

# Electromagnetic fingerprints of the Little Bang\*

Ulrich Heinz  
The Ohio State University

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## Hard Probes 2013

Stellenbosch Institute for Advanced Studies, 3-8 Nov. 2013

\*Work supported by the US DOE

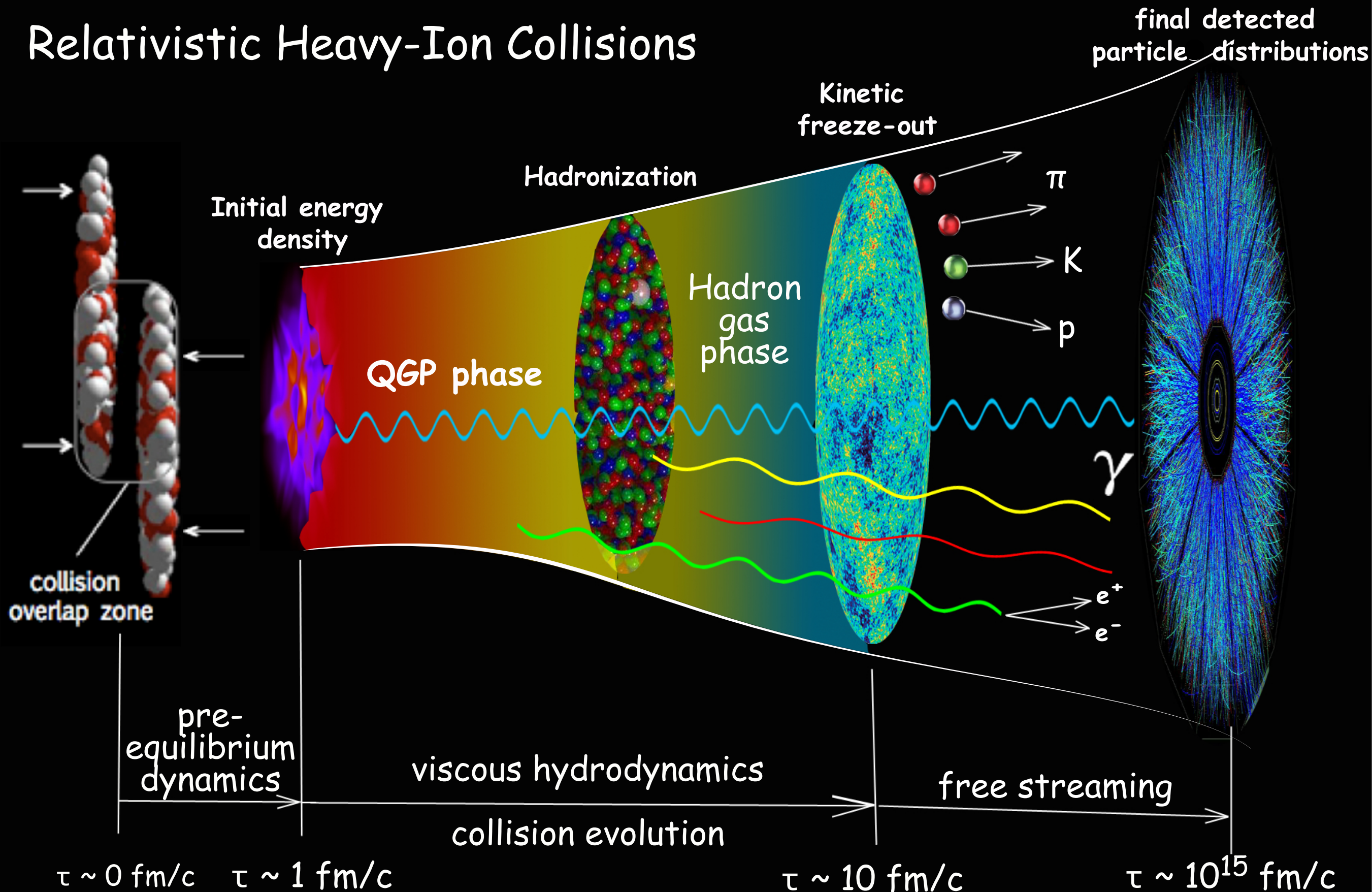


DEPARTMENT OF  
PHYSICS



# The Little Bang

## Relativistic Heavy-Ion Collisions



# Disclaimer:

Only photons, no dileptons in this talk!

(Thermal) dileptons were/will be discussed by

Antonio Uras Tue 13:50

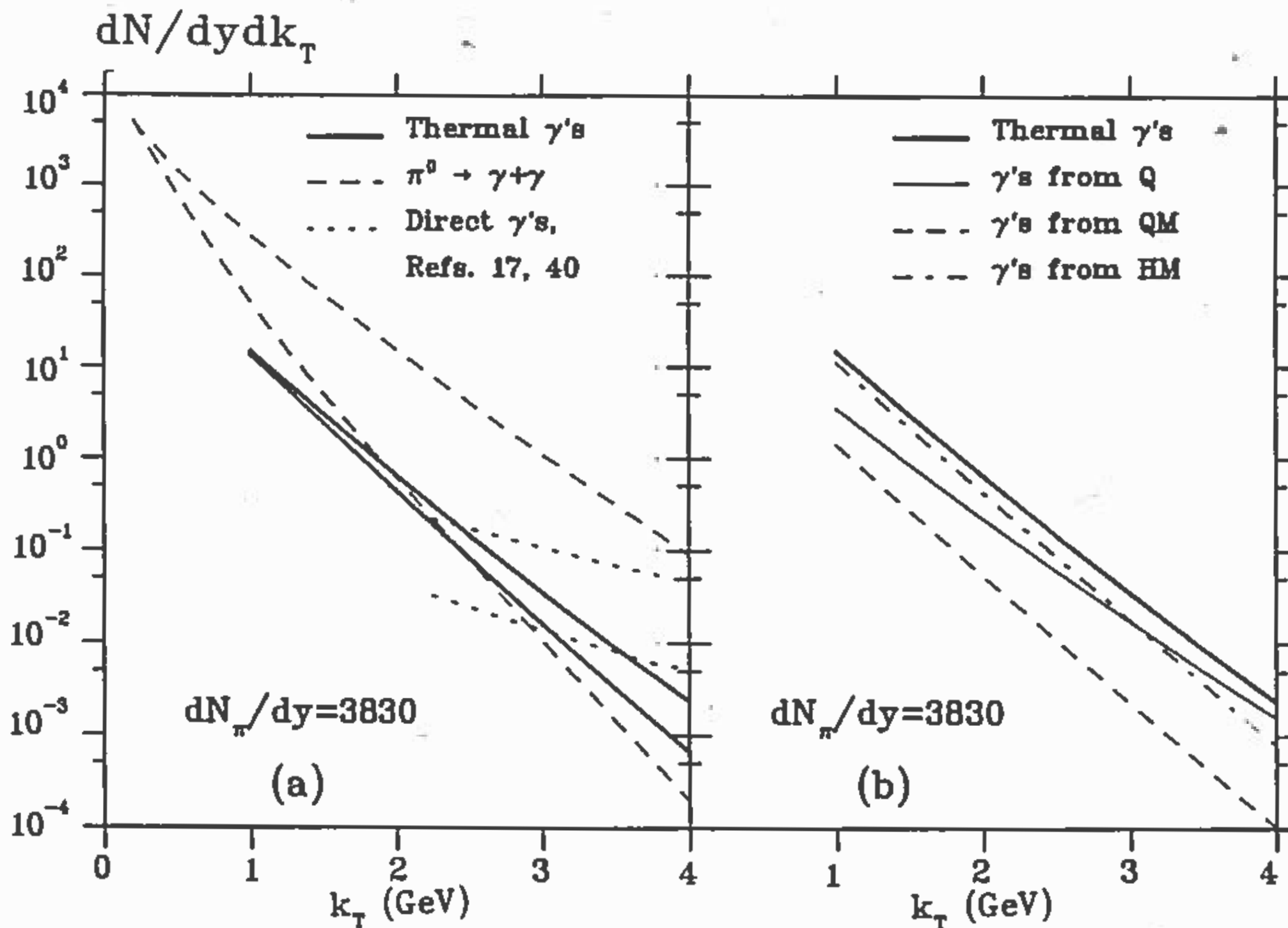
Gojko Vujanovic Tue 14:30

Mikko Laine Tue 15:10

Joey Butterworth Wed 11:00

Wolfgang Cassing Thu 15:40

# It was a long way from first predictions .....



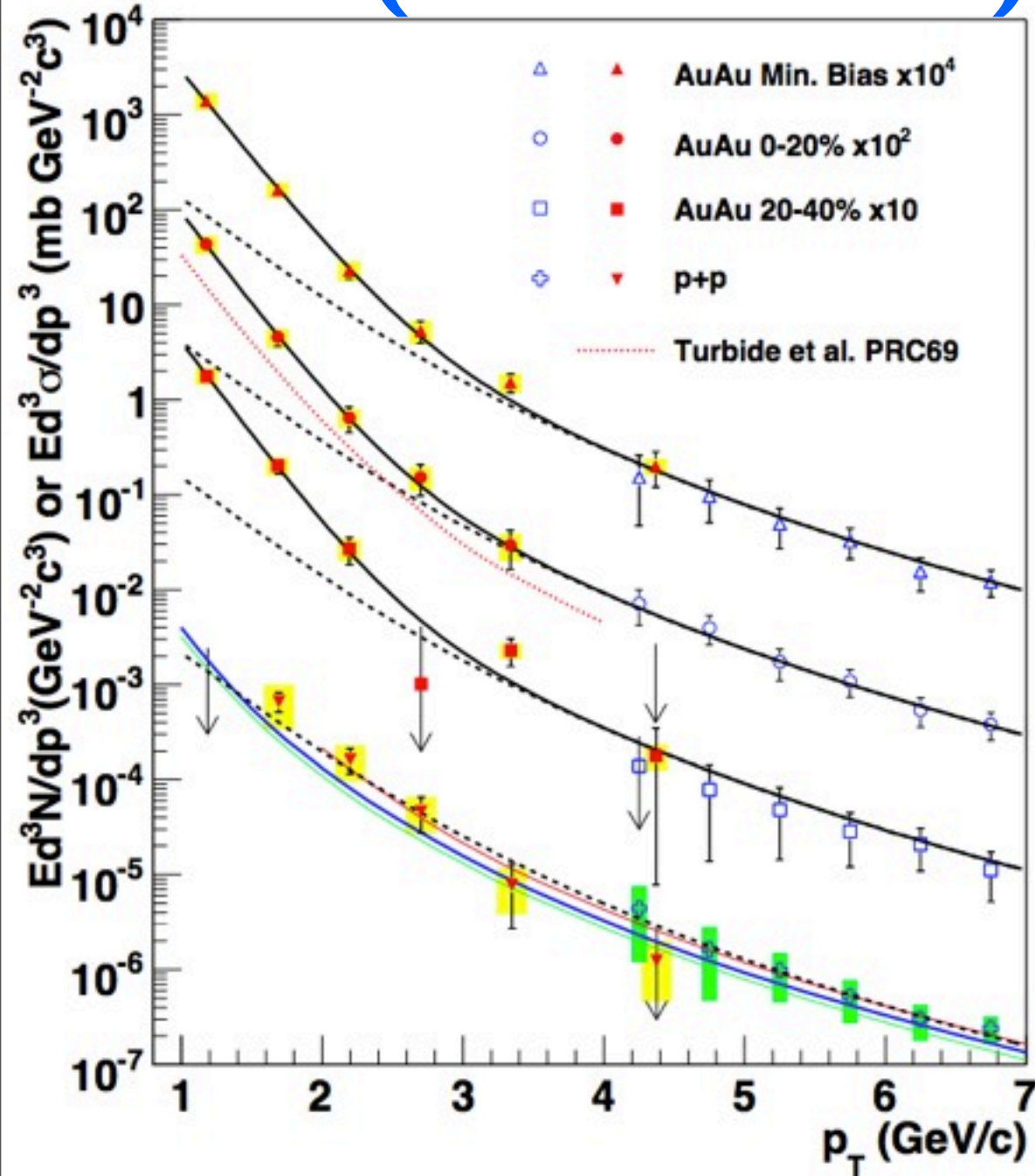
(1+1)-d ideal  
hydro with  
bag model EOS

Vesa Ruuskanen, Il Ciocco **1992** (based on work by S. Gupta)



..... to experimental data:

