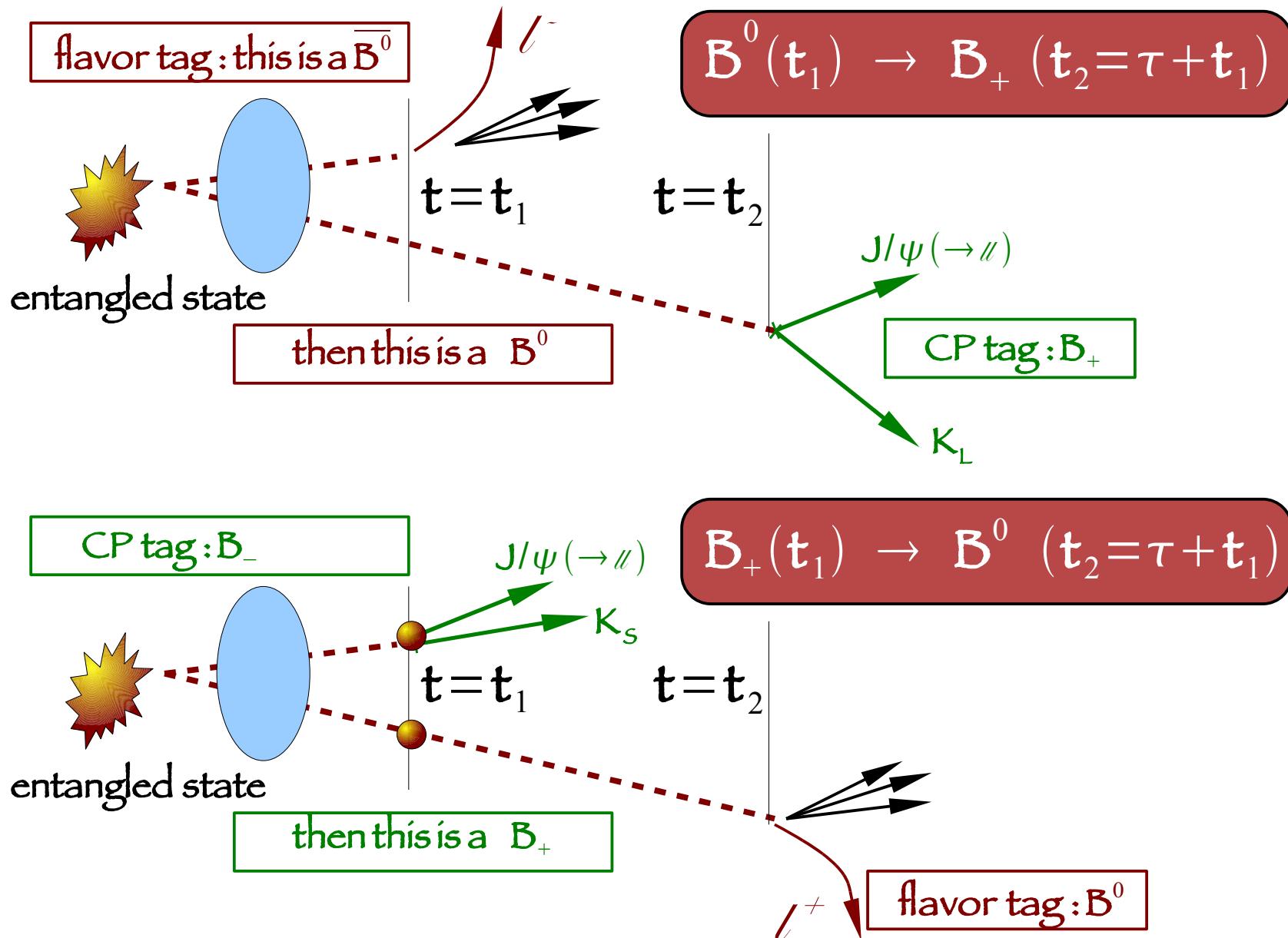
T Analysis in a nutshell



T Analysis in a nutshell



τ Analysis in a nutshell



TV analysis steps

- Define $\Delta\tau \approx t(\text{flavor}) - t(\text{CP})$
- $\alpha = B^0/\bar{B}^0$
- Consider eight combinations (flavor \times CP \times sign of $\Delta\tau$)
- Fit each with EPR-motivated function
- $\beta = K_L/K_S$

$$g_{\alpha,\beta}^{\pm}(\Delta\tau) \propto e^{-\Gamma|\Delta\tau|} \mathcal{H}(\pm\Delta\tau) [1 + S_{\alpha,\beta}^{\pm} \sin(\Delta m_d \Delta\tau) + C_{\alpha,\beta}^{\pm} \cos(\Delta m_d \Delta\tau)]$$

Heavyside step function

- $S_{\alpha\beta}^+$, $C_{\alpha\beta}^+$: fit parameters
- T-Violation : $\Delta S_T^+ = S_{B^0, K_L}^+ - S_{B^0, K_S}^+ \neq 0$
- CP-Violation : $\Delta S_{CP}^- = S_{B^0, K_L}^- - S_{B^0, K_S}^- \neq 0$
- CPT-Violation : $\Delta S_{CPT}^- = S_{B^0, K_S}^- - S_{B^0, K_L}^- \neq 0$
- Assuming CPT & CP fit results, expect :

$$S_{T,\alpha,\beta}^{\pm} = \pm \sin(2\beta)$$

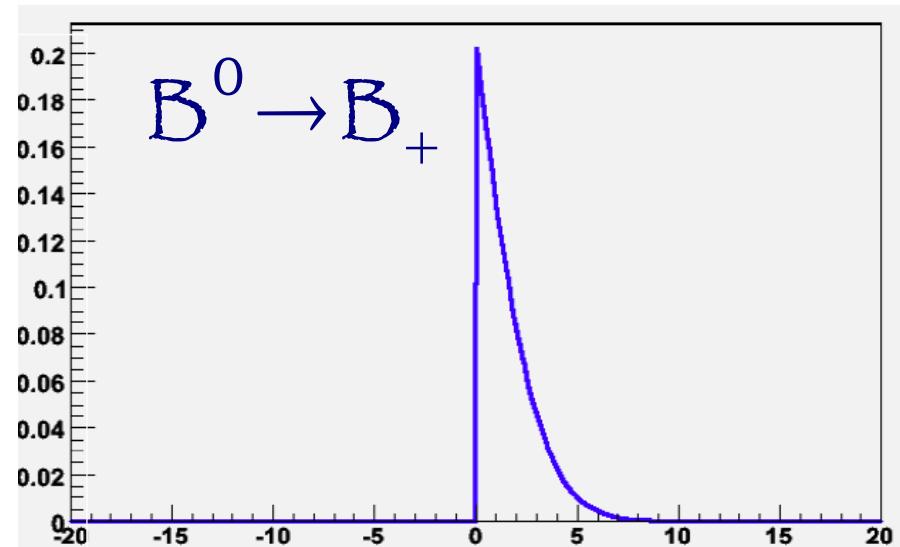
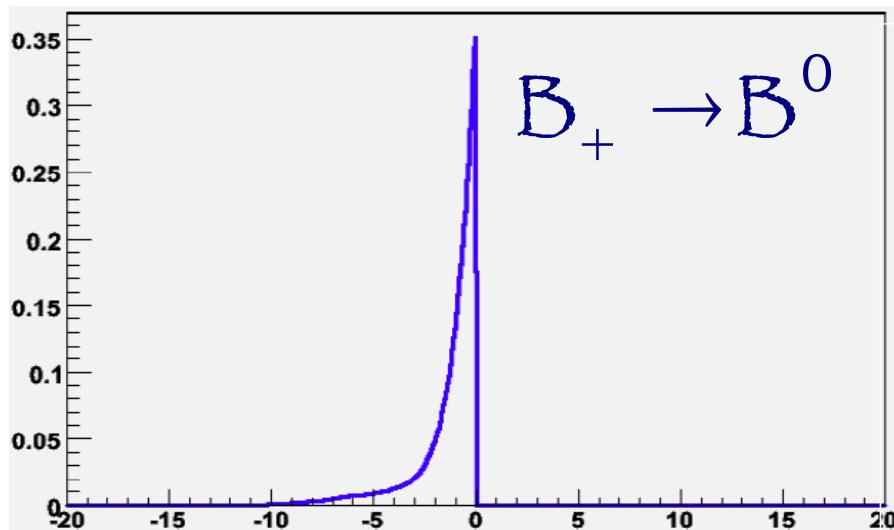
$$\Delta S_T^{\pm} = 2 \sin(2\beta)$$

TV analysis steps

- Define $\Delta\tau = t(\text{flavor}) - t(\text{CP})$
- Consider eight combinations (flavor (α) \times CP (β) \times sign of $\Delta\tau$)
- Fit each with EPR-motivated function

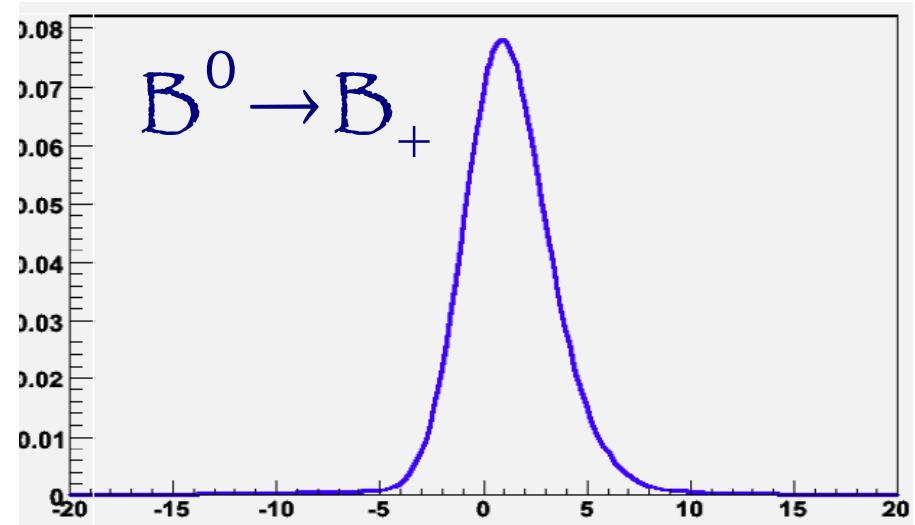
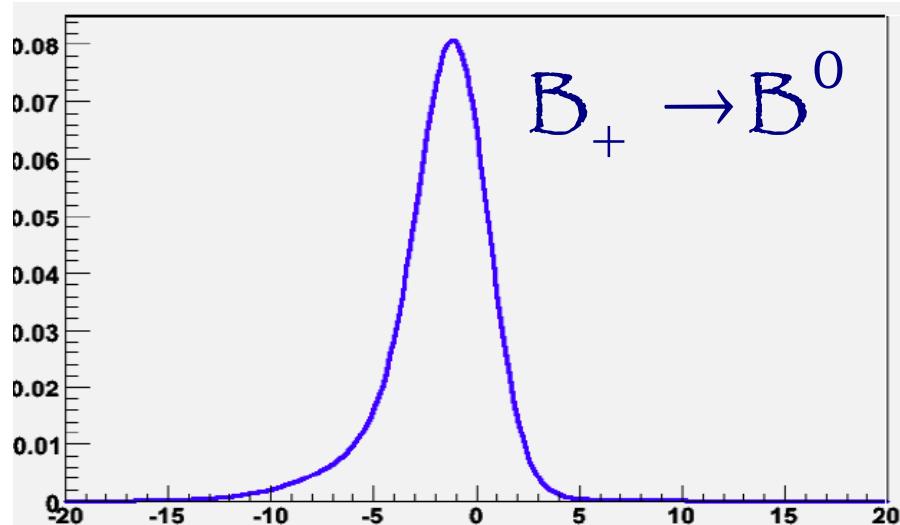
$$g_{\alpha,\beta}^{\pm}(\Delta\tau) \propto e^{-\Gamma|\Delta\tau|} \mathcal{H}(\pm\Delta\tau) [1 + S_{\alpha,\beta}^{\pm} \sin(\Delta m_d \Delta\tau) + C_{\alpha,\beta}^{\pm} \cos(\Delta m_d \Delta\tau)]$$