## RHIC (PHENIX 2010)

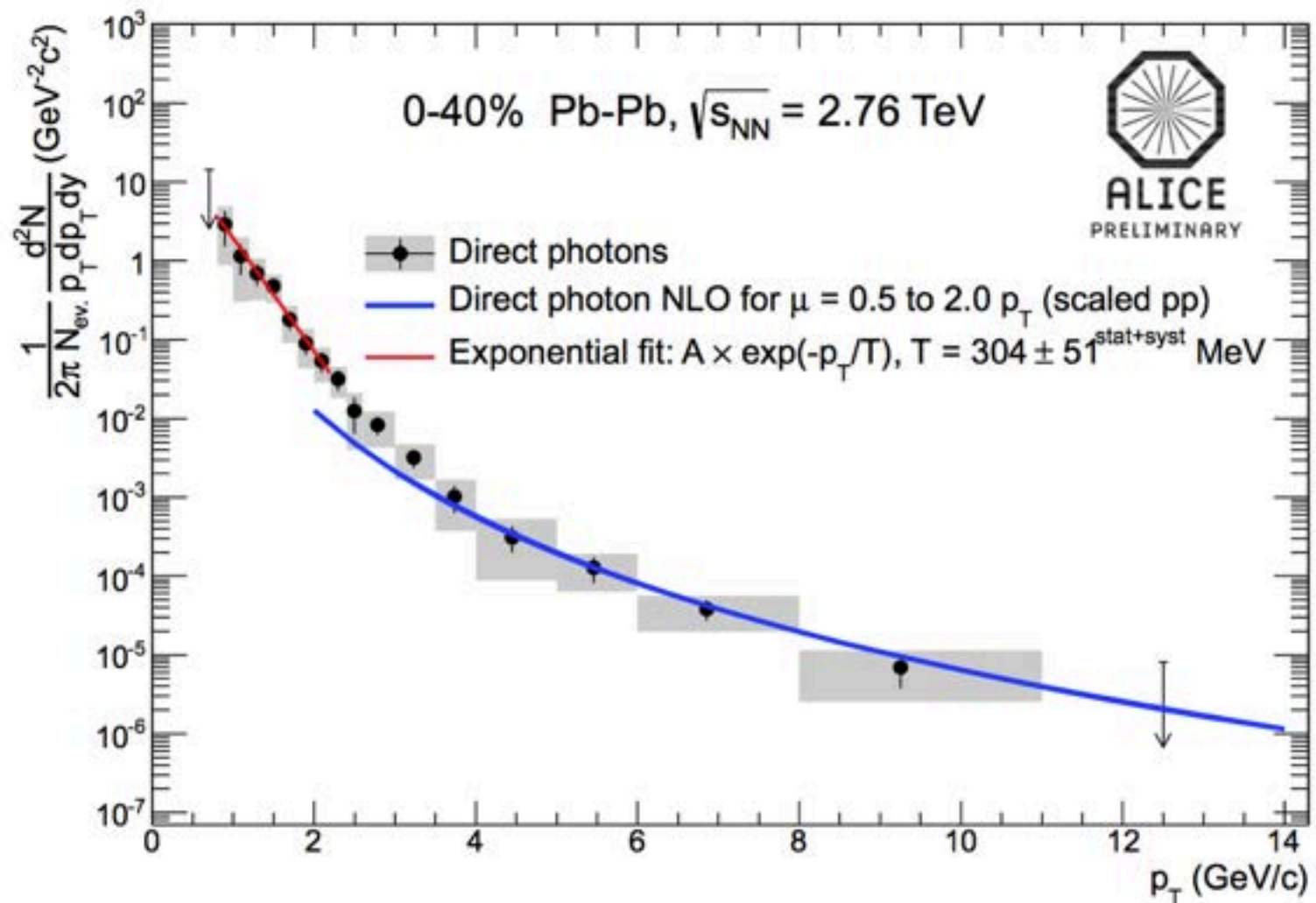


0 – 20%

$$T = 221 \pm 19 \pm 19 \text{ MeV}$$



## LHC (ALICE 2012)



fit:  $A \exp(-p_T/T)$

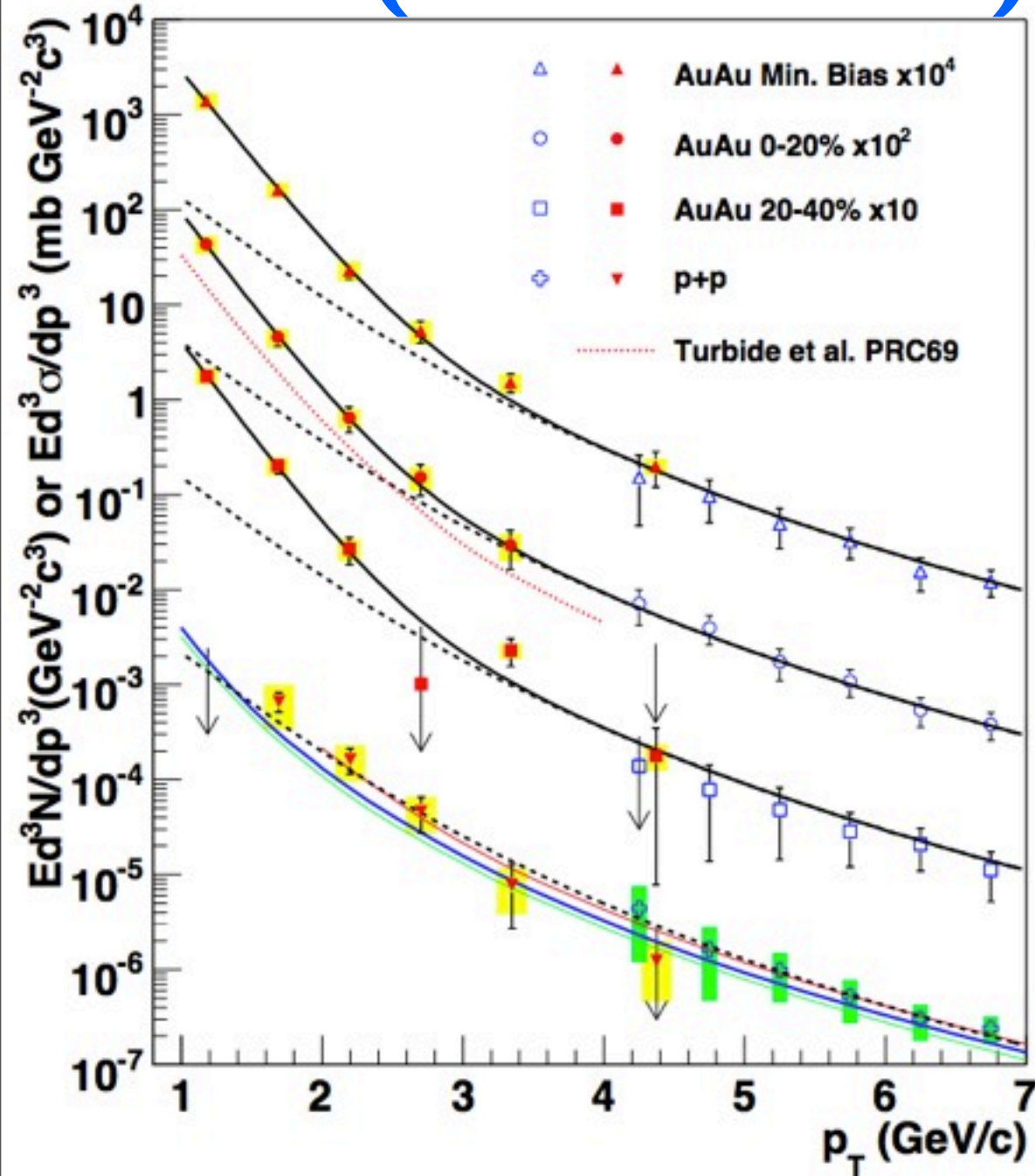
$$T = 304 \pm 51^{\text{stat+syst}} \text{ MeV}$$

(see also new PHENIX analysis presented by B. Bannier Tue 13:30)



..... to experimental data:

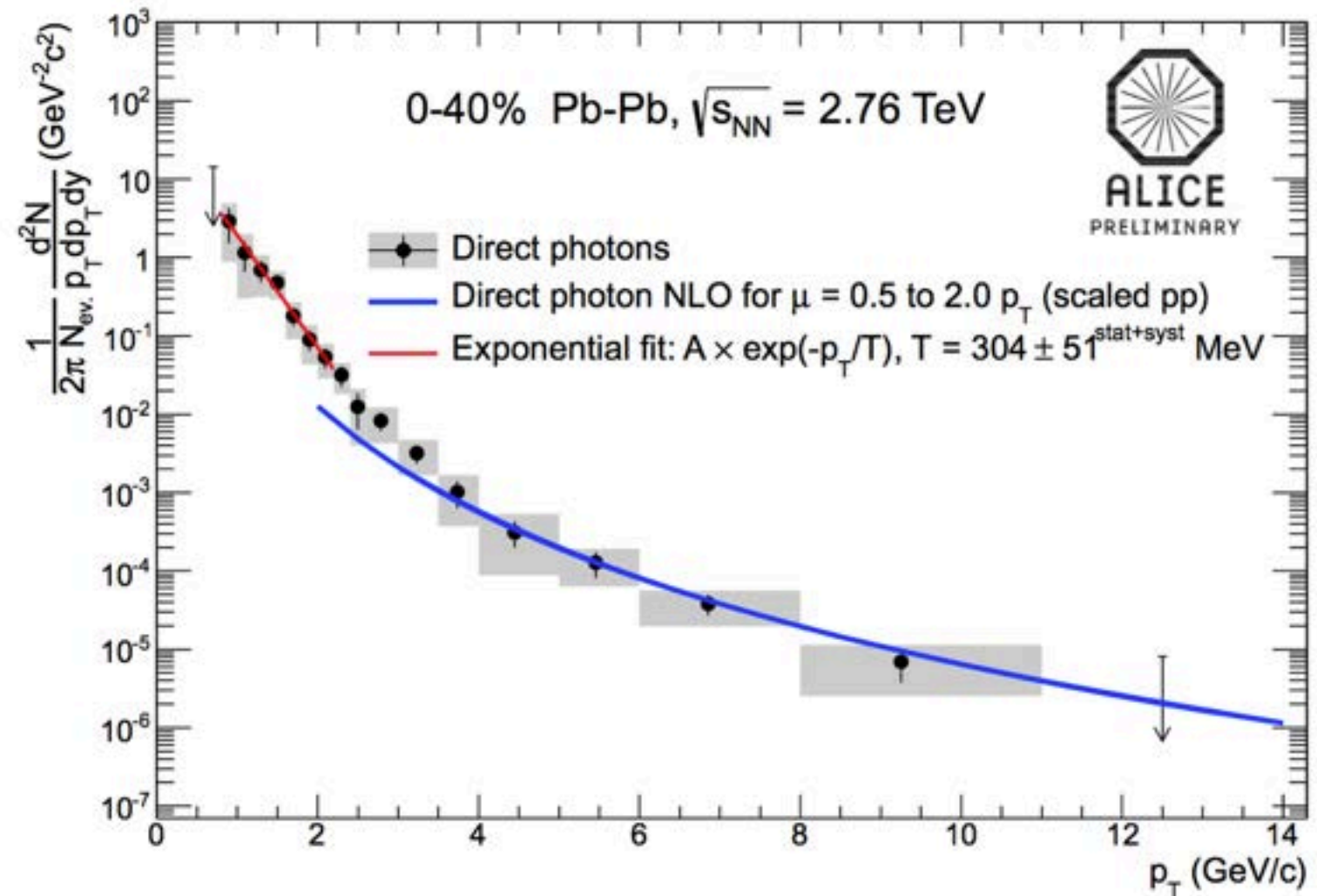
## RHIC (PHENIX 2010)



0 – 20%

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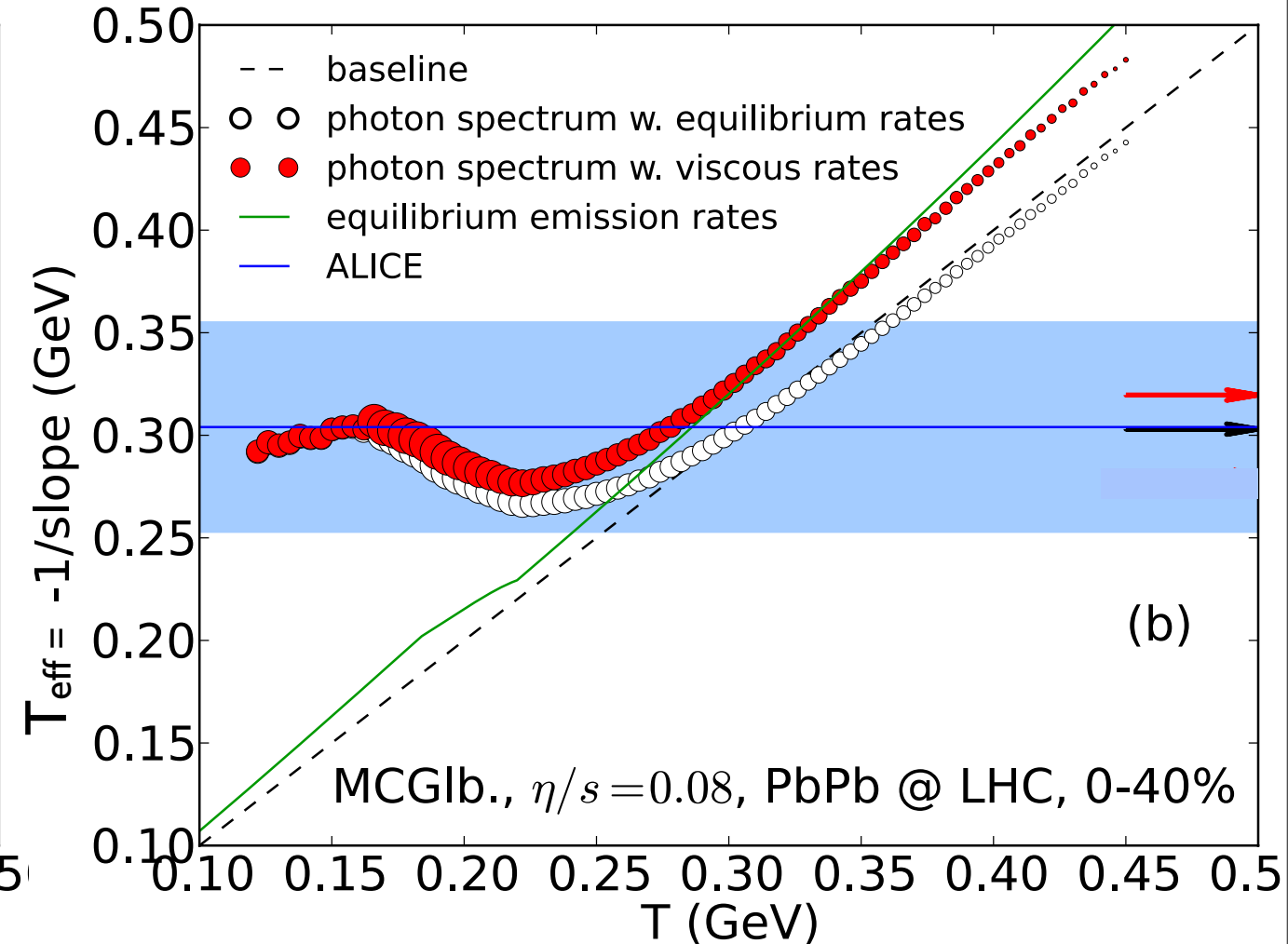
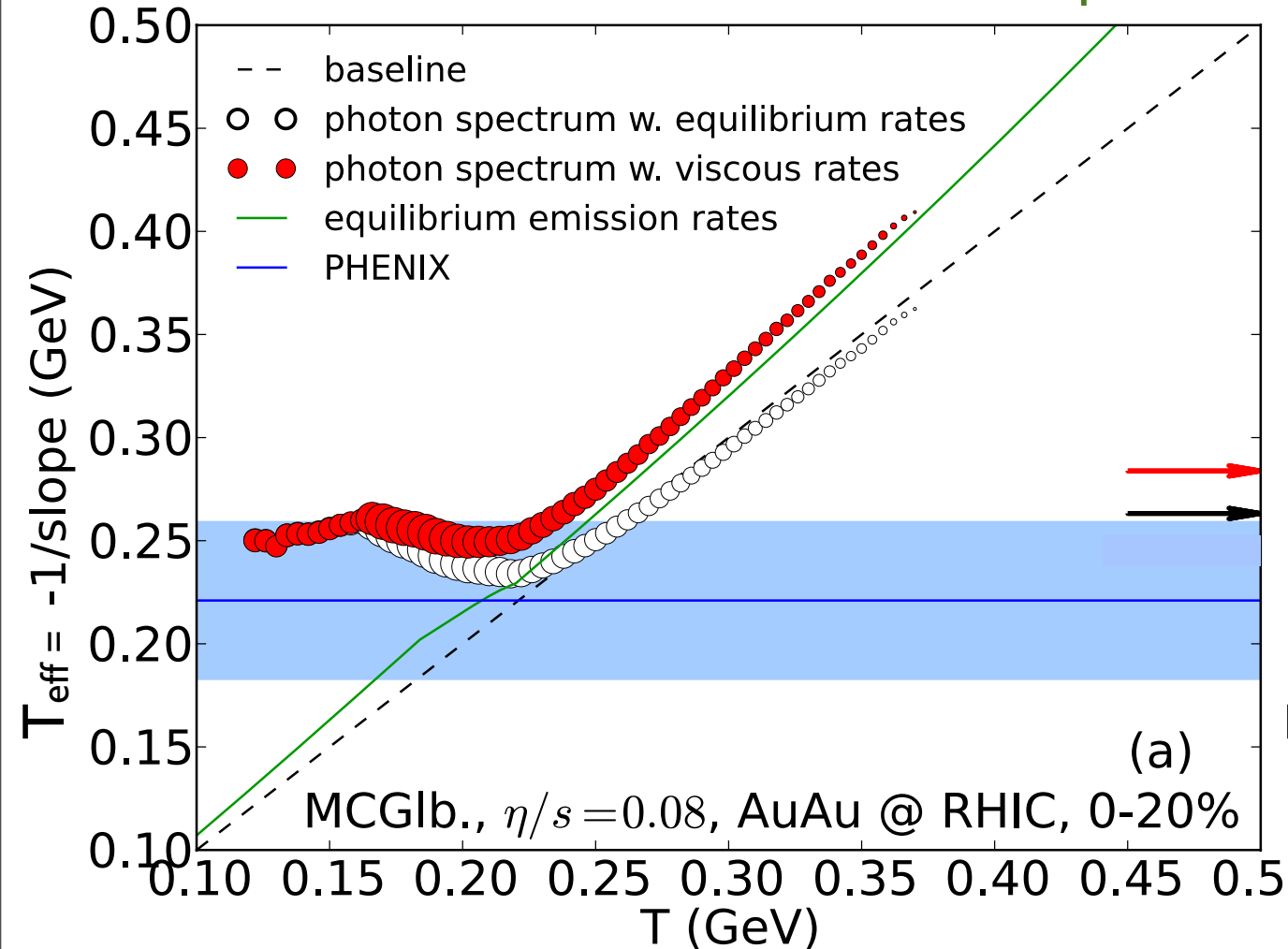
What does this T mean