► Heavyside step function

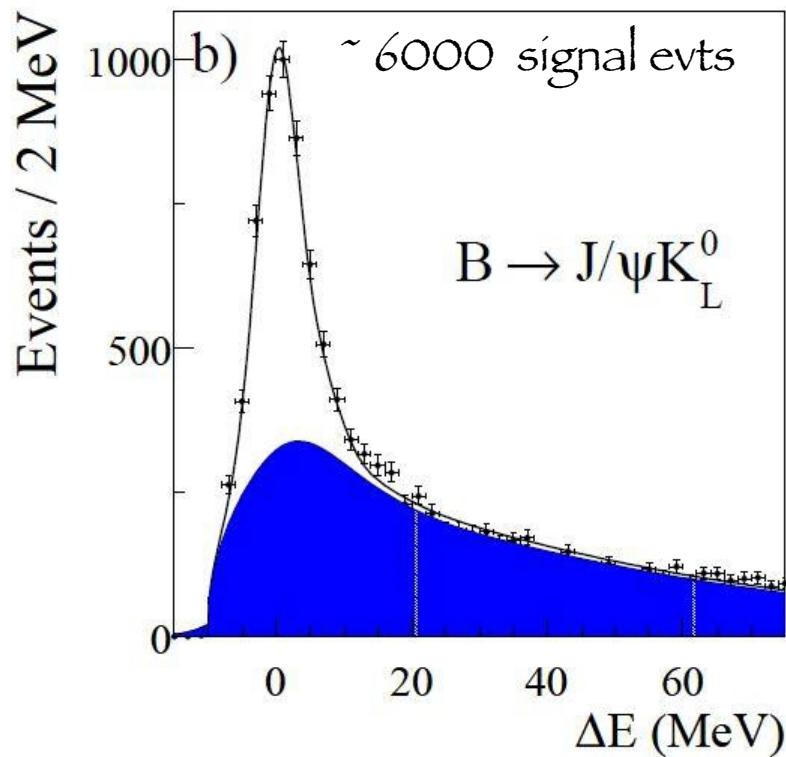
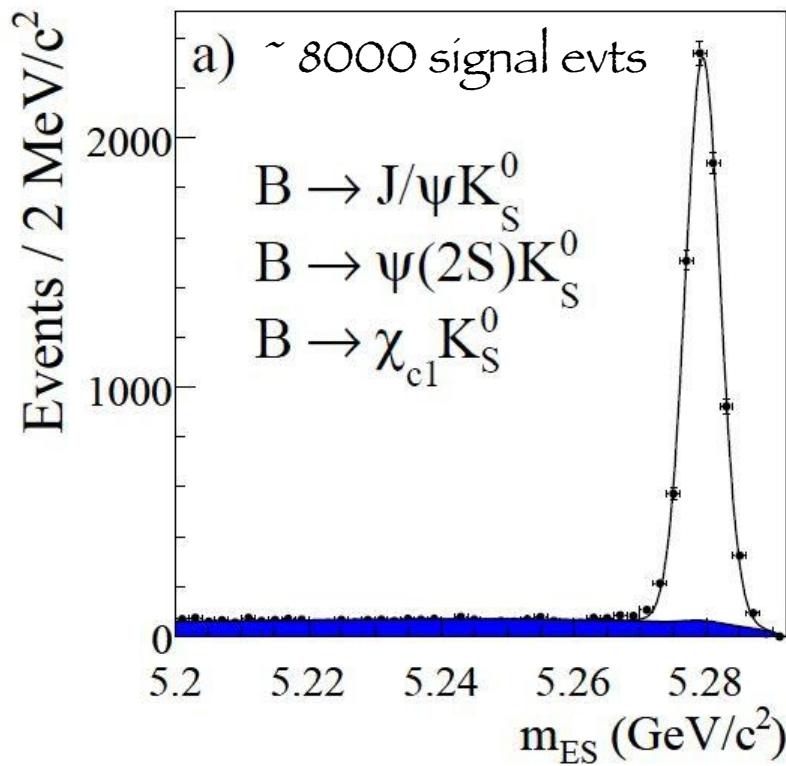


- Need to account for finite $\Delta\tau$ resolution

$$\mathcal{F}_{\alpha,\beta}^{\pm}(\Delta\tau) \propto g_{\alpha,\beta}^{\pm}(\Delta\tau') \times \mathcal{R}(\Delta\tau, \Delta\tau')$$



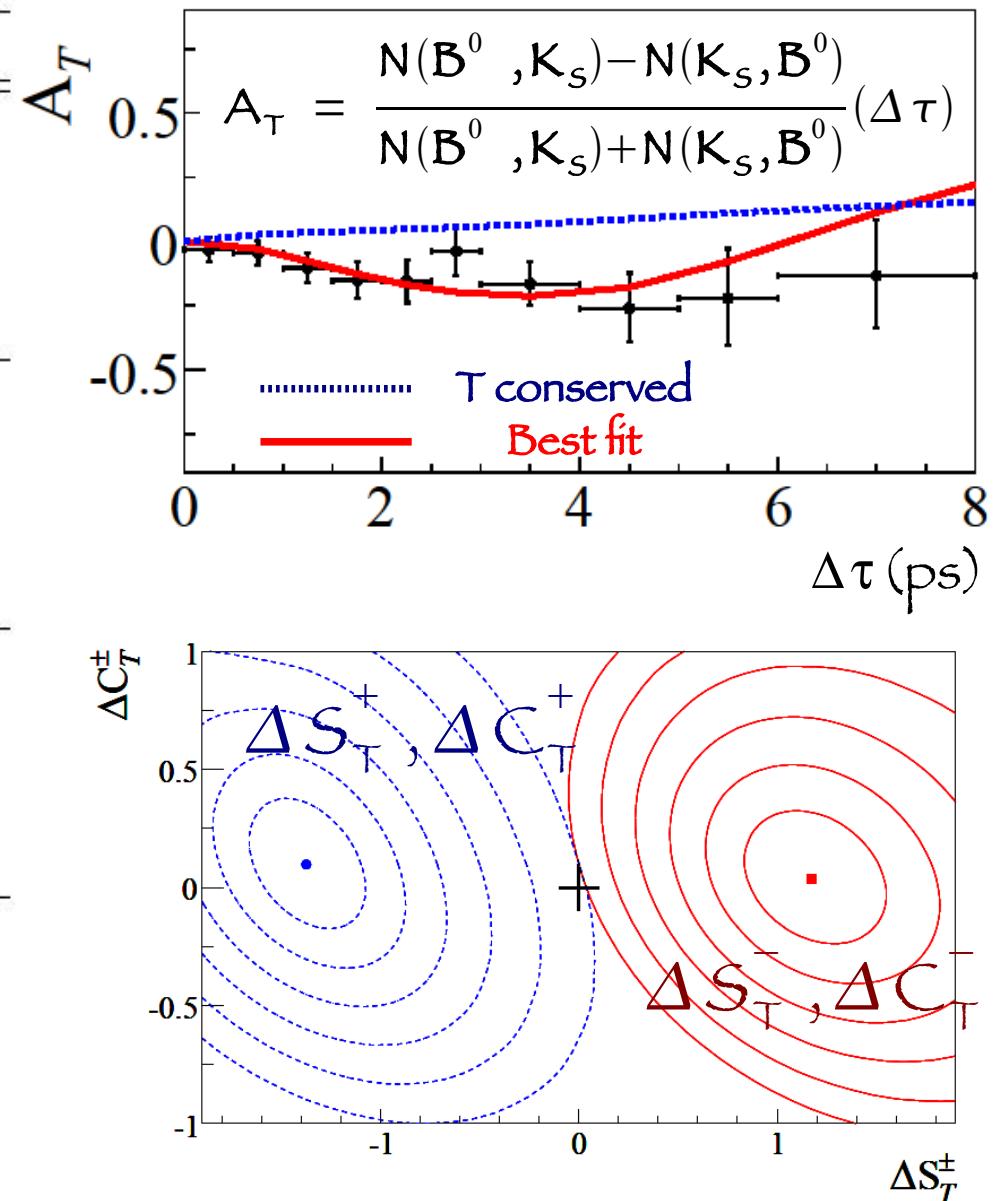
- Need to account for finite $\Delta\tau$ resolution
- Need to account for background (mostly for $J/\psi K_L$)



- Need to account for finite $\Delta\tau$ resolution
- Need to account for background (mostly for $J/\psi K_L$)
- Need to account for dilution from wrong flavor tags
 - Tag-category dependent
 - Use samples of fully reconstructed flavor eigenstates ($D^{(*)}\pi, D^{(*)}K, J/\psi K^{(*)+}$, etc.)

$T\text{-}V$: RESULTS

Parameter	Final result
ΔS_T^+	$-1.37 \pm 0.14 \pm 0.06$
ΔS_T^-	$1.17 \pm 0.18 \pm 0.11$
ΔC_T^+	$0.10 \pm 0.16 \pm 0.08$
ΔC_T^-	$0.04 \pm 0.16 \pm 0.08$
ΔS_{CP}^+	$-1.30 \pm 0.10 \pm 0.07$
ΔS_{CP}^-	$1.33 \pm 0.12 \pm 0.06$
ΔC_{CP}^+	$0.07 \pm 0.09 \pm 0.03$
ΔC_{CP}^-	$0.08 \pm 0.10 \pm 0.04$
ΔS_{CPT}^+	$0.16 \pm 0.20 \pm 0.09$
ΔS_{CPT}^-	$-0.03 \pm 0.13 \pm 0.06$
ΔC_{CPT}^+	$0.15 \pm 0.17 \pm 0.07$
ΔC_{CPT}^-	$0.03 \pm 0.14 \pm 0.08$
$S_{B^0, K_S^0}^+$	$0.545 \pm 0.084 \pm 0.06$
$S_{B^0, K_S^0}^-$	$-0.660 \pm 0.059 \pm 0.04$
$C_{B^0, K_S^0}^+$	$0.011 \pm 0.064 \pm 0.05$
$C_{B^0, K_S^0}^-$	$-0.049 \pm 0.056 \pm 0.03$

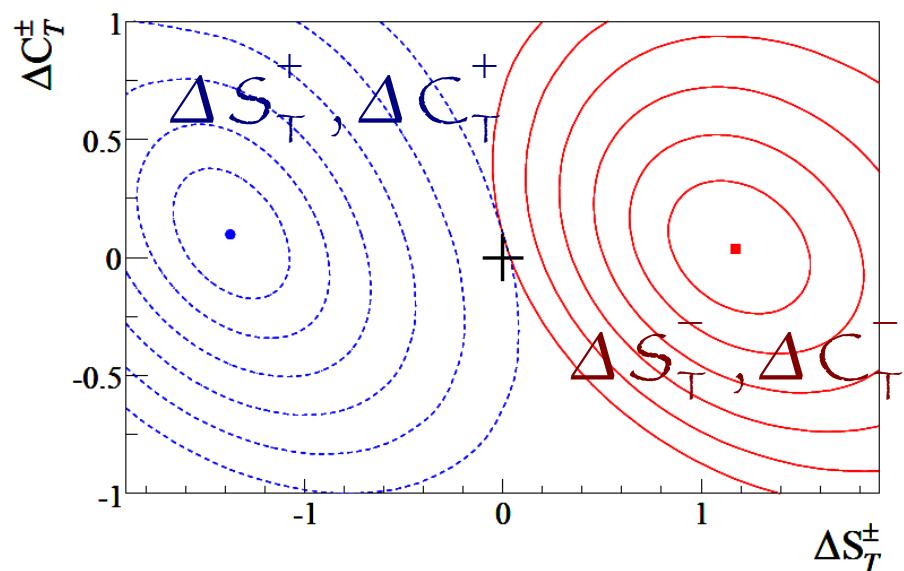
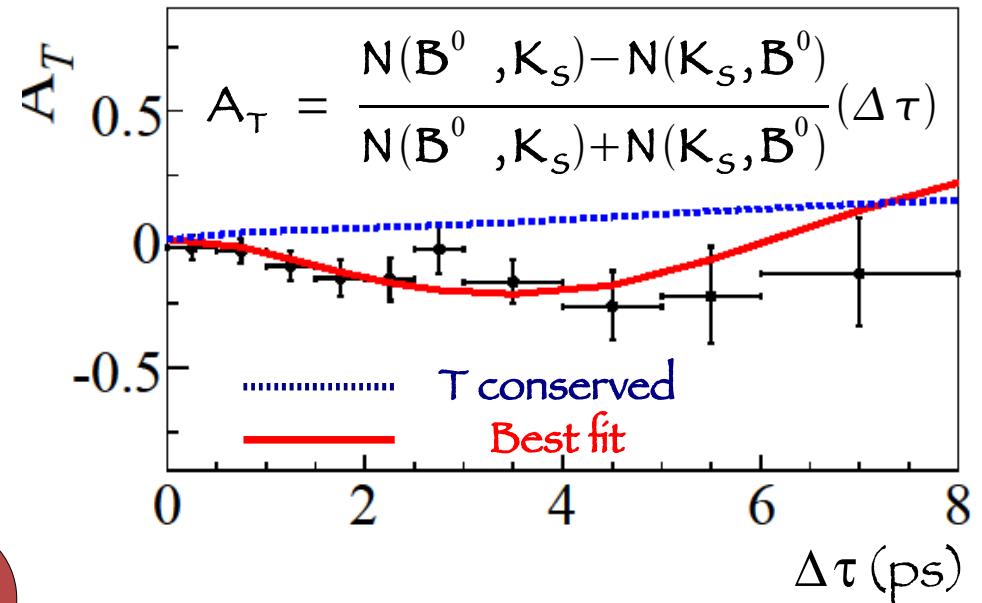


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First unambiguous
observation of
 T -violation in B -Physics
with 14σ significance



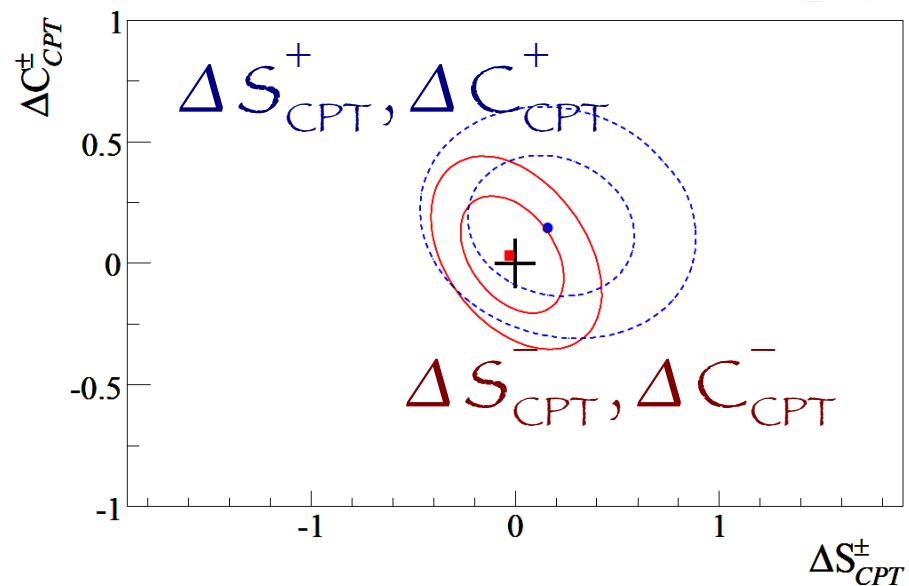
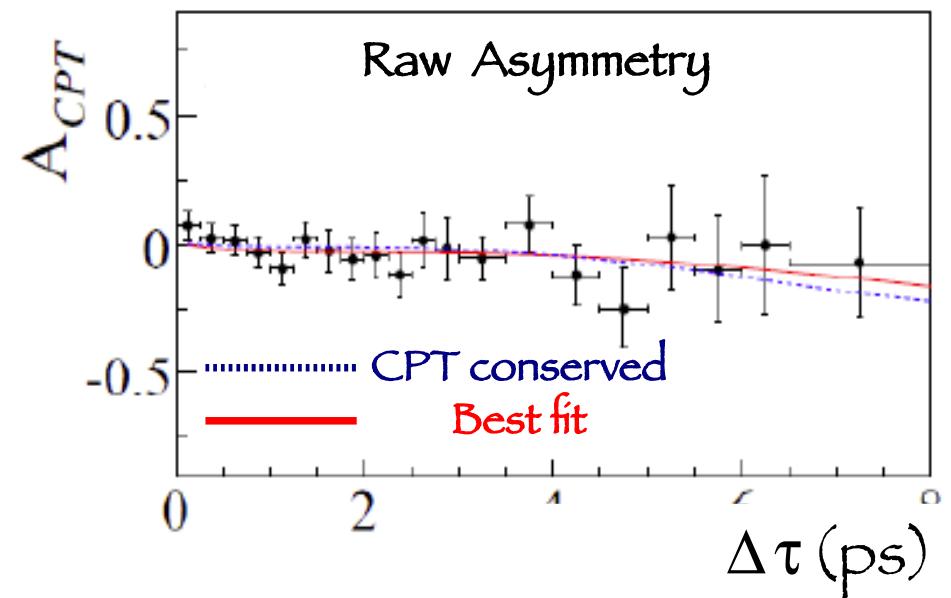
BaBar PRL 109, 211801 (2012)

CPT-V : RESULTS

Parameter	Final result
ΔS_T^+	$-1.37 \pm 0.14 \pm 0.06$
ΔS_T^-	$1.17 \pm 0.18 \pm 0.11$
ΔC_T^+	$0.10 \pm 0.16 \pm 0.08$
ΔC_T^-	$0.04 \pm 0.16 \pm 0.08$
ΔS_{CP}^+	$-1.30 \pm 0.10 \pm 0.07$
ΔS_{CP}^-	$1.33 \pm 0.12 \pm 0.06$
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S_{B^0, K_S}^+	$0.545 \pm 0.084 \pm 0.06$

CPT is Conserved

C_{B^0, K_S}^-	$-0.049 \pm 0.056 \pm 0.03$
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PART II
MIXING – INDUCED CPV

- CPV in mixing if: $\mathcal{P}(\mathcal{B}^0 \rightarrow \overline{\mathcal{B}}^0) \neq \mathcal{P}(\overline{\mathcal{B}}^0 \rightarrow \mathcal{B}^0)$
- CP asymmetry is usually measured through \mathcal{B} semileptonic decays :

$$\mathcal{A}_{\ell\ell} = \frac{N(\mathcal{B}^0 \mathcal{B}^0) - N(\overline{\mathcal{B}}^0 \overline{\mathcal{B}}^0)}{N(\mathcal{B}^0 \mathcal{B}^0) + N(\overline{\mathcal{B}}^0 \overline{\mathcal{B}}^0)} = \frac{N(\ell^+ \ell^+) - N(\ell^- \ell^-)}{N(\ell^+ \ell^+) + N(\ell^- \ell^-)}$$

- Very tiny effects in the SM:

$$\mathcal{A}_{\ell\ell}(\mathcal{B}^0) = (-4.1 \pm 0.6) \cdot 10^{-4}$$

$$\mathcal{A}_{\ell\ell}(\mathcal{B}_s) = (1.9 \pm 0.3) \cdot 10^{-5}$$

(Lenz, Nierste, arXiv:1102.4274 (2011)):

- Positive observation : DISCOVERY OF NEW PHYSICS

- CPV in mixing if: $\mathcal{P}(B^0 \rightarrow \bar{B}^0) \neq \mathcal{P}(\bar{B}^0 \rightarrow B^0)$
- CP asymmetry is usually measured through B semileptonic decays :

$$\mathcal{A}_{ll} = \frac{N(B^0 B^0) - N(\bar{B}^0 \bar{B}^0)}{N(B^0 B^0) + N(\bar{B}^0 \bar{B}^0)} = \frac{N(\ell^+ \ell^+) - N(\ell^- \ell^-)}{N(\ell^+ \ell^+) + N(\ell^- \ell^-)}$$

- A new approach, pionereed by BABAR is here presented:

- “Reco” 1st B : partial reconstruction of $B^0 \rightarrow \ell^+ \nu_\ell D^*$
- “Tag” 2nd B : use charged Kaons

$$\mathcal{A}_{ll} = \frac{N(B^0 B^0) - N(\bar{B}^0 \bar{B}^0)}{N(B^0 B^0) + N(\bar{B}^0 \bar{B}^0)} = \frac{N(\ell^+ K^+) - N(\ell^- K^-)}{N(\ell^+ K^+) + N(\ell^- K^-)}$$

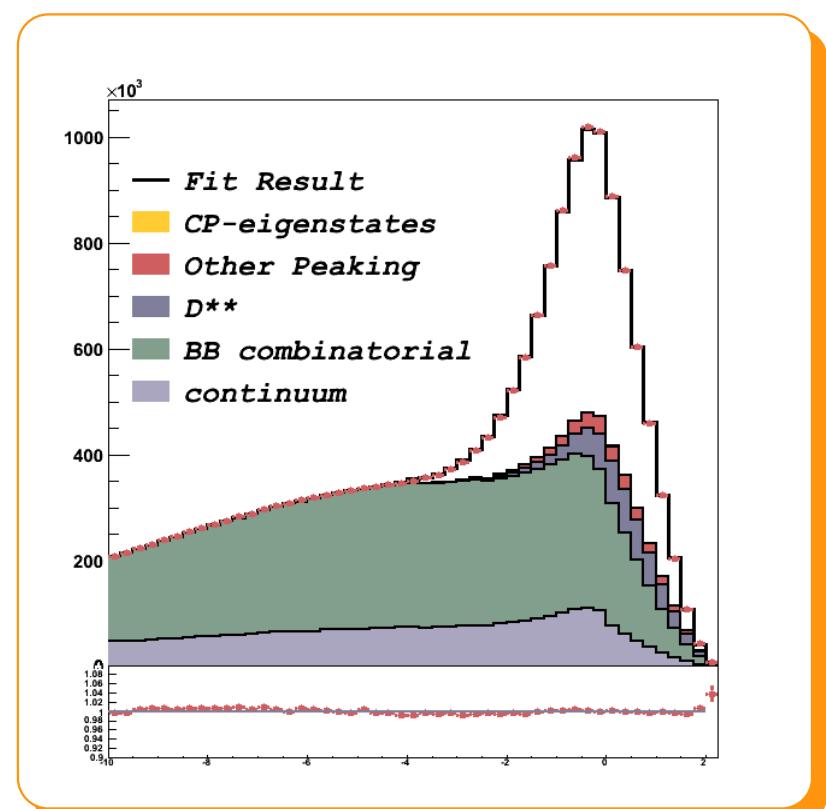
$B \rightarrow D^* \ell \nu$ Partial Reconstruction

- Use only ℓ and low momentum π_s from the decay $D^{*-} \rightarrow \pi_s^- \bar{D}^0$
- Assume B^0 at rest in $Y(4S)$ frame $\vec{P}_B \sim 0$
- Get D^* from π_s : $\vec{P}_{D^*} = \vec{f}(\vec{P}_{\pi_s})$
- Compute missing mass from four momenta difference:

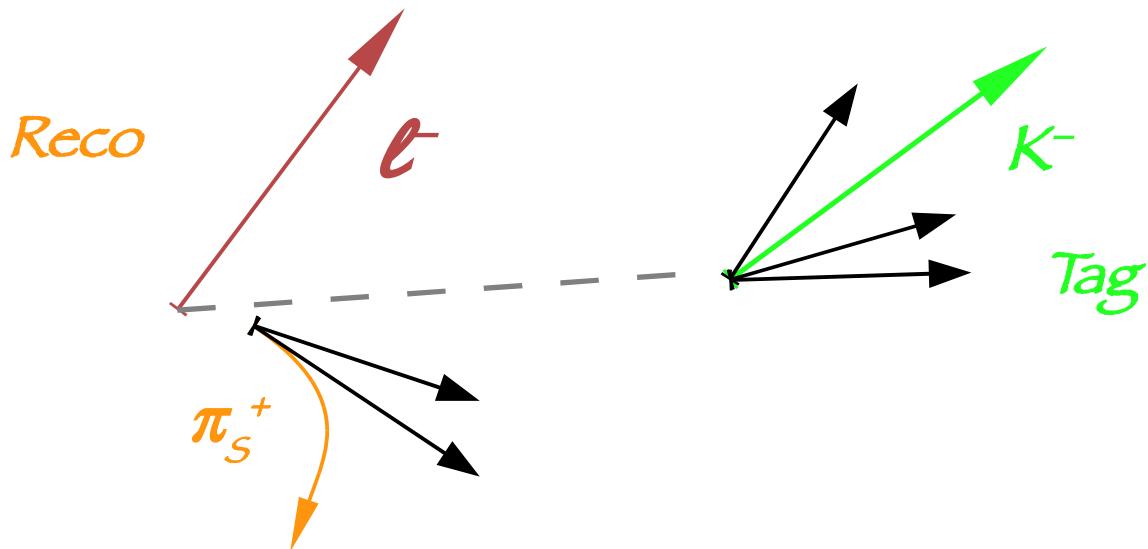
$$M_\nu^2 = (\mathcal{P}_B - \mathcal{P}_{D^*} - \mathcal{P}_\ell)^2$$