# Flow-boosted photons: $T_{\text{eff}}$ vs. true temperature

Shen, UH, Paquet, Gale, arXiv:1308.2440



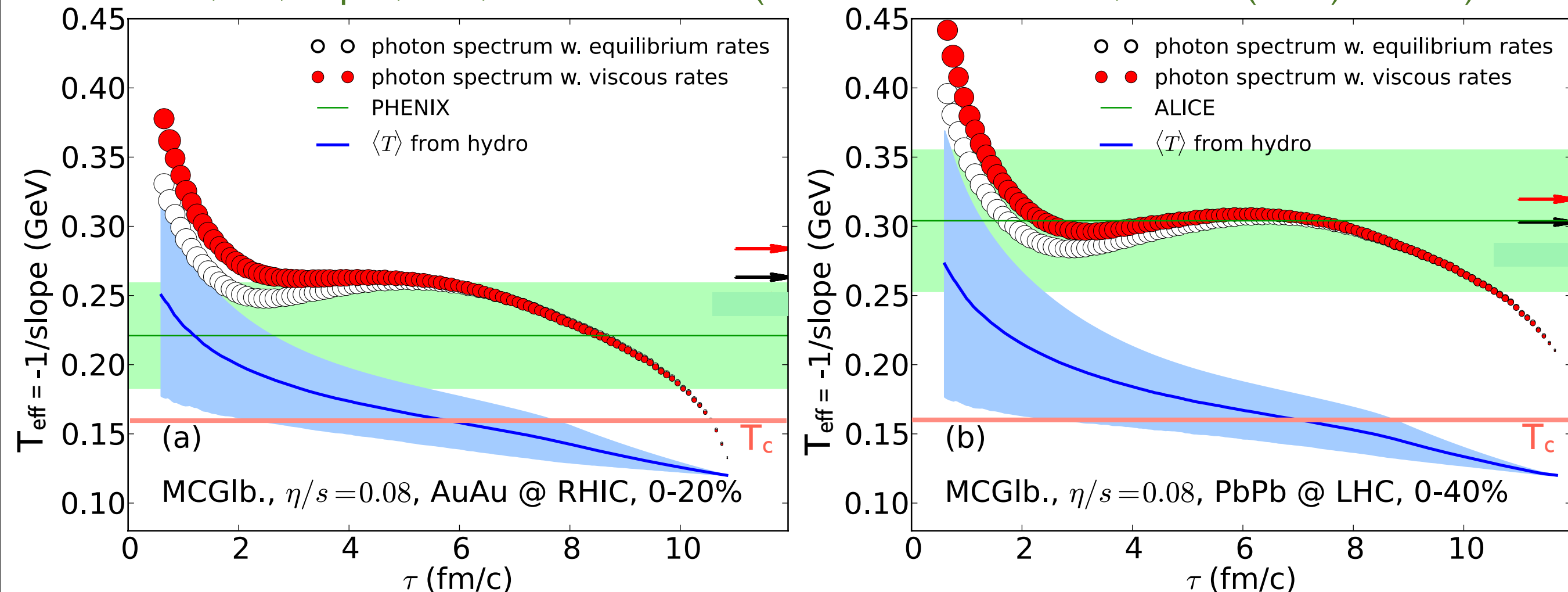
- Photon emission rates  $\propto \exp(-E/T) \log(E/T) \longrightarrow T_{\text{eff}} > T$
- **All** cells with  $T < 250$  MeV at RHIC and  $T < 300$  MeV at LHC contribute photon spectra with  $T_{\text{eff}}$  in the experimental fit range
- About **50-60%** of all photons are emitted from  $T = 165 \sim 250$  MeV; they are strongly blue-shifted by radial flow

$$T_{\text{eff}} = T \sqrt{\frac{1+v}{1-v}}$$



# $T_{\text{eff}} = -1/\text{slope}$ vs. emission time

Shen, UH, Paquet, Gale, arXiv:1308.2440 (see also van Hees et al., PRC84 (2011) 054906)

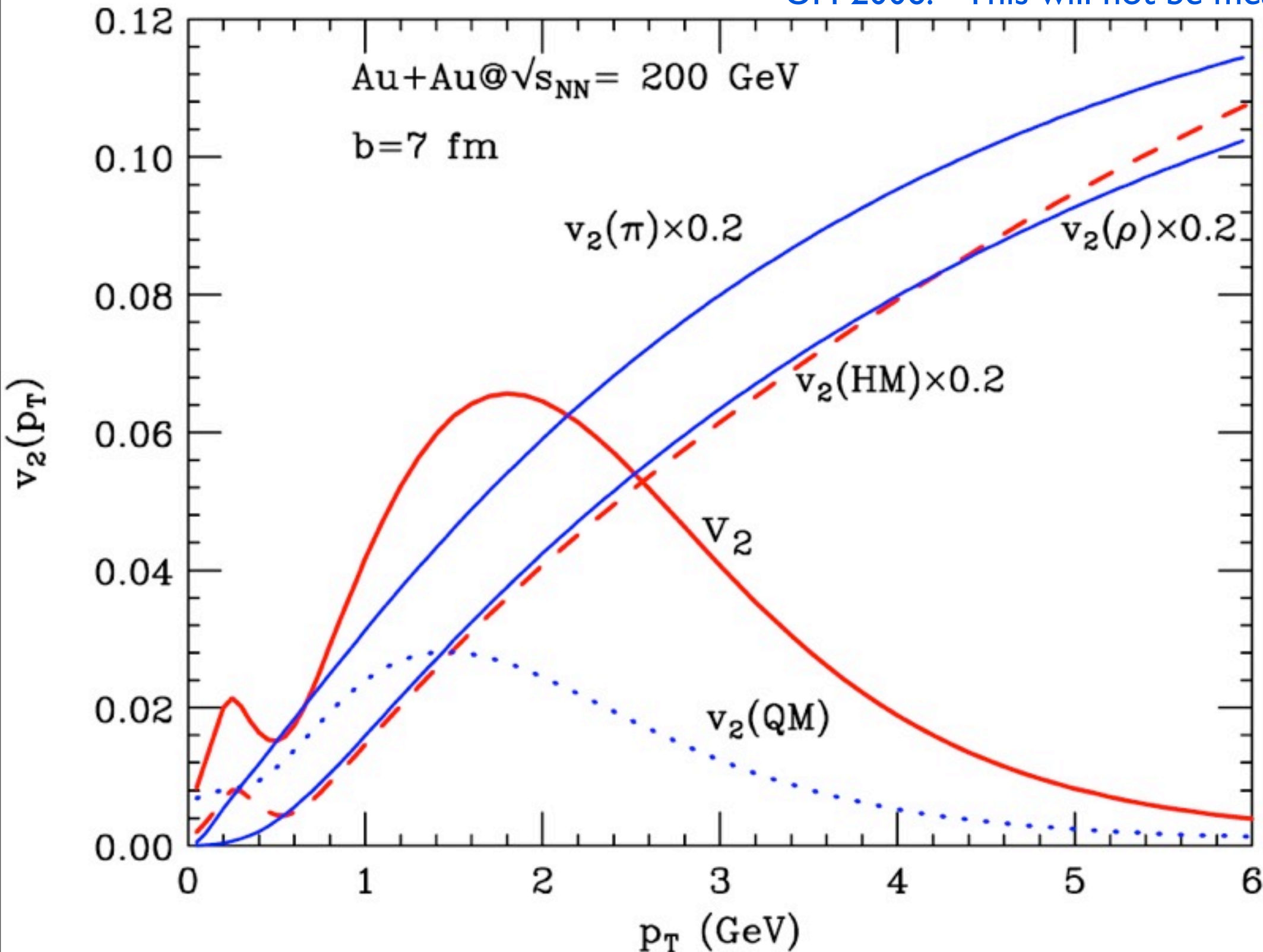


- About 25% of thermal photons are emitted in the first 2 fm/c
- After 2 fm/c, thermal photons are significantly blue shifted by radial flow
- Viscous corrections to the slope of photon spectra are stronger during the early part of the evolution



# A “safe” prediction (2006): thermal photon $v_2$

UH 2006: “This will not be measured in my lifetime!”



(2+1)-d ideal  
hydro with  
1st order  
phase trans.

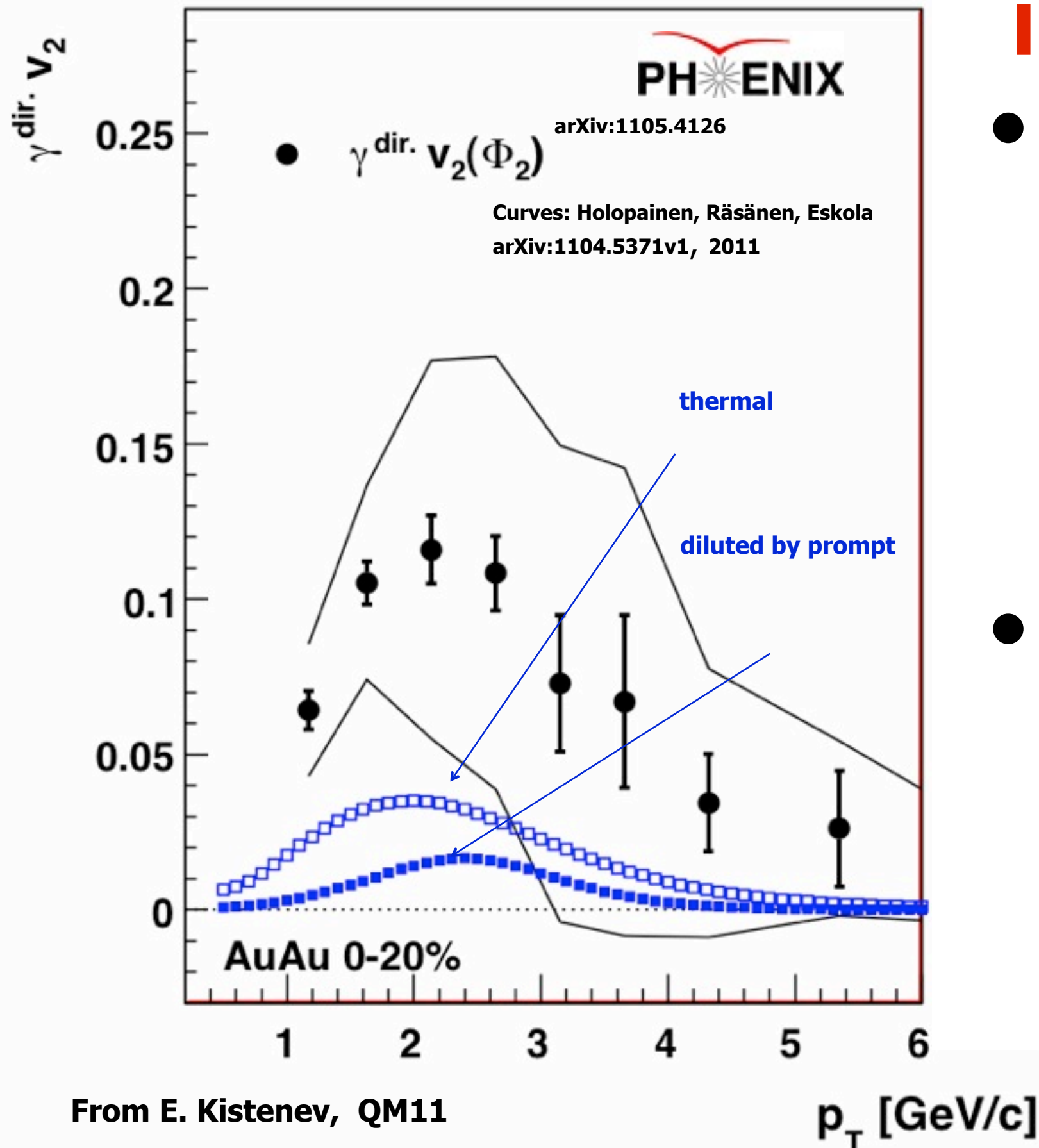
no prompt  
photons!

Chatterjee, Frodermann, UH, Srivastava, PRL 96 (2006) 202302



# Boy, was I wrong!

# PHENIX did it in 2011!



- PHENIX measurements show **large** direct photon  $v_2$  at  $p_T < 4$  GeV

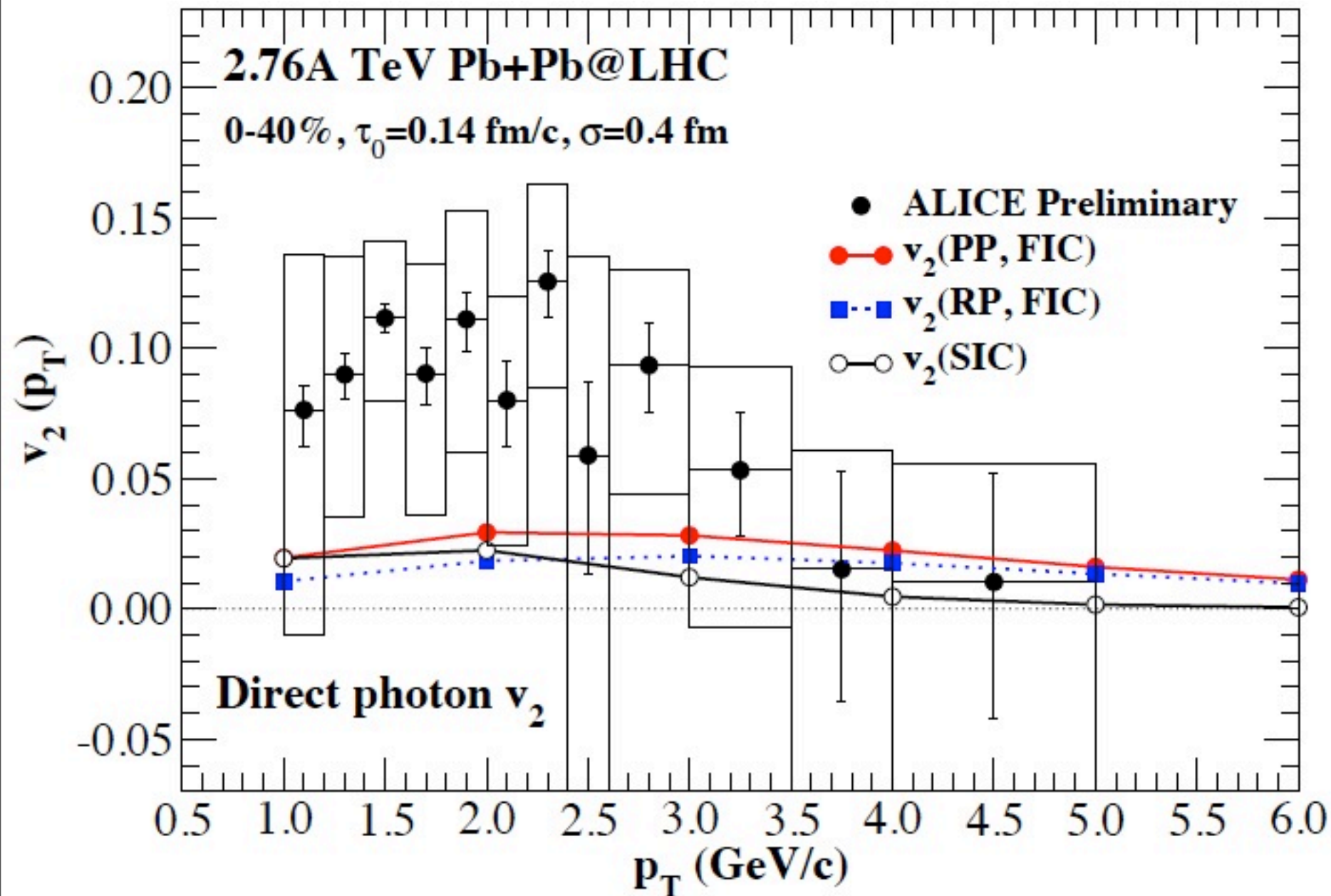
**But:**

- State-of-the-art calculations underestimate the experimental data by a factor of **5**!



# Similar problems with ALICE data (QM2012):

Chatterjee et al., PRC 88 (2013) 034901



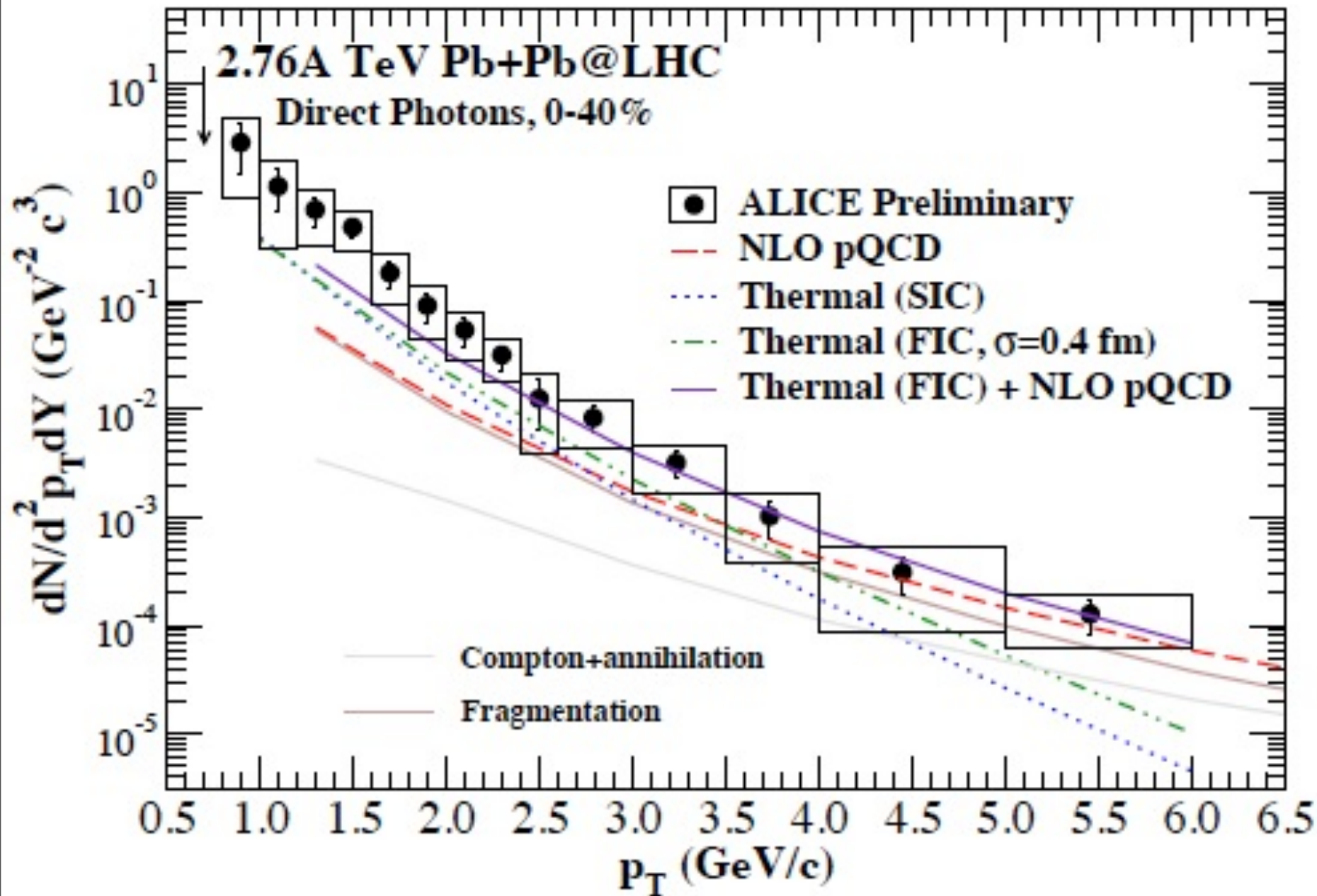
(2+1)-d ideal e-by-e hydro with fluctuating initial conds. and a lattice-motivated EOS

$v_2$  underpredicted by factor 3 in the hydrodynamic region



# Similar problems with ALICE data (QM2012):

Chatterjee et al., PRC 88 (2013) 034901



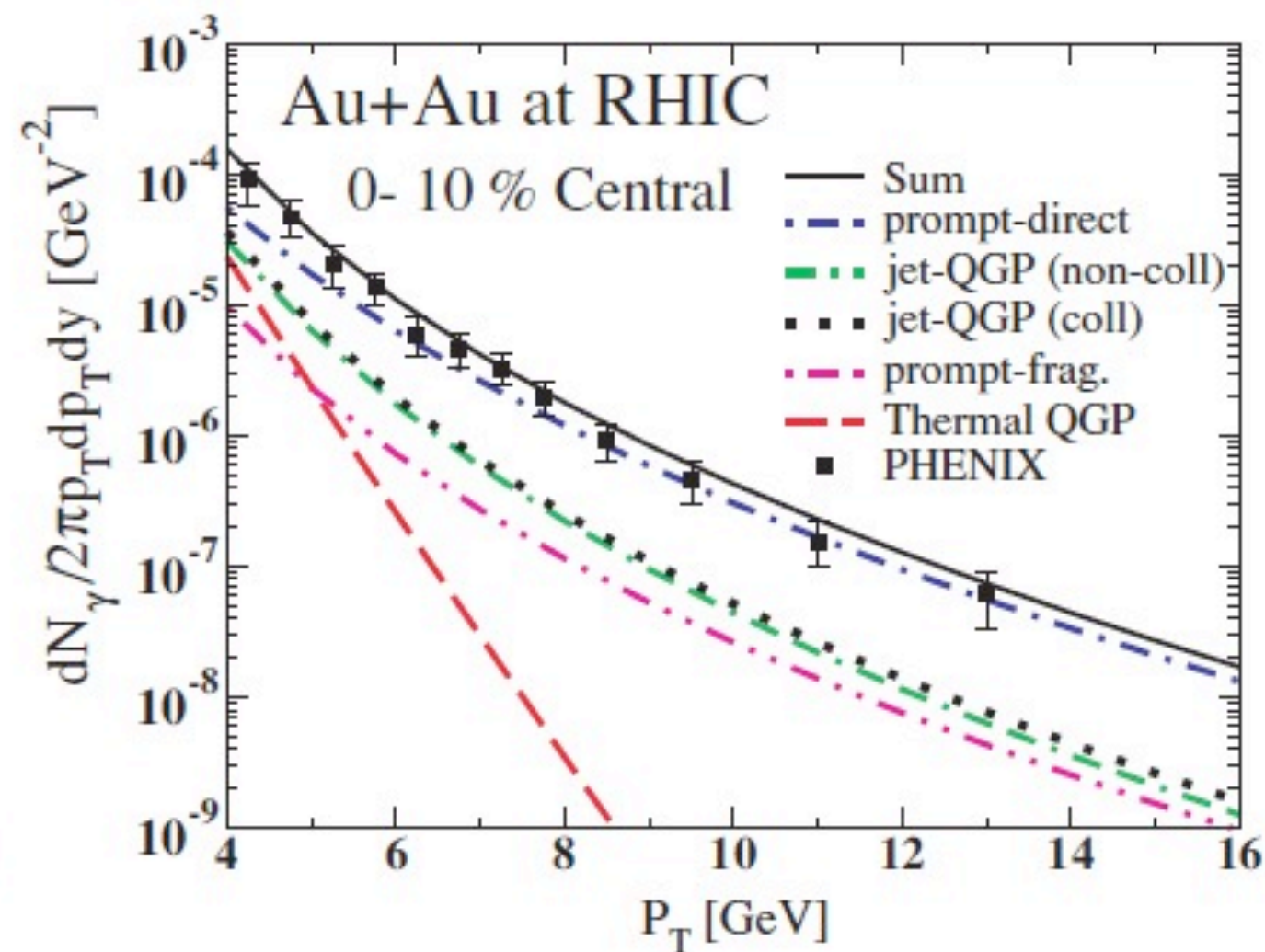
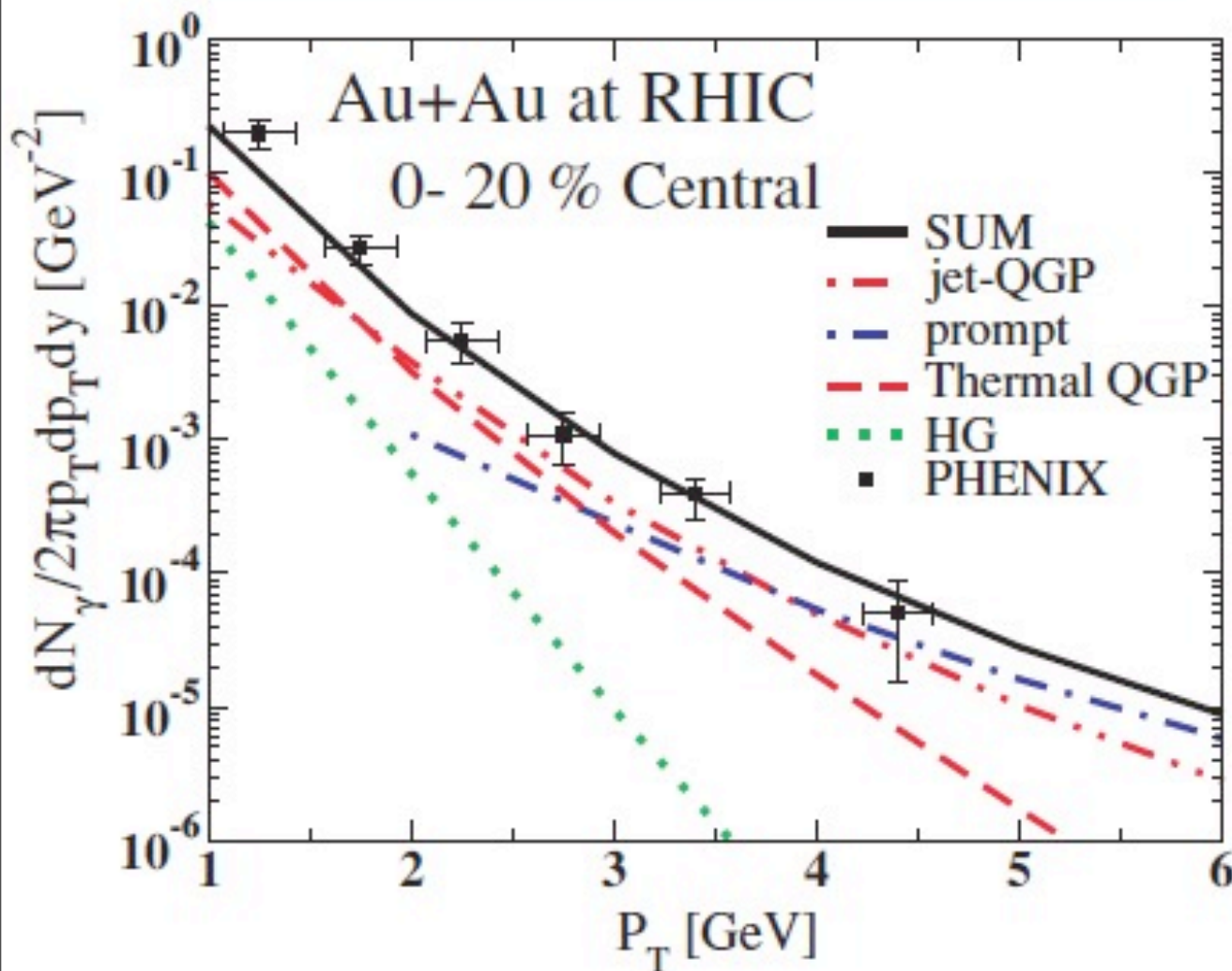
(2+1)-d ideal e-by-e hydro with fluctuating initial conds. and a lattice-motivated EOS

Missing photon yield at low  $p_T$  (also true at RHIC)



# Hard photon production appears to be under control:

Turbide et al., PRC 77 (2008) 024909



But thermal radiation component is not.