- Large event yield

$(5370 \pm 6) \cdot 10^3$ Peaking Events

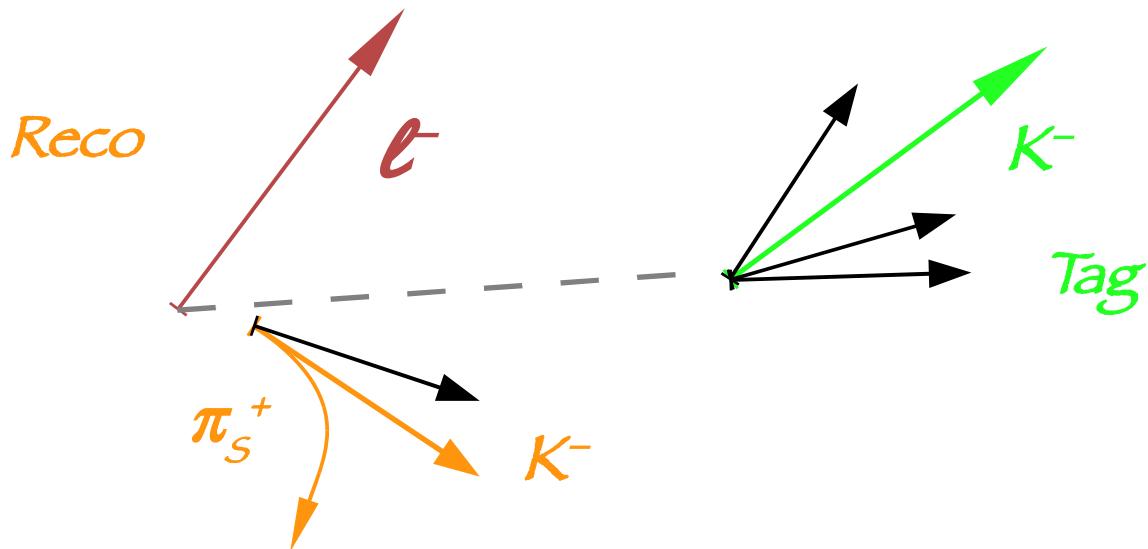


The Kaon Tag



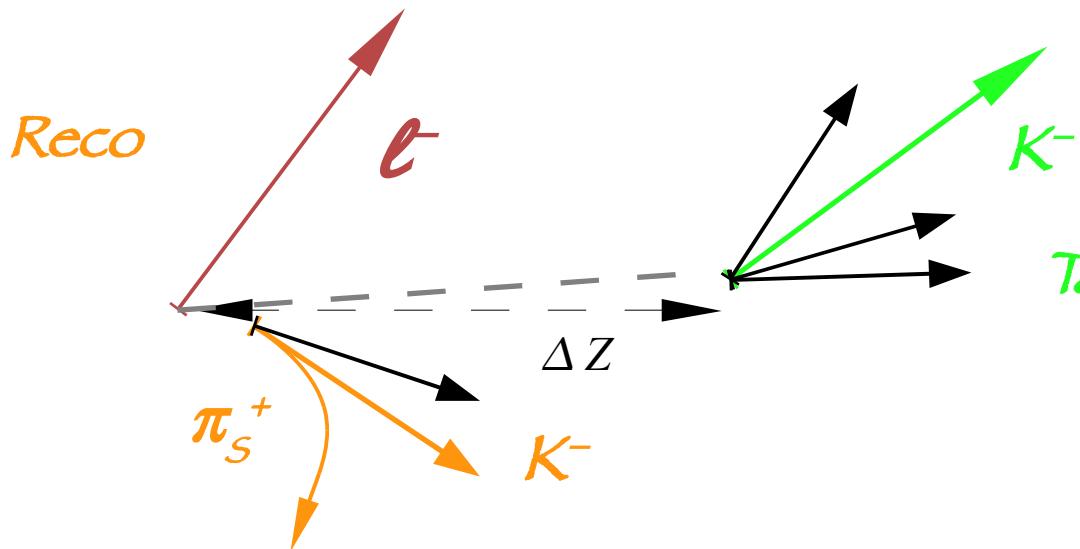
- K identified using dE/dx & Cherenkov with high purity

The Kaon Tag



- ❸ Equal charge Kaons also from the reco side, mimick a mixed event .

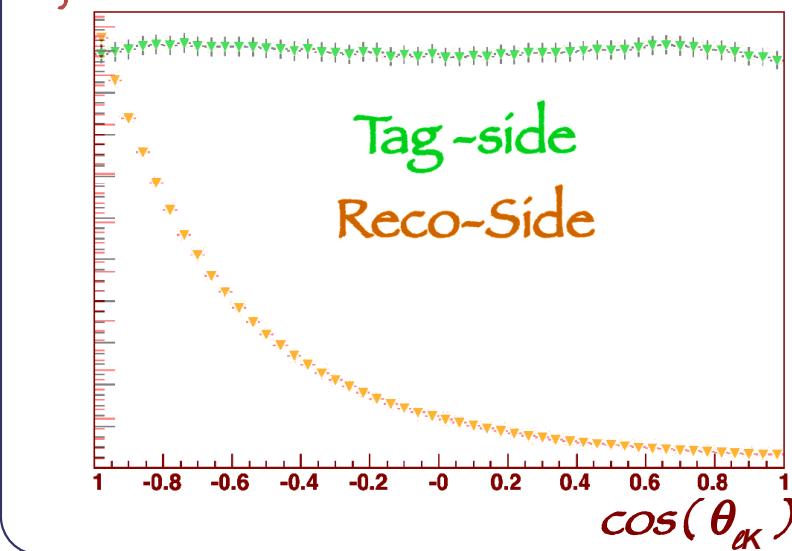
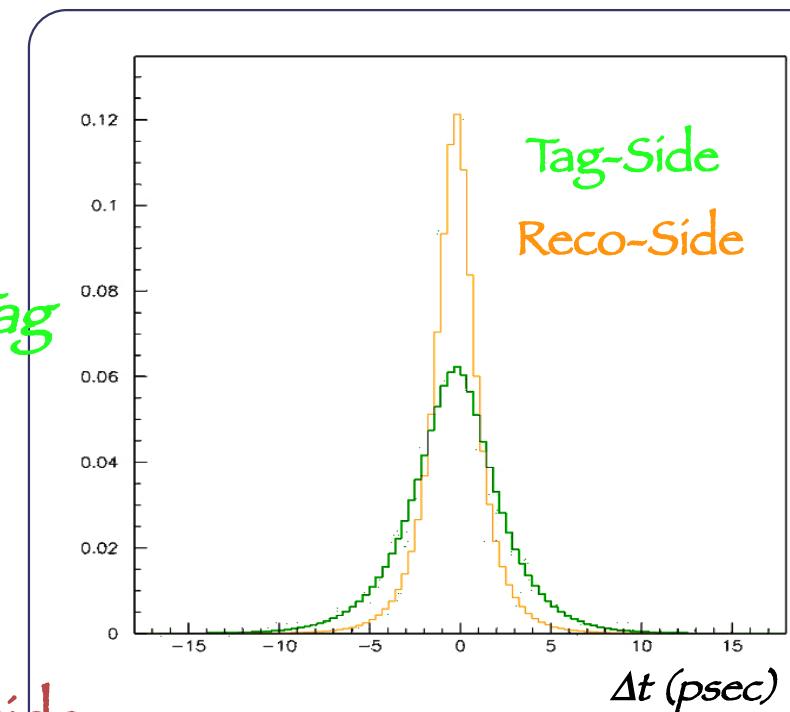
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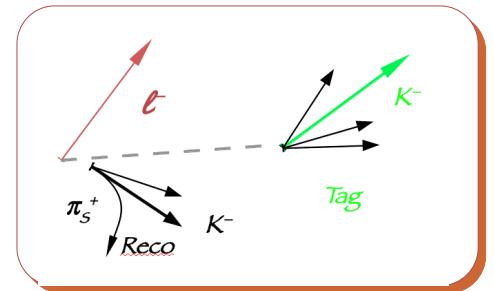
- Separated by:

- $\Delta t \approx (Z_e - Z_K) / (c\beta\gamma)$ (in the Lab)
- $\cos(\theta_{eK})$ (in $Y(4S)$ rest frame)



- Observed asymmetries for mixed reflect RECO-side charge asymmetry, K-id charge asymmetry and Physical asymmetry:

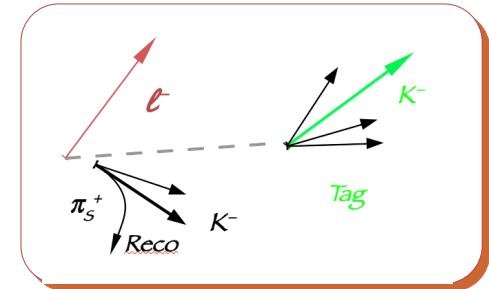
$$\mathcal{A}_{\text{obs},K\text{-Tag}} \simeq \mathcal{A}_{\text{Rec}} + \mathcal{A}_K + \mathcal{A}_{\ell\ell}$$



Asymmetry

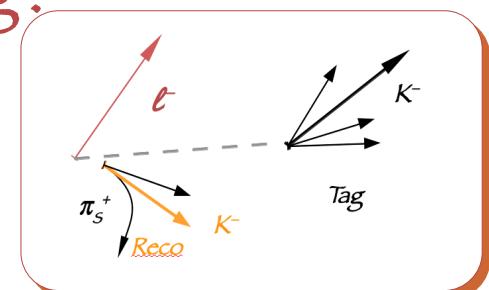
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- Kaons from reco side have tiny contribution from mixing:

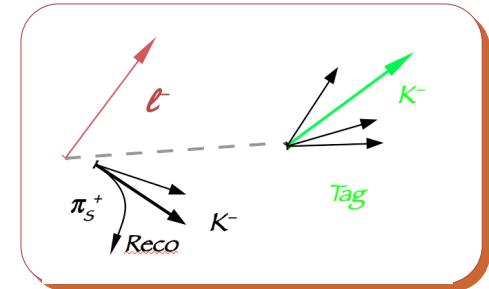
$$\mathcal{A}_{\text{obs}, K\text{-Rec}} \simeq \mathcal{A}_{\text{Rec}} + \mathcal{A}_K + \chi_d \mathcal{A}_{\ell\ell}$$



Asymmetry

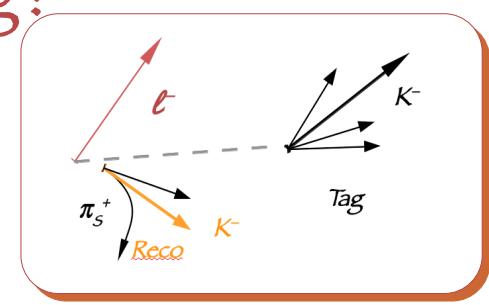
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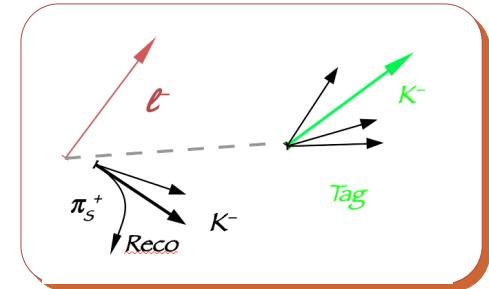
- Measure also single lepton asymmetry (before tagging) :

$$\mathcal{A}_{\text{obs}, \text{Rec}} \simeq \mathcal{A}_{\text{Rec}} + \chi_d \mathcal{A}_{\ell\ell}$$

Asymmetry

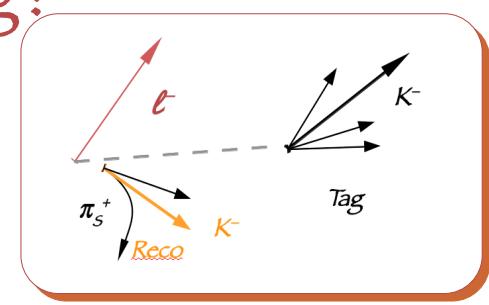
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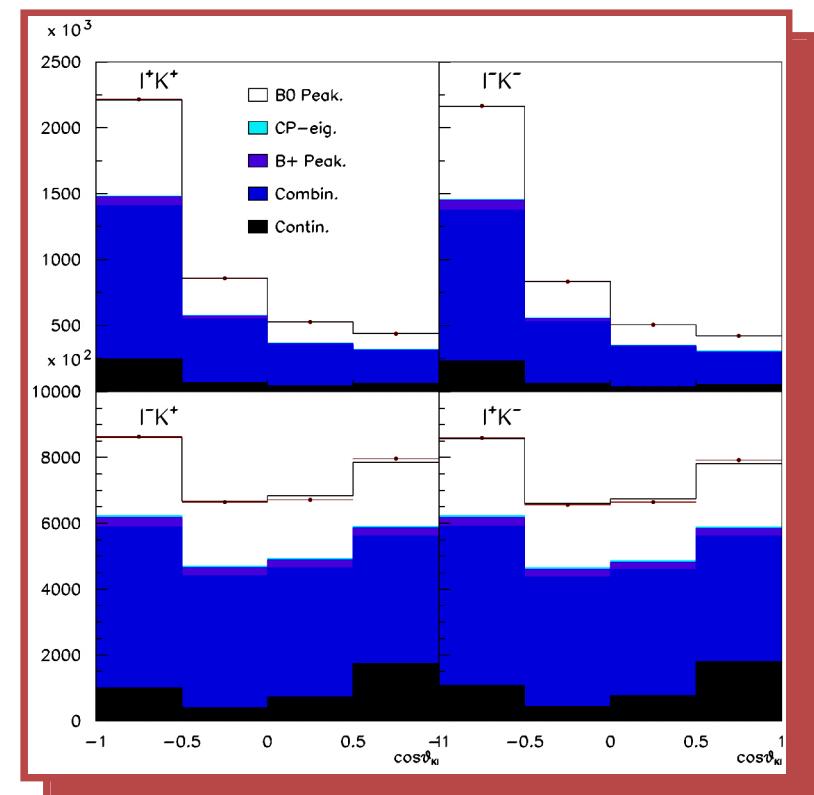
$$\mathcal{A}_{\text{obs},\text{Rec}} \simeq \mathcal{A}_{\text{Rec}} + \chi_d \mathcal{A}_{\ell\ell}$$

- Constrained system:

determine $\mathcal{A}_{\ell\ell}$ and main sources of systematic uncertainty from the data

- 4D binned fit to $(\Delta Z, \cos\theta_{eK}, M_\nu^2, p_K)$ space
- Use also opposite sign ℓ^+K^- / ℓ^-K^+ to improve precision
- More than 100 free parameters:
 - A_{ee} , A_{Rec} , A_K , K-Rec fraction, fraction of wrong tags (charge dependent), fraction of DCSC Kaons, ΔZ resolution parameters, ...

BABAR Preliminary



$\cos\theta_{eK}$

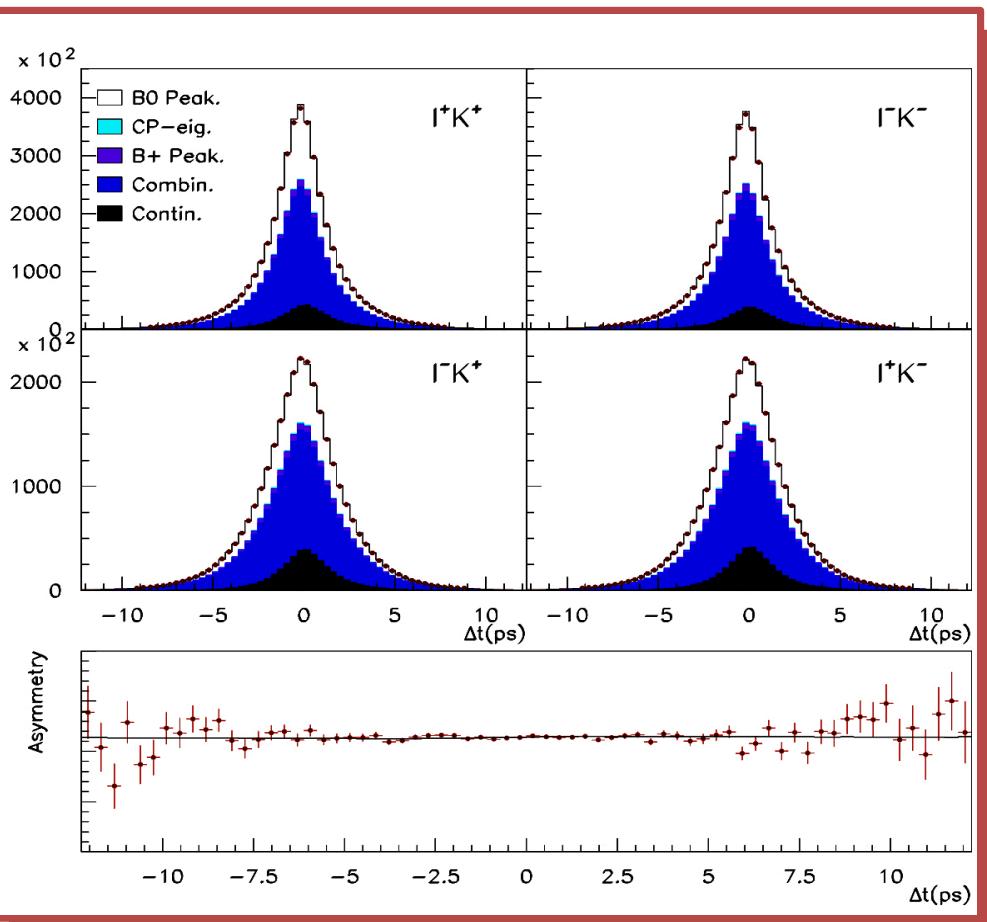
Results

$$\mathcal{A}_{ll} = (0.06 \pm 0.16^{+0.36}_{-0.32})\%$$

No positive observation



BABAR Preliminary



Source	$\Delta q/p $
Peaking Sample Composition	$+1.17 \times 10^{-3}$
Combinatorial Sample Composition	-1.50×10^{-3}
ΔT Resolution Model	$\pm 0.39 \times 10^{-3}$
Dtag fraction	$+0.60 \times 10^{-3}$
Dtag ΔT distribution	$\pm 0.11 \times 10^{-3}$
Fit Bias	$+0.65 \times 10^{-3}$
CP-eigenstate description	$+0.46 \times 10^{-3}$
Physical Parameters	-0.58×10^{-3}
Total	$+0.28 \times 10^{-3}$

$\frac{1}{2}\sigma(\mathcal{A}_{ll})$	$\Delta q/p $
$+0.28 \times 10^{-3}$	$+1.61 \times 10^{-3}$

Results

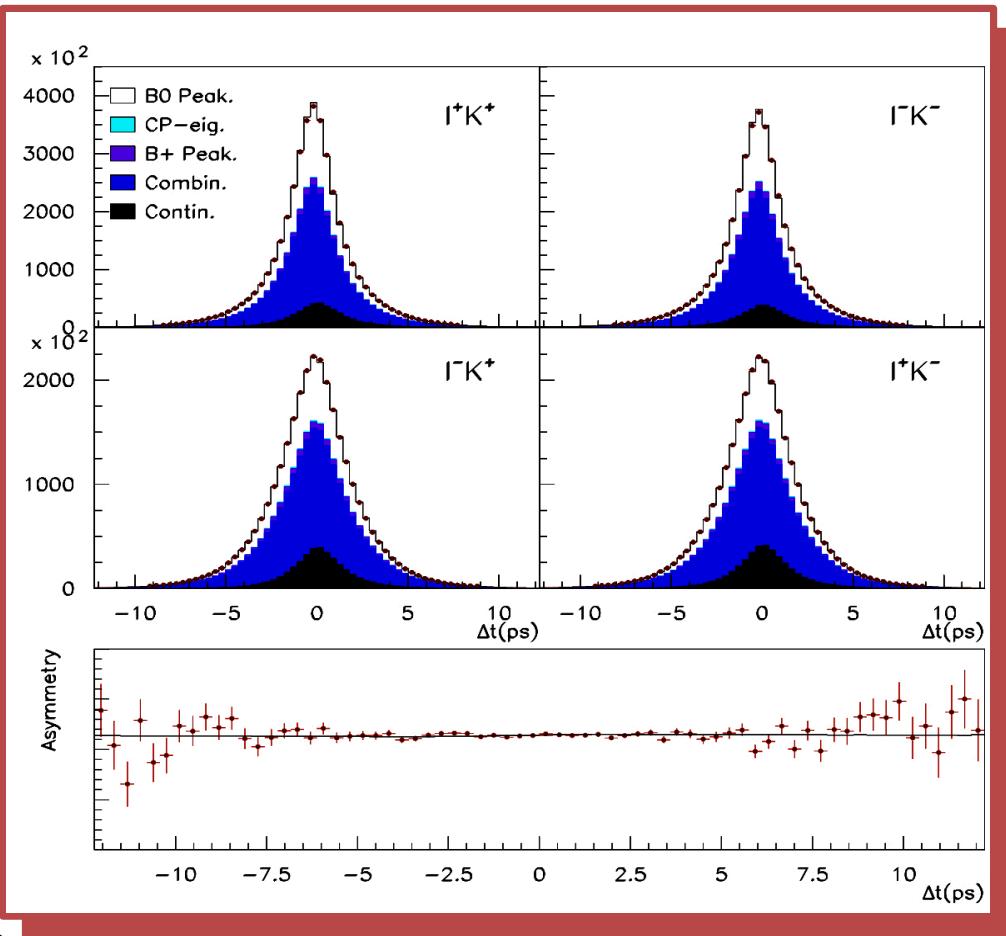
BABAR Preliminary

$$\mathcal{A}_{ll} = (0.06 \pm 0.16^{+0.36}_{-0.32})\%$$

- More precise than previous B-Factories average:



$$\mathcal{A}_{ll} = (-0.05 \pm 0.56)\%$$



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Peaking Sample Composition	$+1.17 \times 10^{-3}$
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CP-eigenstate description	$+0.46 \times 10^{-3}$
Physical Parameters	-0.58×10^{-3}
Total	$+0.28 \times 10^{-3}$
	$+1.61 \times 10^{-3}$
	-1.78×10^{-3}

$$\frac{1}{2}\sigma(\mathcal{A}_{ll})$$

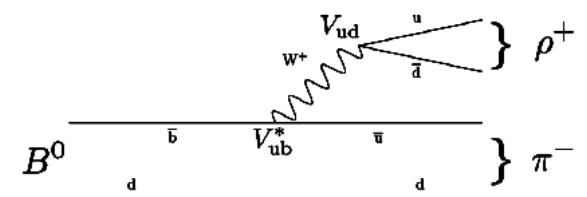
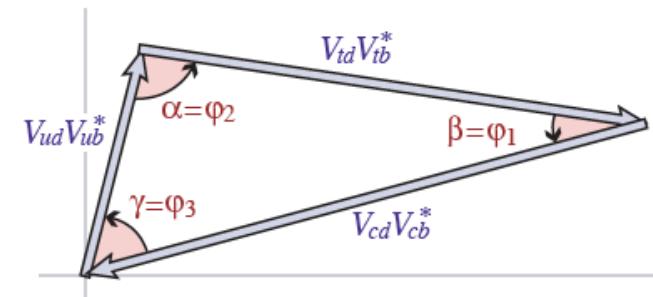
PART III

Measurement of α from $B \rightarrow \pi^+ \pi^- \pi^0$

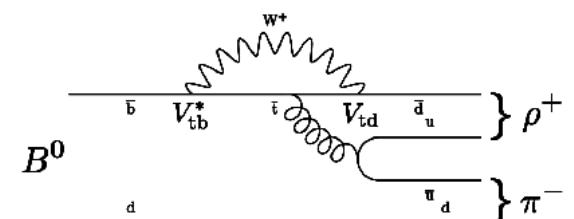
Measurement of α

- Interference between mixing and decay would allow to compute $\sin 2\alpha$ a-la $\sin 2\beta$
- Tree & penguin diagram have comparable size. Their interference:
 - introduces a strong phase difficult to compute
 - may induce a sizable amount of direct CP violation
- Time dependent tagged analysis across the $\rho\pi$ Dalitz plot permits – in principle – an unambiguous measurement of α

Snyder- Quinn Phys.Rev. D 48,2139 (1993)



Tree Diagram



Penguin Diagram

BABAR has recently updated its 2007 measurement:

- to the full dataset (431 fb^{-1} , + 25%)
- improved tracking + PID
- re-optimized selection requirements
- performed a robustness study to assess the reliability with which the true value of α can be extracted

Time-Dependent PDF

Direct CPV

$$|\mathcal{A}_{3\pi}^{\pm}(\Delta t)|^2 = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \left[|\mathcal{A}_{3\pi}|^2 + |\overline{\mathcal{A}}_{3\pi}|^2 \mp \left(|\mathcal{A}_{3\pi}|^2 - |\overline{\mathcal{A}}_{3\pi}|^2 \right) \cos(\Delta m_d \Delta t) \pm \right. \\ \left. 2\text{Im} \left[\frac{q}{p} \overline{\mathcal{A}}_{3\pi} \mathcal{A}_{3\pi}^* \right] \sin(\Delta m_d \Delta t) \right]$$

$\sin(2\alpha_{\text{eff}})$

$$\begin{aligned} \mathcal{A}_{3\pi} &= f_+ A^+ + f_- A^- + f_0 A^0 \quad \text{for} \quad B^0 \rightarrow \pi^+ \pi^- \pi^0 \\ \overline{\mathcal{A}}_{3\pi} &= f_+ \overline{A}^+ + f_- \overline{A}^- + f_0 \overline{A}^0 \quad \text{for} \quad \overline{B}^0 \rightarrow \pi^+ \pi^- \pi^0 \end{aligned}$$

$$\rho^+ \quad \rho^- \quad \rho^0$$

$$f_\kappa(m, \theta_\kappa) \propto F_{\rho(770)}(m, \theta_\kappa) + a_{\rho'} e^{i\phi_{\rho'}} F_{\rho(1450)}(m, \theta_\kappa)$$