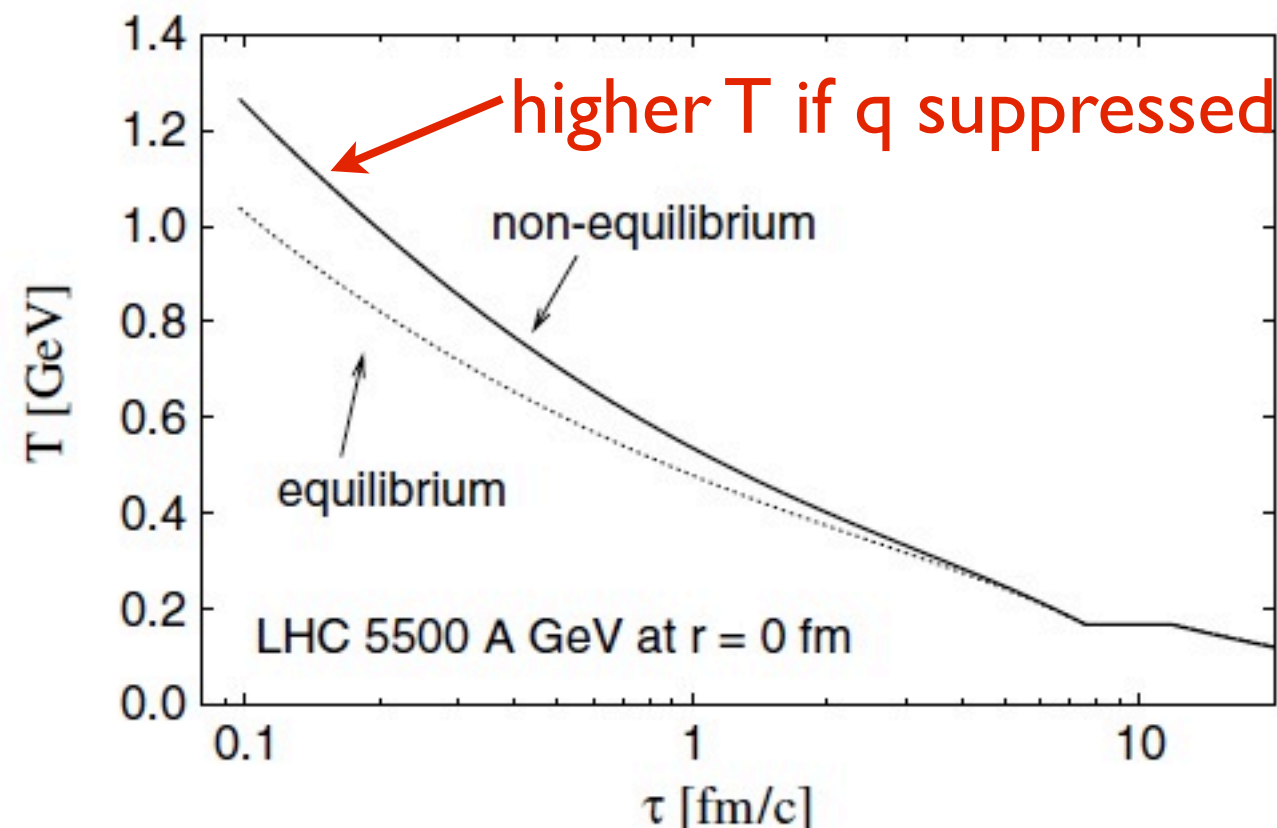
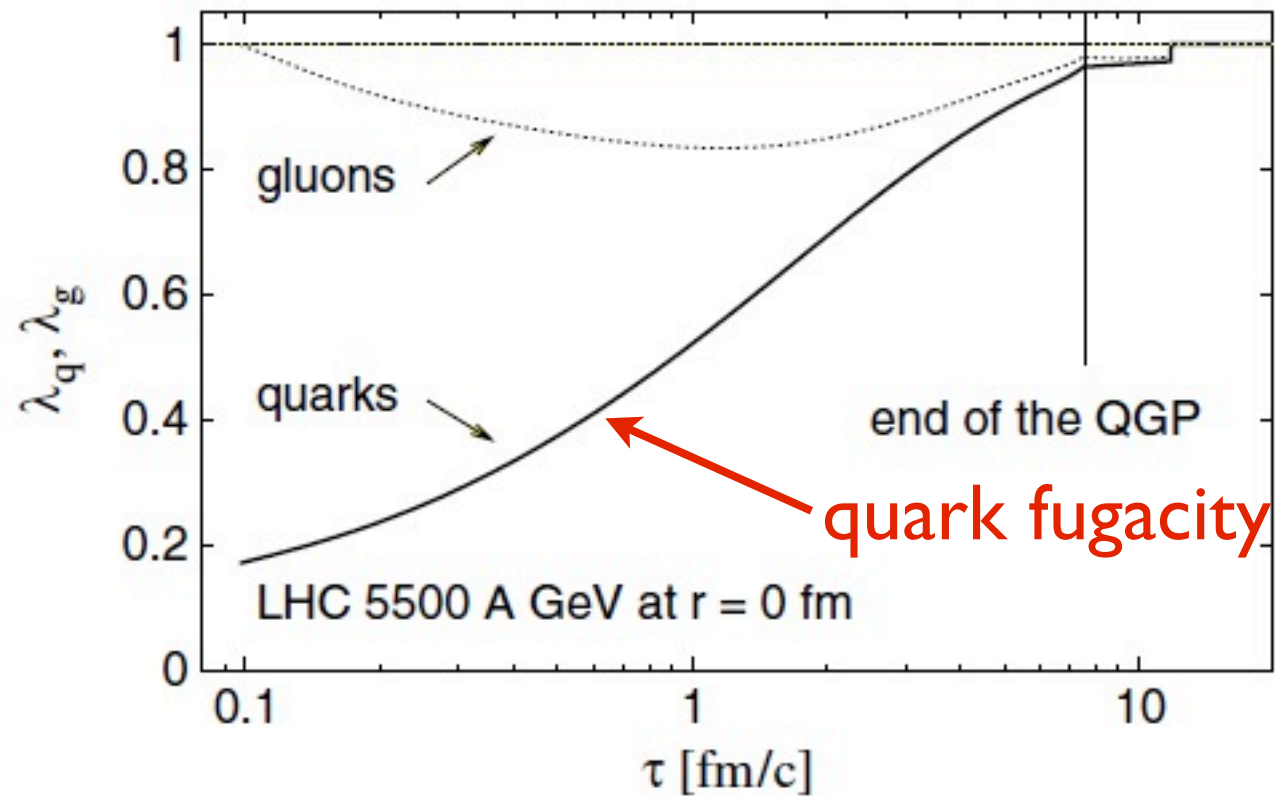
# Ingredients in s.o.t.a. thermal photon calculations:

- Initial-state e-by-e temperature fluctuations
- Event-by-event  $(2+1)$ -d or  $(3+1)$ -d hydrodynamic evolution
- Realistic lattice QCD-based EOS
- Viscous effects on hydrodynamic evolution and electromagnetic emission rates
- Addition of hard photon production channels
- Delayed chemical q-g equilibrium in QGP



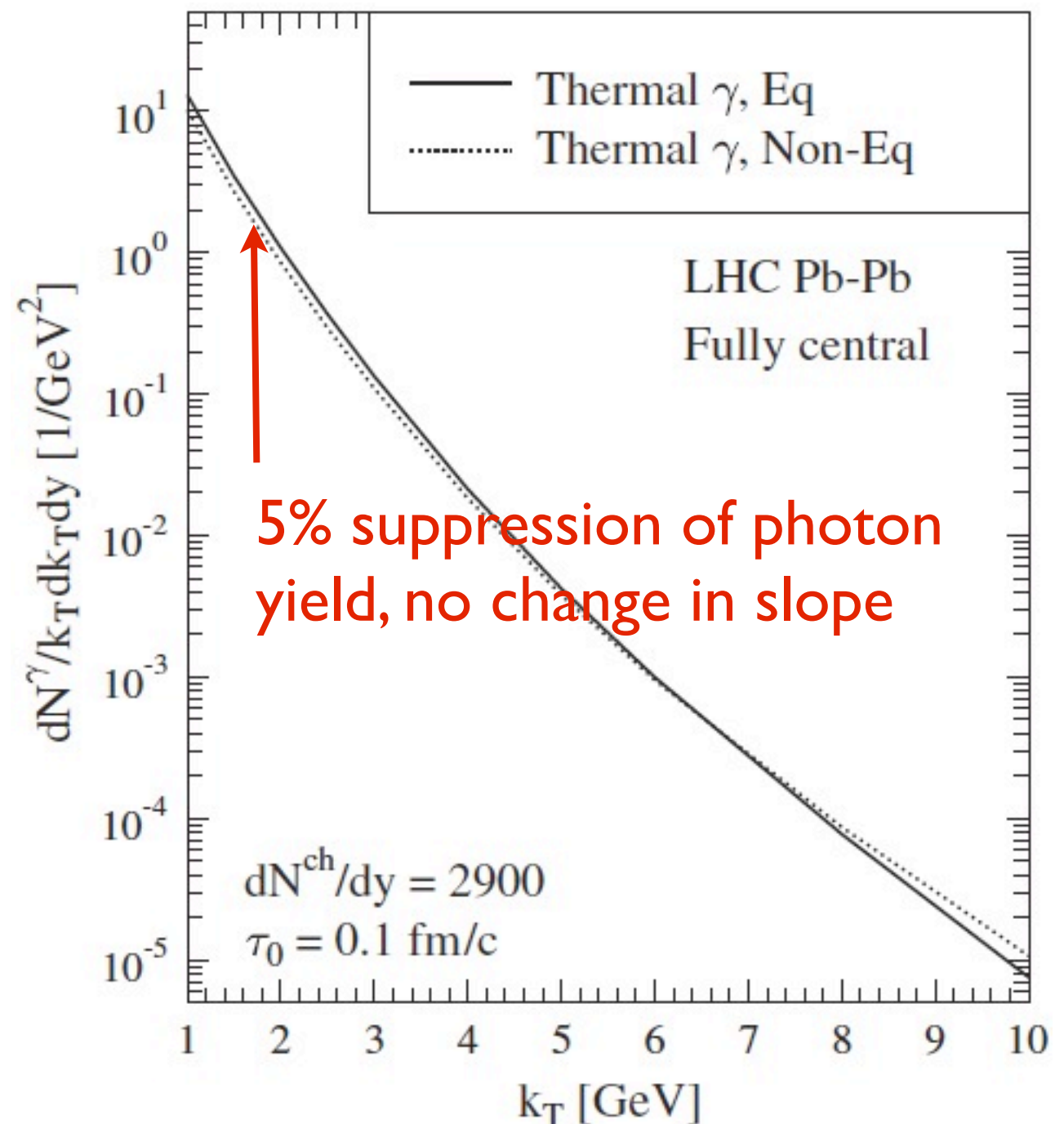


# Delayed chemical QGP equilibration doesn't much affect the photon spectra:



Gelis et al., JPG30 (2004) S1031

(see also Biro et al., PRC48 (1993) 1275)