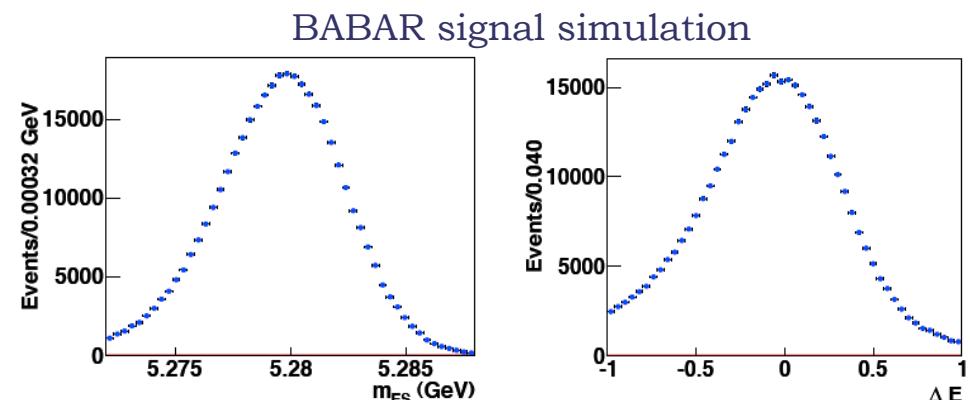
$\rho(1700)$ is neglected

Event Selection

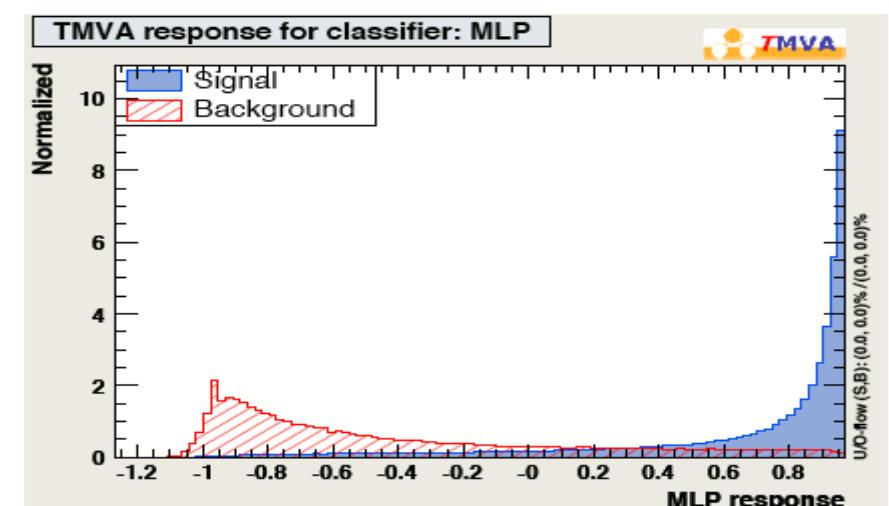
- Usual tags from $B(\pi\pi\pi)$ invariant mass and energy

$$m_{ES} = \sqrt{\left(\frac{\sqrt{s}}{2}\right)^2 - (p_B^*)^2}$$

$$\Delta E = E_B^* - \frac{1}{2}\sqrt{s}$$



- NN to reject jet-like ($udsc$) continuum background
- Still large amount of residual background
- Fit (see below) estimates :



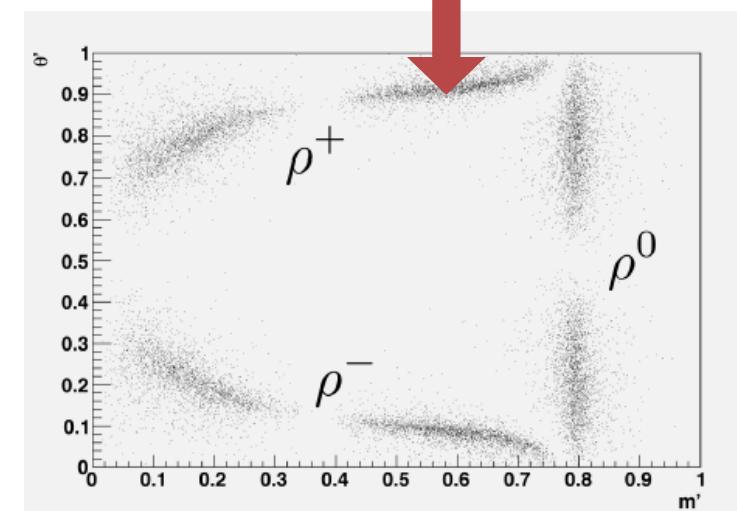
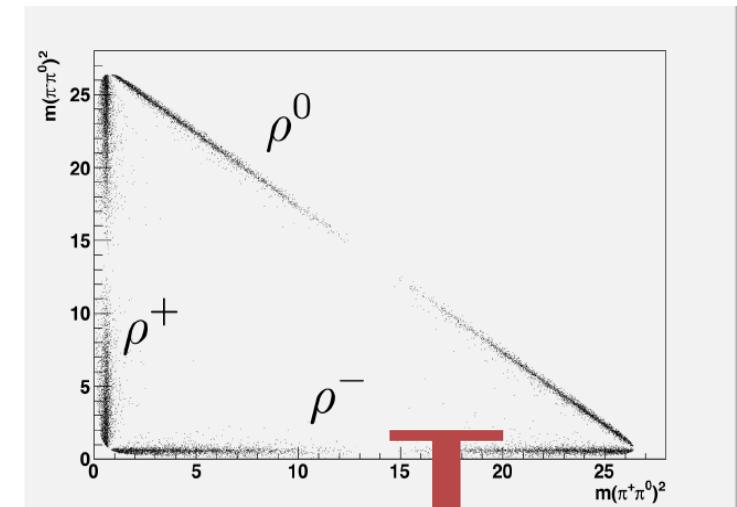
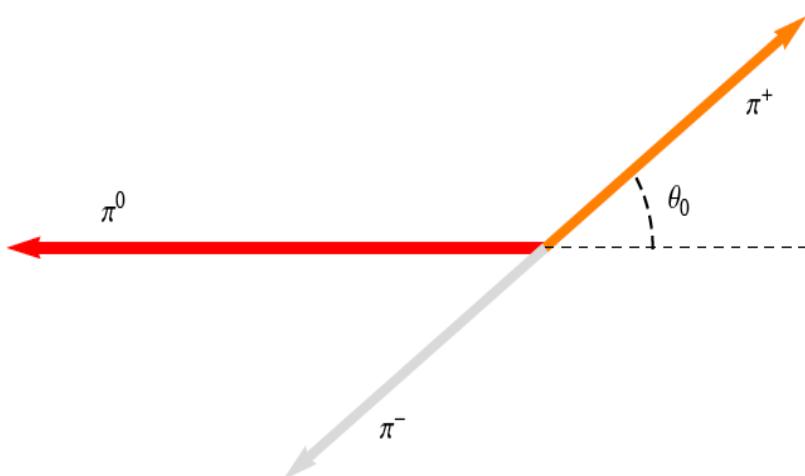
2900 ± 100 signal events
 46700 ± 200 continuum background events

- Dalitz variables mapped to a square domain :

$\pi^+\pi^-$ invariant mass

$$m' \equiv \frac{1}{\pi} \arccos \left(2 \frac{m_0 - m_0^{\min}}{m_0^{\max} - m_0^{\min}} - 1 \right)$$

$$\theta' \equiv \frac{1}{\pi} \theta_0 \quad \text{helicity angle}$$



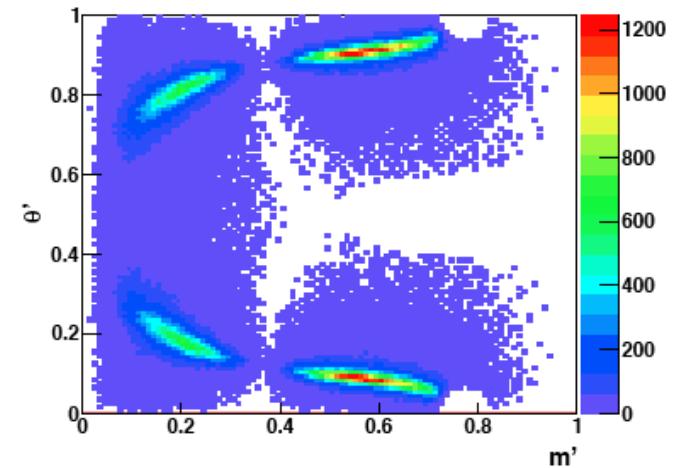
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$\theta' \equiv \frac{1}{\pi} \theta_0$ helicity angle

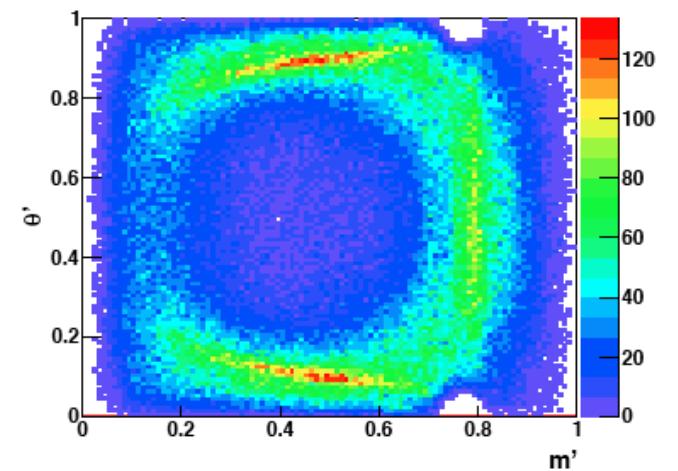
Correctly Reconstructed Signal MC



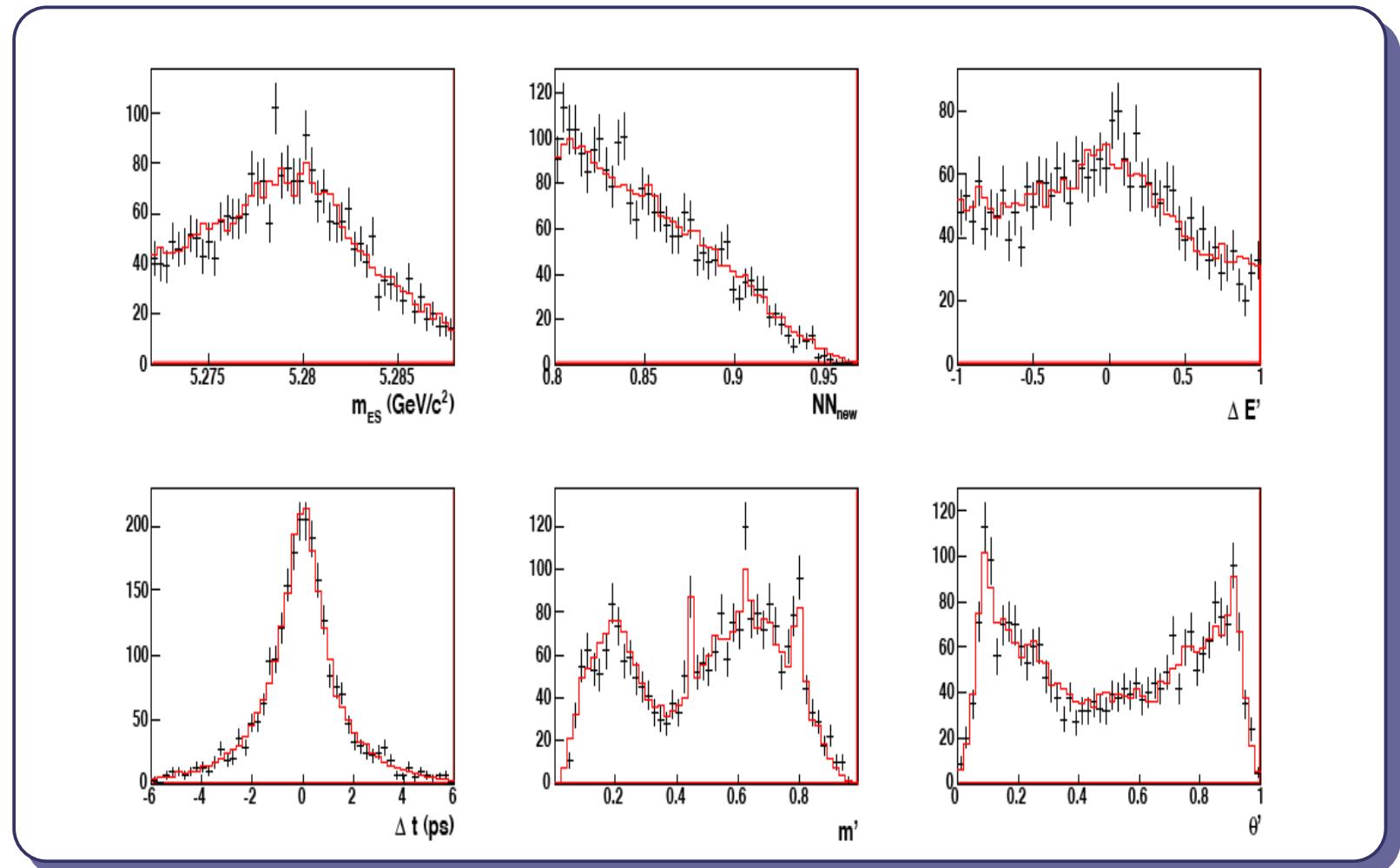
- Data model:

- Signal, BB background (MC)
- Continuum (sidebands, data collected below Y(4S) threshold)