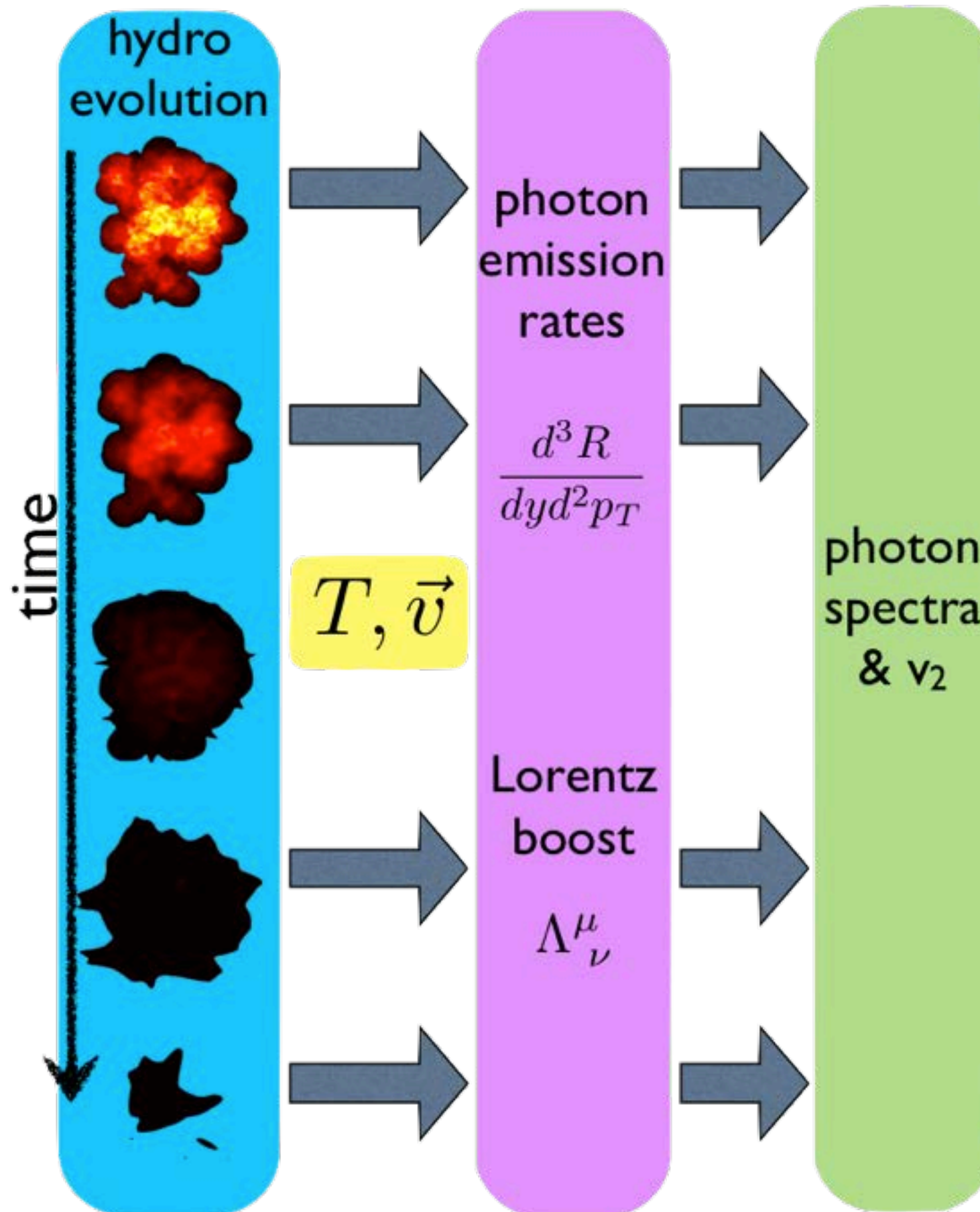


# How to deal with viscosity in thermal photon emission

Shen Mo 17:20  
Vujanovic Tue 14:30

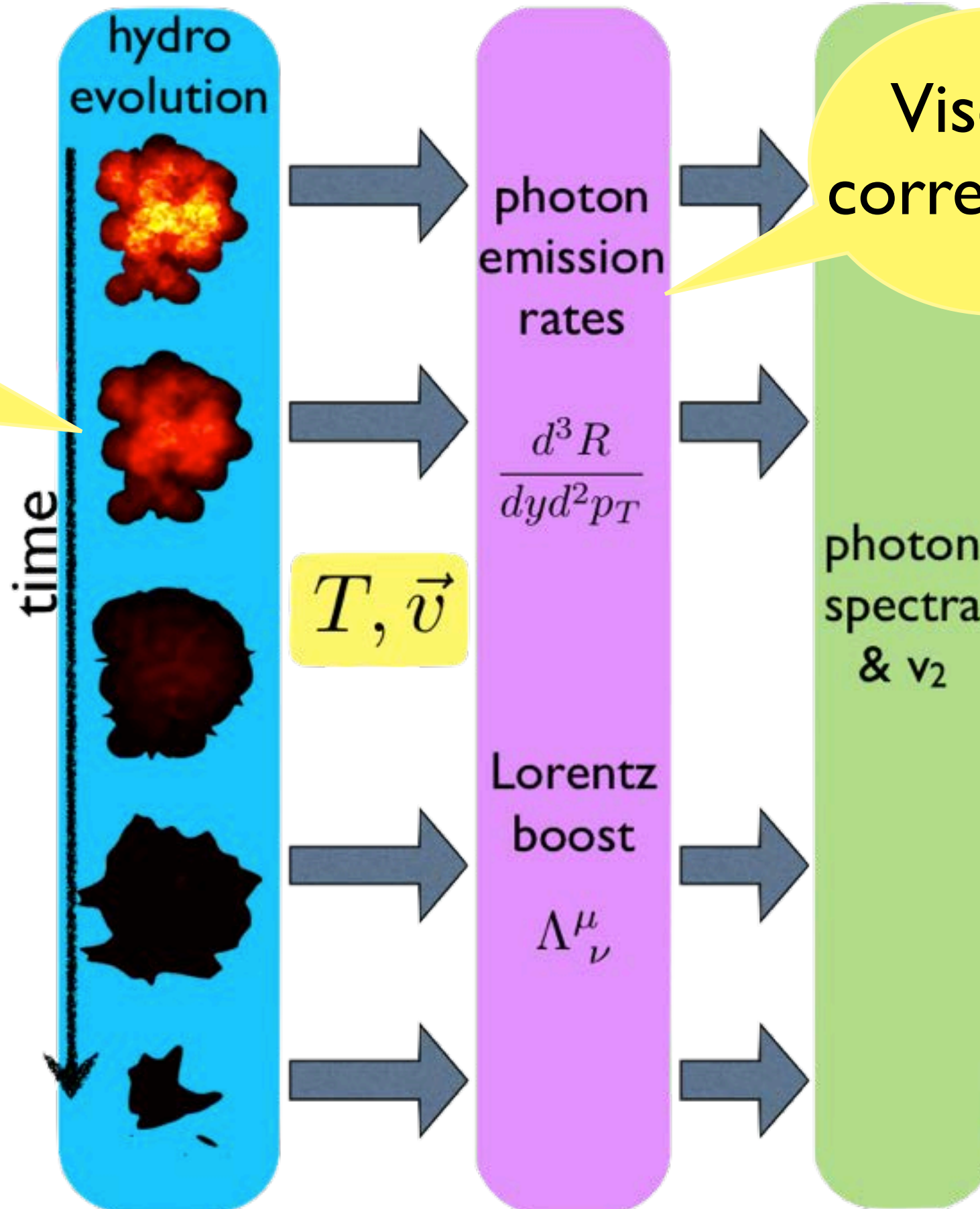


# Setting up the calculation



# Setting up the calculation

Viscous  
corrections



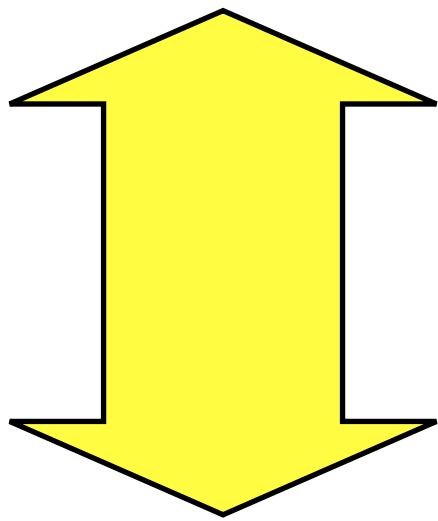
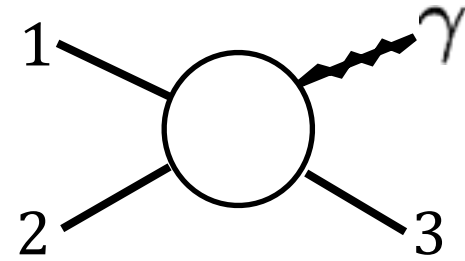
Viscous  
corrections



# Computing thermal photon emission rates

## Kinetic Approach:

$$E_q \frac{dR}{d^3q} = \int \frac{d^3p_1}{2E_1(2\pi)^3} \frac{d^3p_2}{2E_2(2\pi)^3} \frac{d^3p_3}{2E_3(2\pi)^3} \frac{1}{2(2\pi)^3} |\mathcal{M}|^2$$
$$\times f_1(E_1) f_2(E_2) (1 \mp f_3(E_3)) (2\pi)^4 \delta^{(4)}(p_1 + p_2 - p_3 - q)$$



At weak coupling these are  
equivalent in thermal  
equilibrium (KMS reln.)

## Diagrammatic Approach:

$$E_q \frac{dR}{d^3q} = \frac{i}{2(2\pi)^3} \Pi_{\mu}^{<\mu}(Q)$$

Laine Tue 15:10

C. Shen (2013): At weak coupling, high T, equivalence continues to  
hold to first order in viscous corrections

# Including viscous corrections in the rates:

E. g. in the kinetic approach

$$E_q \frac{dR}{d^3q} = \int \frac{d^3p_1}{2E_1(2\pi)^3} \frac{d^3p_2}{2E_2(2\pi)^3} \frac{d^3p_3}{2E_3(2\pi)^3} \frac{1}{2(2\pi)^3} |\mathcal{M}|^2 \\ \times f_1(p_1^\mu) f_2(p_2^\mu) (1 \pm f_3(p_3^\mu)) (2\pi)^4 \delta^{(4)}(p_1 + p_2 - p_3 - q)$$

Viscous corrections arise from momentum anisotropies in the dist. fct.:

$$f(p^\mu) = f_0(E) + f_0(E)(1 \pm f_0(E)) \frac{\pi^{\mu\nu} \hat{p}_\mu \hat{p}_\nu}{2(e + p)} \chi\left(\frac{p}{T}\right)$$

Expanding the rate around thermal equilibrium to first order in  $\pi^{\mu\nu}$ :

$$q \frac{dR}{d^3q} = \Gamma_0 + \frac{\pi^{\mu\nu} \hat{q}_\mu \hat{q}_\nu}{2(e + p)} a_{\alpha\beta} \Gamma^{\alpha\beta},$$

work out in global  
(hydro) frame

work out and tabulate as fct. of  $q/T$   
in l.r.f. aligned with photon mom.

$$a_{\mu\nu} = \frac{3}{2(u \cdot \hat{q})^4} \hat{q}_\mu \hat{q}_\nu + \frac{1}{(u \cdot \hat{q})^2} u_\mu u_\nu + \frac{1}{2(u \cdot \hat{q})^2} g_{\mu\nu} - \frac{3}{2(u \cdot \hat{q})^3} (\hat{q}_\mu u_\nu + \hat{q}_\nu u_\mu).$$

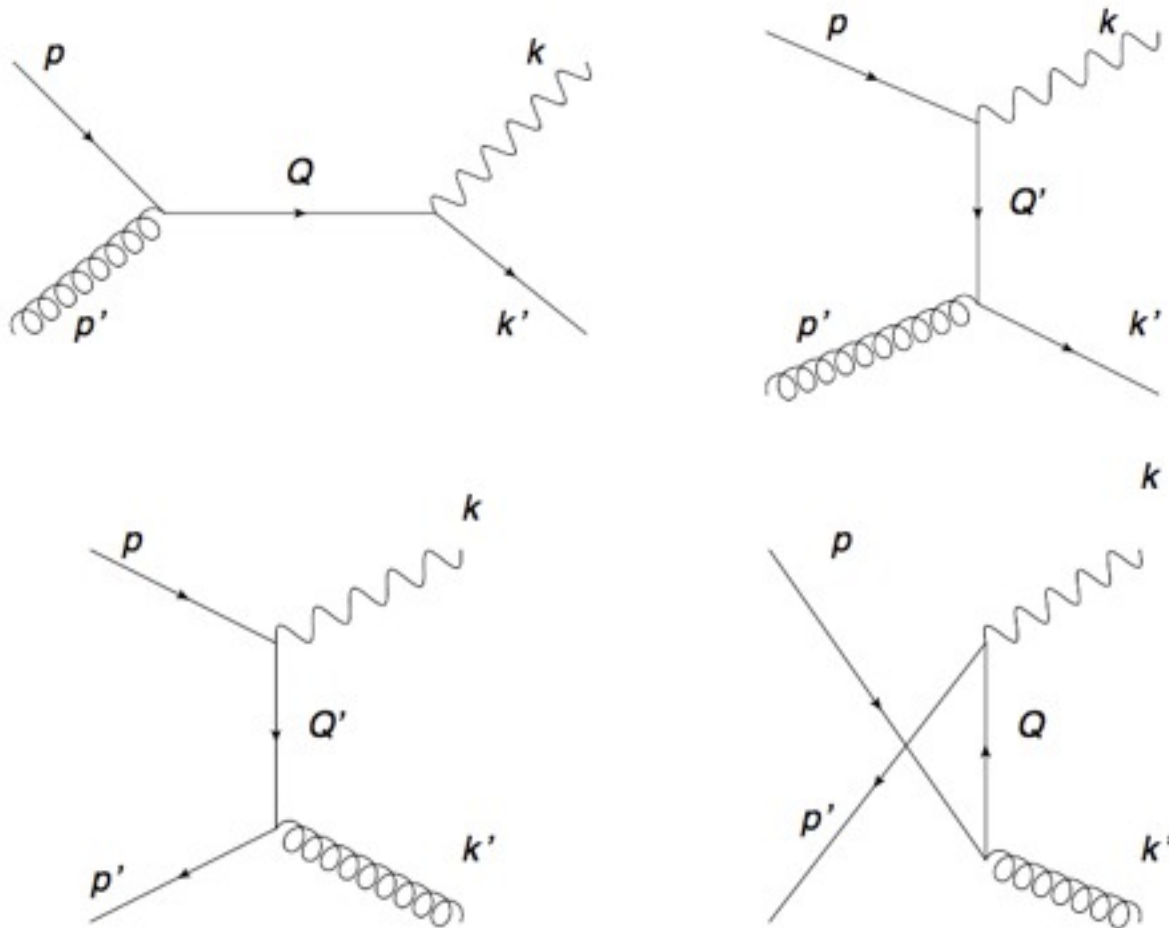


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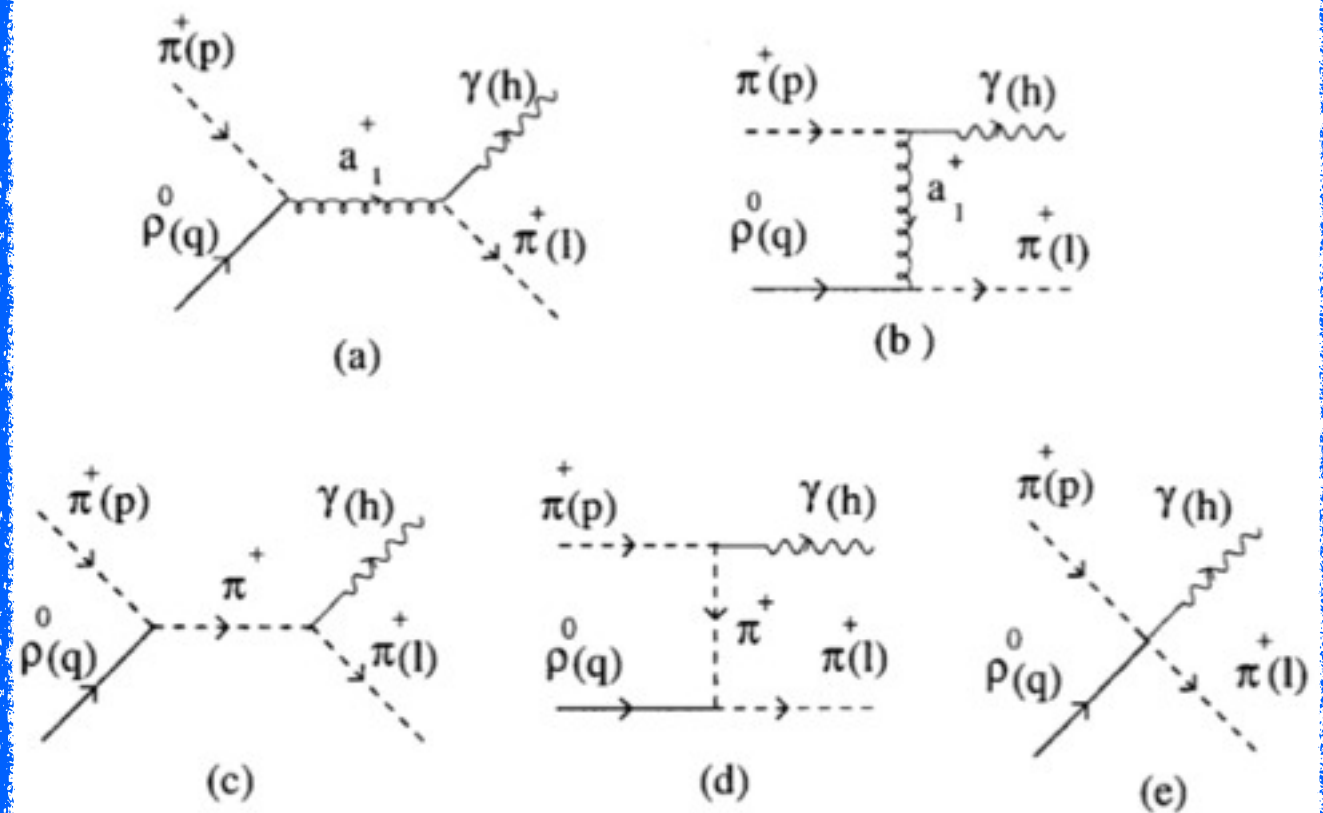
$$q \frac{dR}{d^3q} = \Gamma_0 + \frac{\pi^{\mu\nu} \hat{q}_\mu \hat{q}_\nu}{2(e+p)} a_{\alpha\beta} \Gamma^{\alpha\beta}$$

Equilibrium rates

## QGP



## Hadron Gas



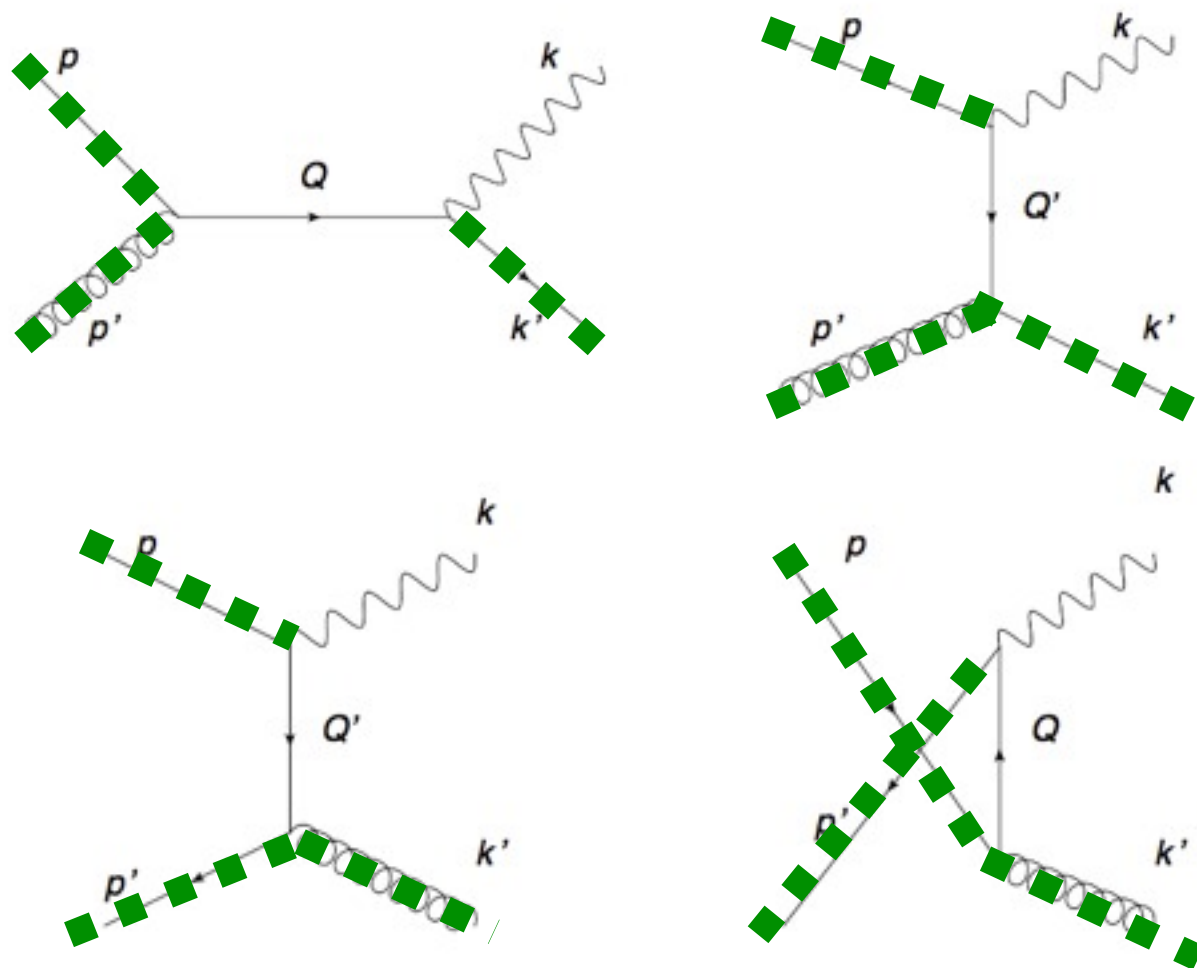
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Equilibrium rates

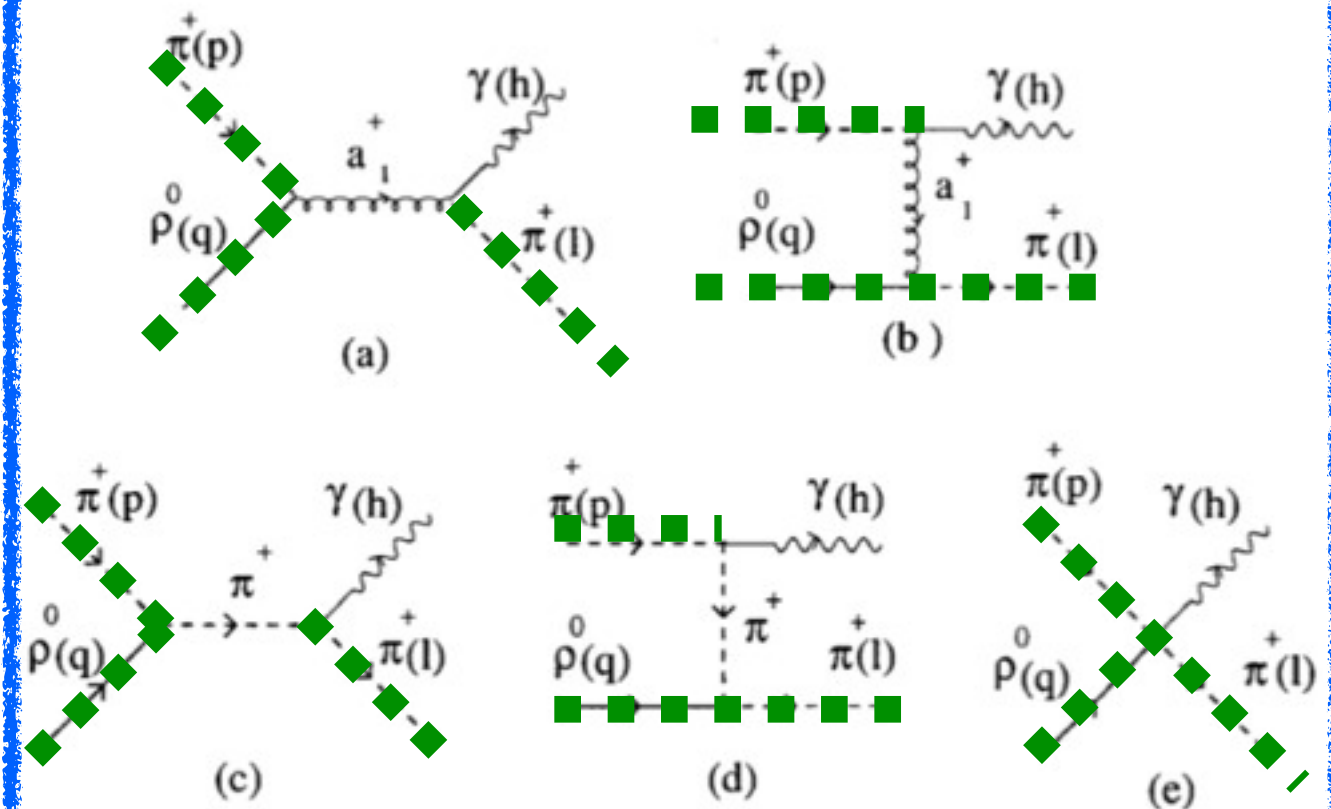
off-equilibrium  $\delta f$  corrections

## QGP



Dusling NPA839 (2010) 70

## Hadron Gas



Dion et al. PRC84 (2011) 064901



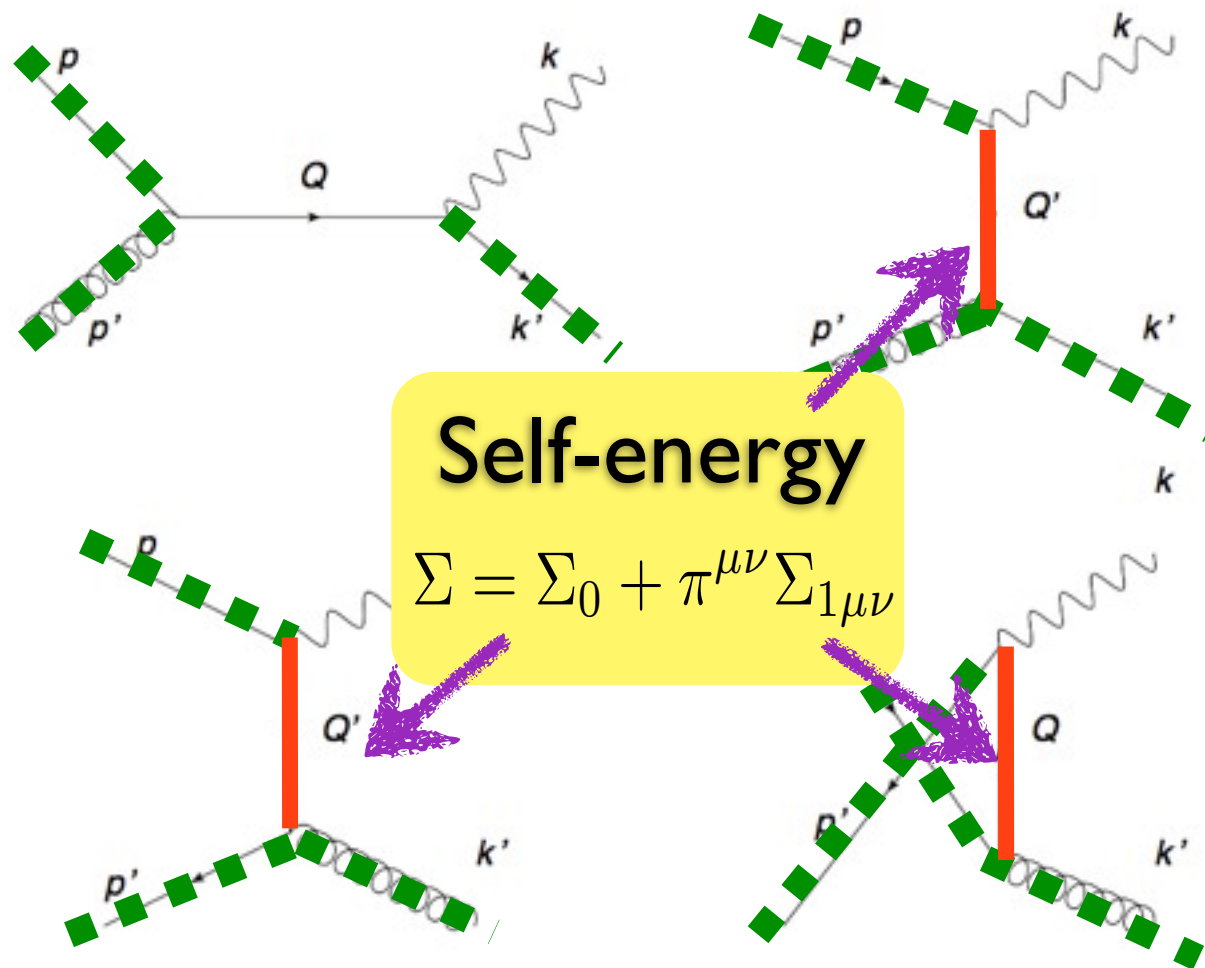
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Equilibrium rates

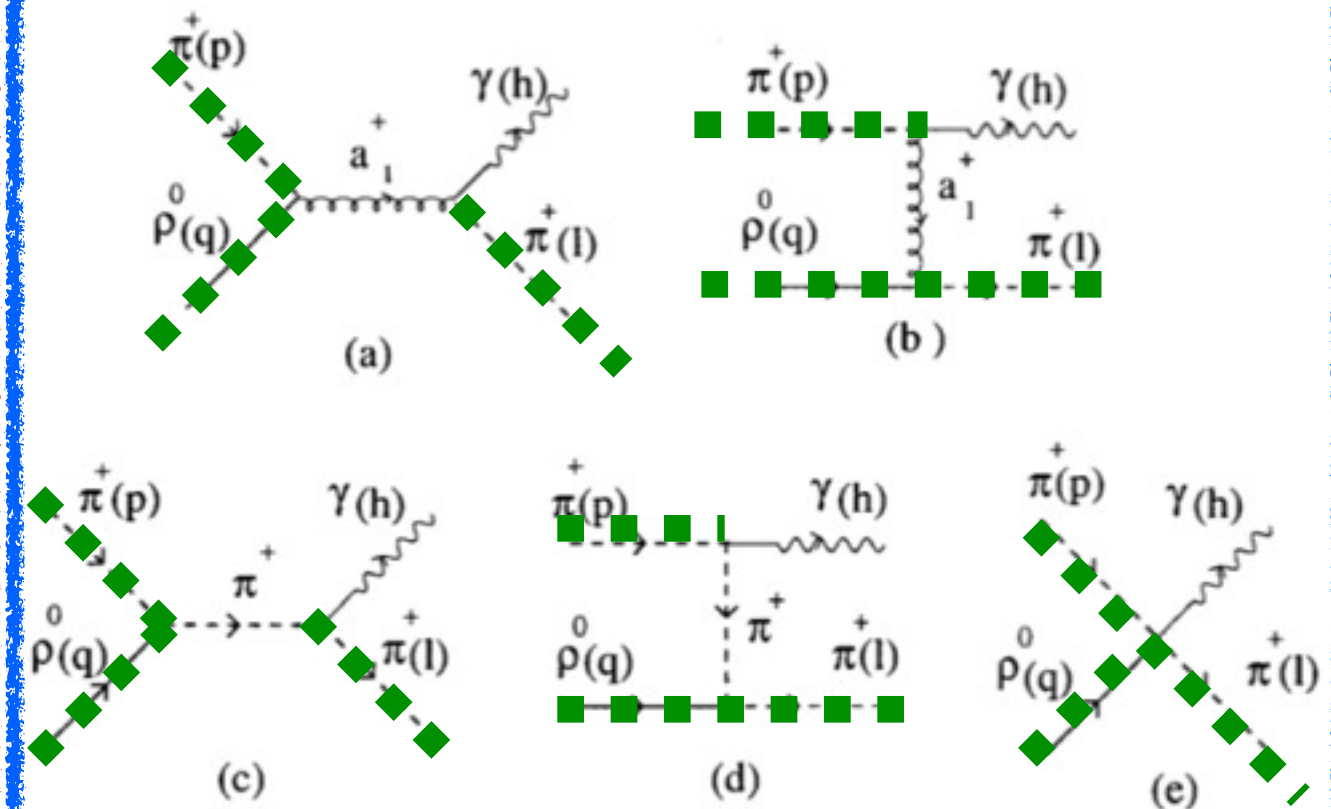
off-equilibrium  $\delta f$  corrections

**QGP**



Shen, Paquet et al. (2013)