MES Sideband Data



- 6-D fit ($m_{ES}, \Delta E, NN, \Delta t, m', \theta'$) performed in the U,I formalism (26 param.) and then mapped into the physical quantities .
- Good overall agreement:

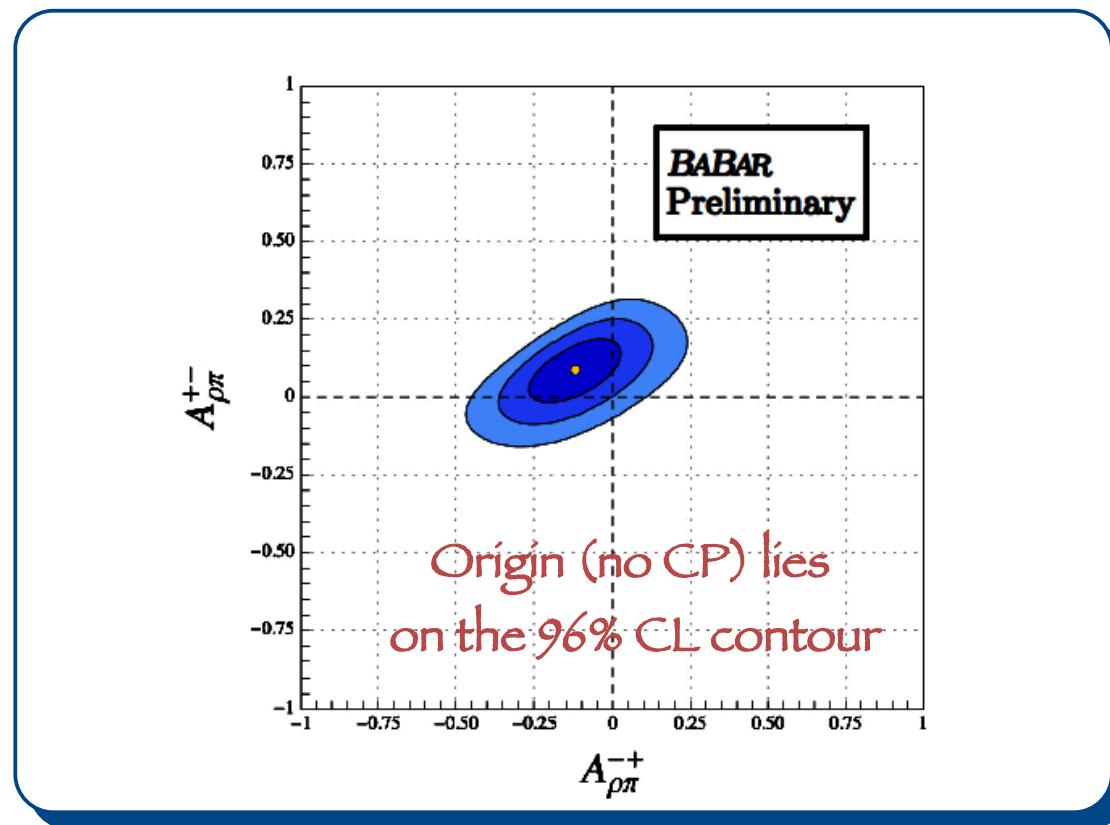


Results (1) : direct CP

- Observe direct CP violation from the asymmetries:

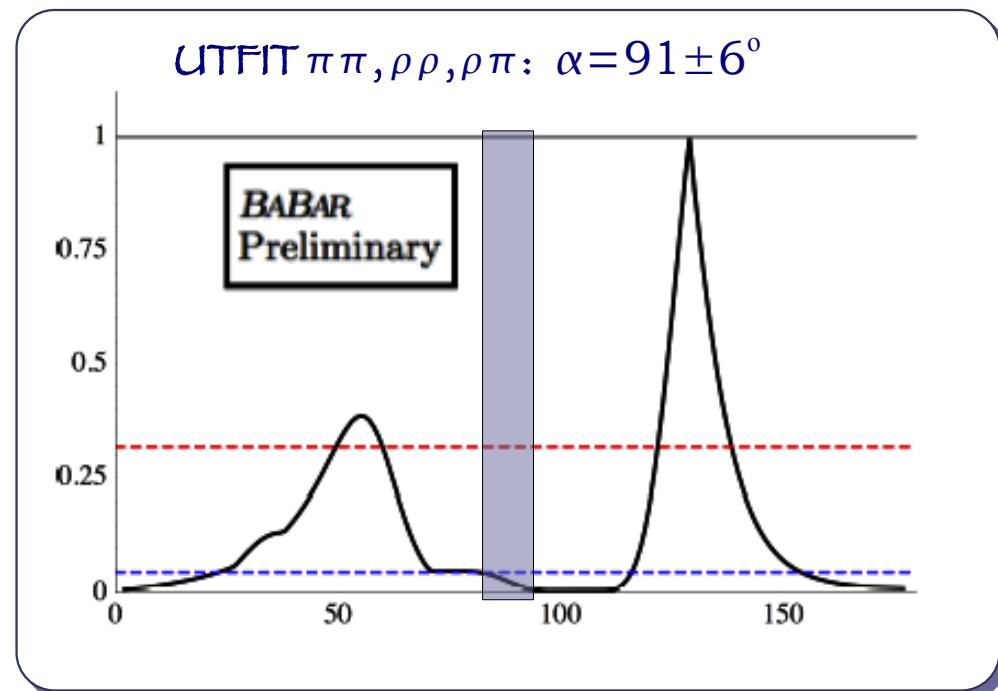
$$\mathcal{A}_{\rho\pi}^{+-} \equiv \frac{\Gamma(\overline{B}^0 \rightarrow \rho^- \pi^+) - \Gamma(B^0 \rightarrow \rho^+ \pi^-)}{\Gamma(\overline{B}^0 \rightarrow \rho^- \pi^+) + \Gamma(B^0 \rightarrow \rho^+ \pi^-)} = 0.09_{-0.06}^{+0.05} \pm 0.04$$

$$\mathcal{A}_{\rho\pi}^{-+} \equiv \frac{\Gamma(\overline{B}^0 \rightarrow \rho^+ \pi^-) - \Gamma(B^0 \rightarrow \rho^- \pi^+)}{\Gamma(\overline{B}^0 \rightarrow \rho^+ \pi^-) + \Gamma(B^0 \rightarrow \rho^- \pi^+)} = -0.12 \pm 0.08_{-0.05}^{+0.04}$$



Results (2) : α

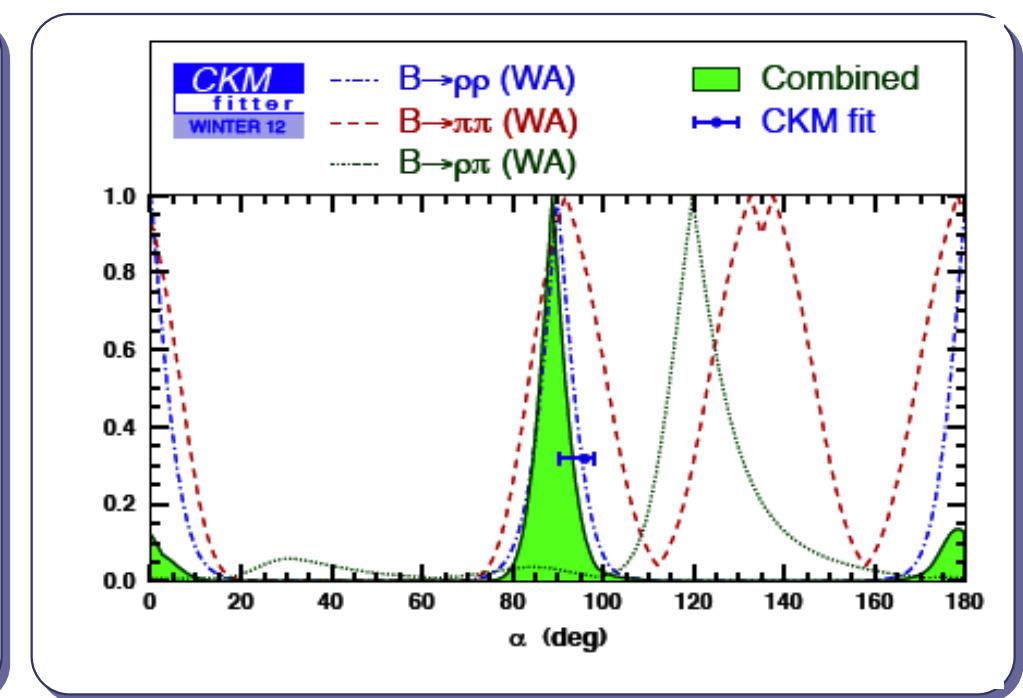
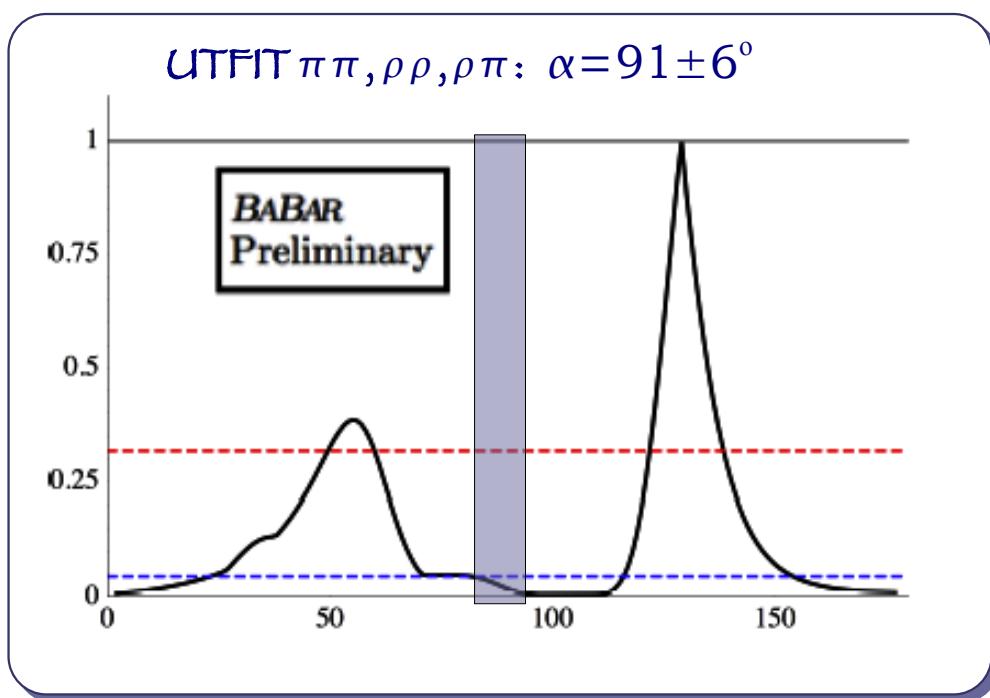
- parameter scan to get $\Delta\chi^2$ profile and 1-CL plot



- result disagree with World Average ($B \rightarrow \pi\pi$, $B \rightarrow \rho\rho$)

Results (2) : α

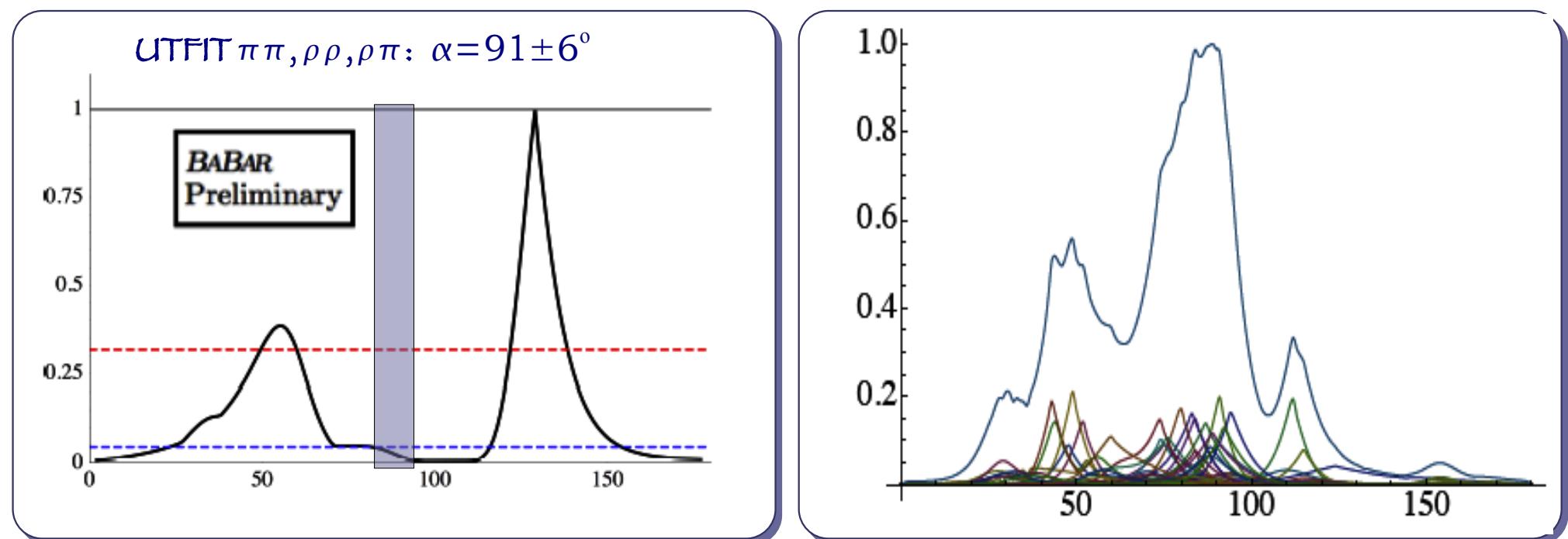
- parameter scan to get $\Delta\chi^2$ profile and 1-CL plot



- result disagree with WA ($B \rightarrow \pi\pi$, $B \rightarrow pp$)
- confirms bias observed in previous analysis by BABAR & Belle

Results (2) : α

- parameter scan to get $\Delta\chi^2$ profile and 1-CL plot



- result disagree with WA ($B \rightarrow \pi\pi$, $B \rightarrow \rho\rho$)
- confirms bias observed in previous analysis by $BABAR$ & $Belle$
- toy MC : due to small S/N, secondary minima are often favored

Conclusions

Four years after end running, BABAR has still glamour results on CP/T-Violation:

- First uncontroversial evidence of T-Violation in the B -meson system
- Most precise measurement of mixing-induced CP-Violation
- Direct CP-Violation on $B \rightarrow p\pi$ assessed at 96% CL

<http://www.economist.com/node/21561111>





Backup

$$f_{Q\text{tag}}^{\rho^\pm \pi^\mp}(\Delta t) = (1 \pm \mathcal{A}_{\rho\pi}) \frac{e^{-|\Delta t|/\tau}}{4\tau} \\ \times [1 + Q_{\text{tag}}(\mathcal{S} \pm \Delta\mathcal{S}) \sin(\Delta m_d \Delta t) \\ - Q_{\text{tag}}(\mathcal{C} \pm \Delta\mathcal{C}) \cos(\Delta m_d \Delta t)] .$$

$$\begin{aligned}\mathcal{C} &= (\mathcal{C}^+ + \mathcal{C}^-)/2, \\ \Delta\mathcal{C} &= (\mathcal{C}^+ - \mathcal{C}^-)/2, \\ \mathcal{S} &= (\mathcal{S}^+ + \mathcal{S}^-)/2, \\ \Delta\mathcal{S} &= (\mathcal{S}^+ - \mathcal{S}^-)/2.\end{aligned}$$

Param	Value	σ_{stat}	σ_{syst}
$\mathcal{A}_{\rho\pi}$	-0.100	0.029	0.021
\mathcal{C}	0.016	0.059	0.036
$\Delta\mathcal{C}$	0.234	0.061	0.048
\mathcal{S}	0.053	0.081	0.034
$\Delta\mathcal{S}$	0.054	0.082	0.039
\mathcal{C}_{00}	0.19	0.23	0.15
\mathcal{S}_{00}	-0.37	0.34	0.20
f_{00}	0.092	0.011	0.008

- Information about the unitarity triangle angle α is extracted in a likelihood scan based on our final U/I fit results and full stat+syst covariance matrix
- Perform a χ^2 minimization at each value of α from $(0 - 180)$ degrees using

$$\chi_{\alpha \text{ scan}}^2 = [V^{\text{data}} - V^{\text{scan}}]^T (C^{\text{data}})^{-1} [V^{\text{data}} - V^{\text{scan}}]$$

- The variables that float in these fits are actually the tree and penguin amplitudes which are related to the ρ amplitudes by:

$$\begin{aligned} A^+ &= T^+ e^{-i\alpha} + P^+ \\ A^- &= T^- e^{-i\alpha} + P^- \\ A^0 &= T^0 e^{-i\alpha} + P^0 \\ \bar{A}^+ &= T^- e^{+i\alpha} + P^- \\ \bar{A}^- &= T^+ e^{+i\alpha} + P^+ \\ \bar{A}^0 &= T^0 e^{+i\alpha} + P^0 \end{aligned}$$

CLEAR observes $K_0 \leftrightarrow \bar{K}_0$ asymmetry

PLB444 43,1998

$$A_K = (6.6 \pm 1.6) \cdot 10^{-3}$$

- Time-integrated asymmetry
- requires $\sim \Delta \Gamma(K) \neq 0$
- Not unambiguous interpretation as T-violation (could also be mixing-induced CPV):

Wolfenstein [PRL83,911,(1999); Int.Journ.Mod.Phys.E8,501,(1999)]

Gerber, and references therein, Eur. Phys. Jour. C 35, 195 (2004)

$T\text{-}V$ in the PDG

e electric dipole moment	$< 10.5 \times 10^{-28}$ ecm, CL = 90%
μ electric dipole moment	$(-0.1 \pm 0.9) \times 10^{-19}$ ecm
μ decay parameters	
transverse e^+ polarization normal to plane of μ	$(-2 \pm 8) \times 10^{-3}$
spin, e^\pm momentum	
α'/A	$(-10 \pm 20) \times 10^{-3}$
β'/A	$(2 \pm 7) \times 10^{-3}$
$\text{Re}(d_T = \tau$ electric dipole moment)	-0.220 to 0.45×10^{-16} ecm, CL = 95%
P_T in $K^+ \rightarrow \pi^0 \mu^+ \nu_\mu$	$(-1.7 \pm 2.5) \times 10^{-3}$
P_T in $K^+ \rightarrow \mu^+ \nu_\mu \gamma$	$(-0.6 \pm 1.9) \times 10^{-2}$
$\text{Im}(\xi)$ in $K^+ \rightarrow \pi^0 \mu^+ \nu_\mu$ decay (from transverse μ pol.)	-0.006 ± 0.008
asymmetry A_T in K^0 - \bar{K}^0 mixing	$(6.6 \pm 1.6) \times 10^{-3}$
$\text{Im}(\xi)$ in $K_{\mu 3}^0$ decay (from transverse μ pol.)	-0.007 ± 0.026
$A_T(D^\pm \rightarrow K_S^0 K^\pm \pi^+ \pi^-)$	[b] $(-12 \pm 11) \times 10^{-3}$
$A_T(D^0 \rightarrow K^+ K^- \pi^+ \pi^-)$	[b] $(1 \pm 7) \times 10^{-3}$
$A_T(D_s^\pm \rightarrow K_S^0 K^\pm \pi^+ \pi^-)$	[b] $(-14 \pm 8) \times 10^{-3}$
p electric dipole moment	$< 0.54 \times 10^{-23}$ ecm
n electric dipole moment	$< 0.29 \times 10^{-25}$ ecm, CL = 90%
$n \rightarrow p e^- \bar{\nu}_e$ decay parameters	
ϕ_{AV} , phase of g_A relative to g_V	[c] $(180.018 \pm 0.026)^\circ$
triple correlation coefficient D	[d] $(-1.2 \pm 2.0) \times 10^{-4}$
triple correlation coefficient R	[d] 0.008 ± 0.016
Λ electric dipole moment	$< 1.5 \times 10^{-16}$ ecm, CL = 95%
triple correlation coefficient D for $\Sigma^- \rightarrow n e^- \bar{\nu}_e$	0.11 \pm 0.10

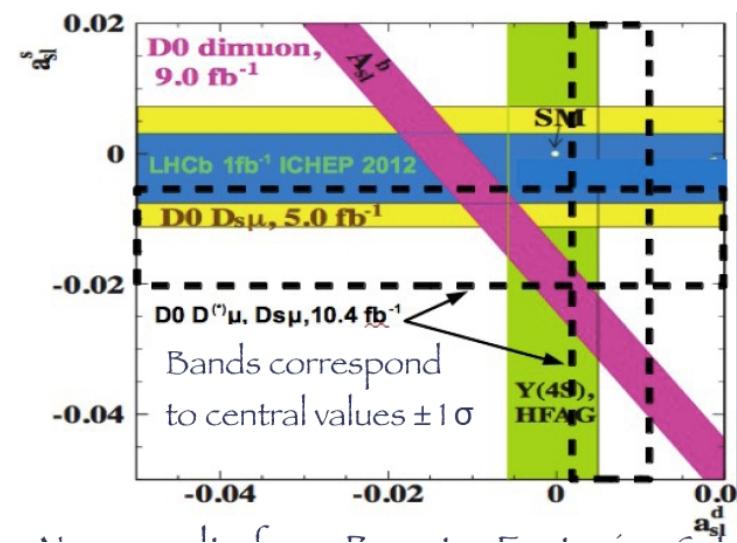
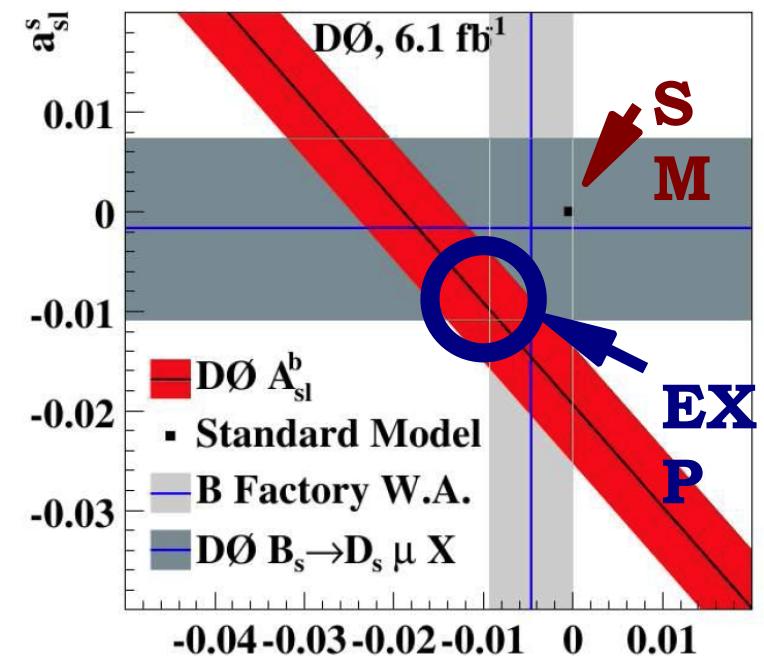
CLEAR: PLB 444, 43 (1998)
 Compares $K^0 \rightarrow \bar{K}^0$ with $\bar{K}^0 \rightarrow K^0$
 Mixing rate.

- Related by T and CP.
- Not time-dependent.
- Various criticisms.

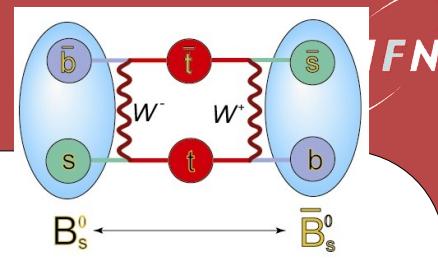
BABAR:
 PRD(RC)81, 111103 (2010)
 PRD(RC) 84, 031103 (2011)
 Triple products

Dilepton Asymmetry @ colliders

- DO claims large unexpected asymmetry in equal charge dilepton B decays at ICHEP 2010
- Lifetime analysis : effect connected to B_s mixing
- DO and LHCb then measure asymmetry in the rates of $B_s \rightarrow D^{(*)}_s \mu \nu$ decays
- These measurements are consistent both with the SM and with DO dilepton results



B^0 Mixing parameters



- Two-levels system evolution:

$$i \frac{d}{dt} \left(\frac{B_q}{\bar{B}_q} \right) = \left[\begin{pmatrix} M_{11}^q & M_{21}^{q*} \\ M_{21}^q & M_{11}^q \end{pmatrix} - \frac{i}{2} \begin{pmatrix} \Gamma_{11}^q & \Gamma_{21}^{q*} \\ \Gamma_{21}^q & \Gamma_{11}^q \end{pmatrix} \right] \left(\frac{B_q}{\bar{B}_q} \right)$$

- Mass eigenstates are related to flavor eigenstates by the relation:

$$|B_{L,H}\rangle = \frac{1}{\sqrt{p^2 + q^2}} (|B^0\rangle \pm \frac{q}{p} |\bar{B}^0\rangle)$$

- Where

$$\mathcal{A}_{\ell\ell} = \frac{1 - |q/p|^4}{1 + |q/p|^4} = \frac{\Gamma_{12}}{M_{12}} \sin \phi \quad (\phi = -\text{Arg} \frac{M_{12}}{\Gamma_{12}})$$

- We have:

$$|q/p| = 1 - (0.3^{+1.8}_{-2.0}) \cdot 10^{-3} \quad \text{This Measurement}$$

$$|q/p| = 1 + (0.2 \pm 2.8) \cdot 10^{-3} \quad \text{Previous W.A.}$$