**Hadron Gas**



# Present status of the calculation:

(i) 2 to 2 processes in Hadron Gas

QGP



(ii) Equivalence of diagrammatic and kinetic approaches for 2 to 2 processes in weakly coupled QGP

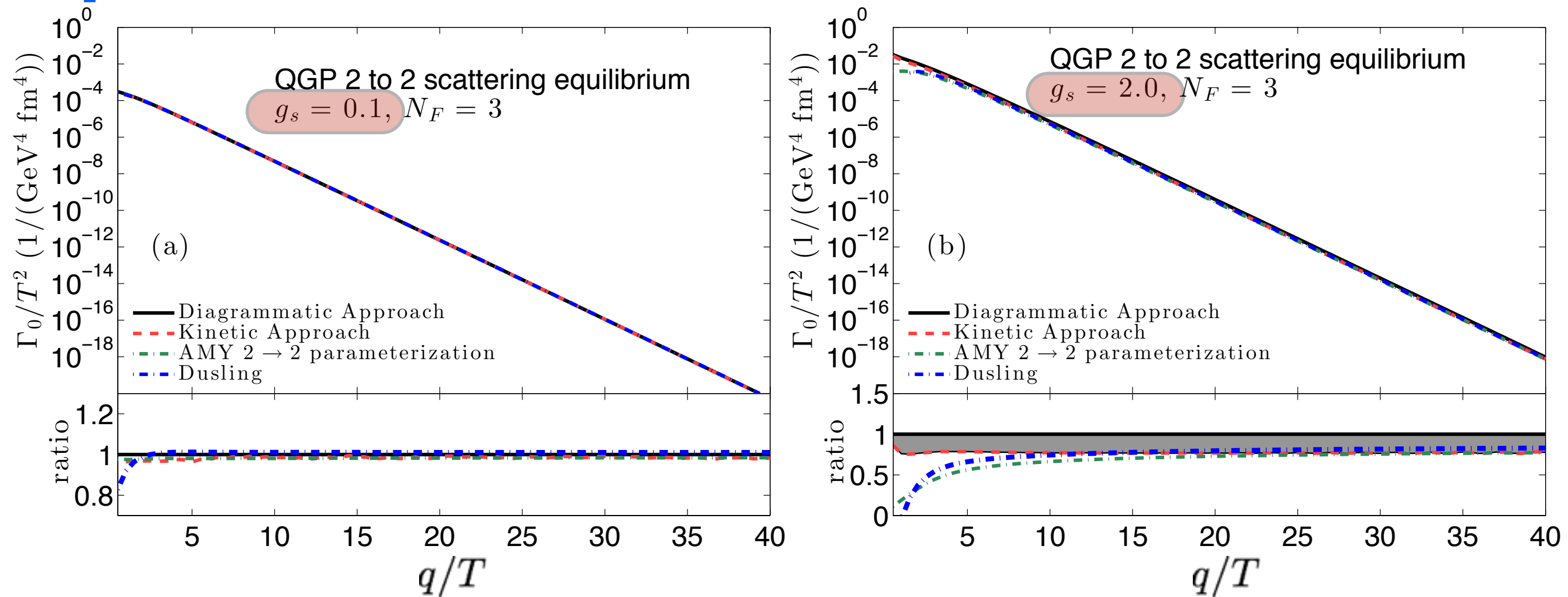


(iii) Viscous corrections to resummed AMY kernel for collinear photon emissions --- in progress  
(Shen, Paquet)



# Equivalence of kinetic and diagrammatic approaches:

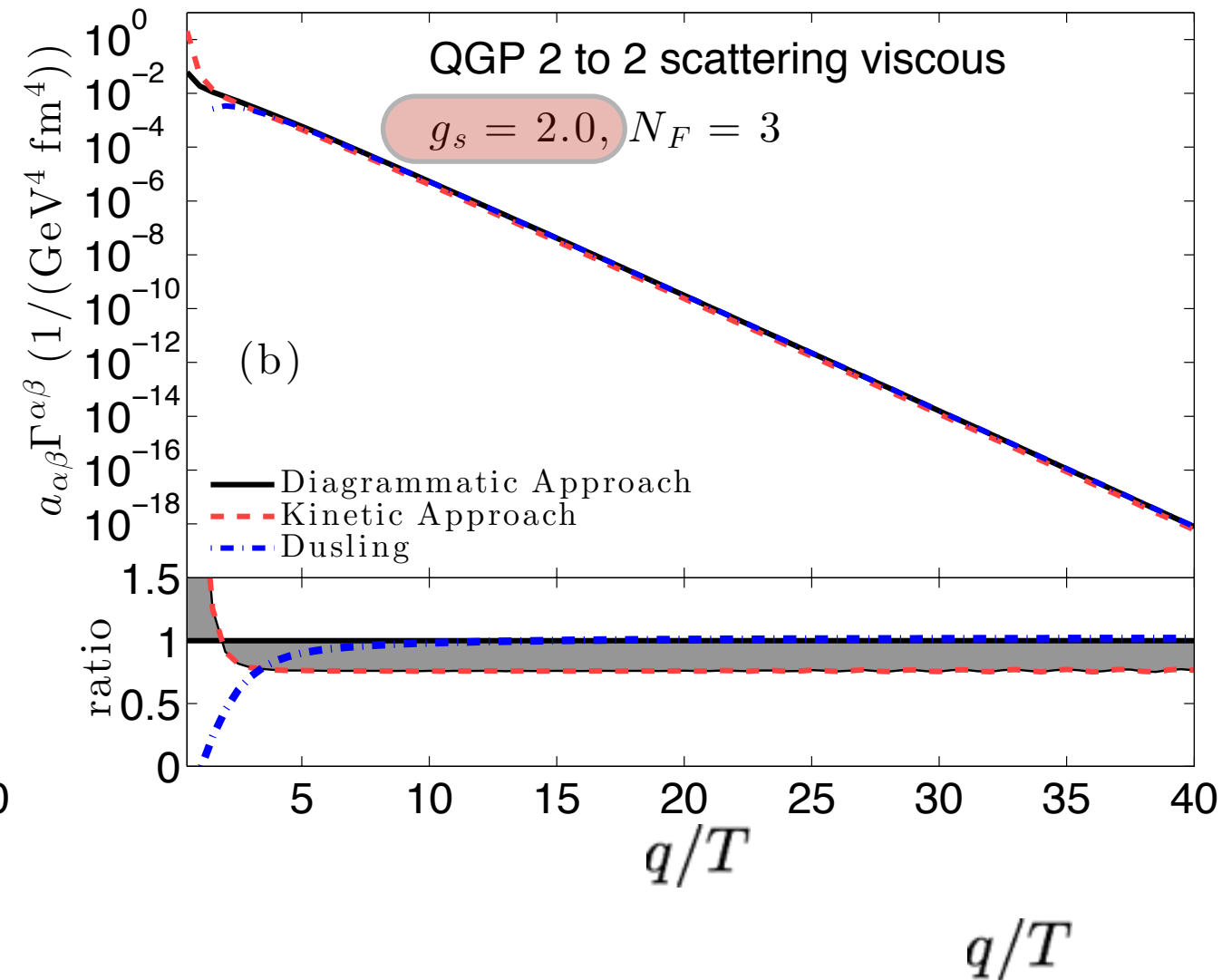
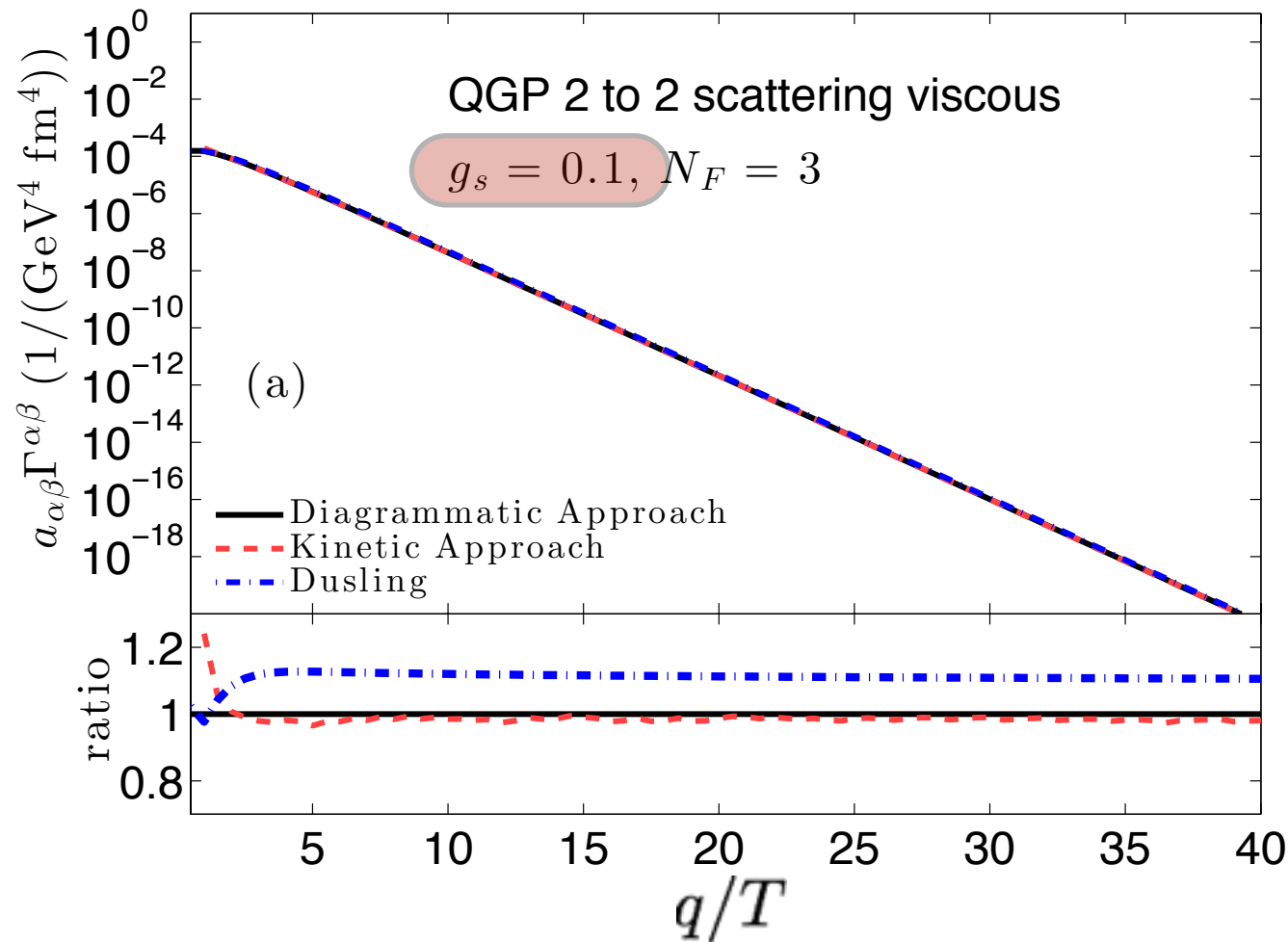
## Equilibrium rates:



- Diagrammatic approach requires matching soft and hard rates at  $gT < q^* < T$ ; kinetic approach doesn't (can use HTL matrix element everywhere).
- For small  $g$  find broad matching window of insensitivity; window disappears for large  $g$ . Match at  $q^*$  where sensitivity is minimal.
- Equivalence holds only at leading order in  $g$ ; for  $g=2$ , diagrammatic approach gives 25% larger yield than kinetic (irreducible systematic error at  $O(g)$ )

# Equivalence of kinetic and diagrammatic approaches:

## Viscous corrections:

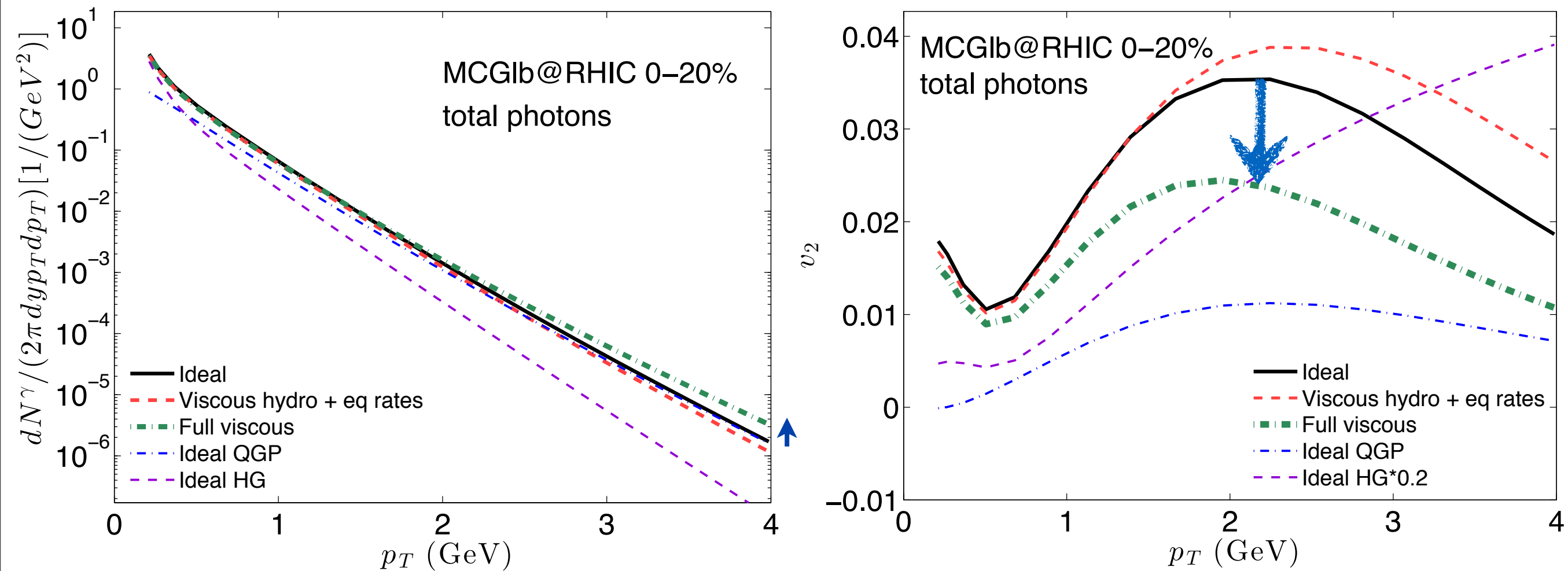


- Viscous effects in HTL matrix element (not included by Dusling) reduce viscous rate corrections by 15% ( $g=0.1$ ) to 25% ( $g=2$ ) over most of  $q$  range.
- For small  $g$  find broad matching window of insensitivity; window disappears for large  $g$ . Match at  $q^*$  where sensitivity is minimal.
- For  $g=2$ ,  $O(25\%)$  systematic uncertainty from different approaches.



# Results

# Example: Au+Au@200 AGeV w/ $\eta/s = 0.08$



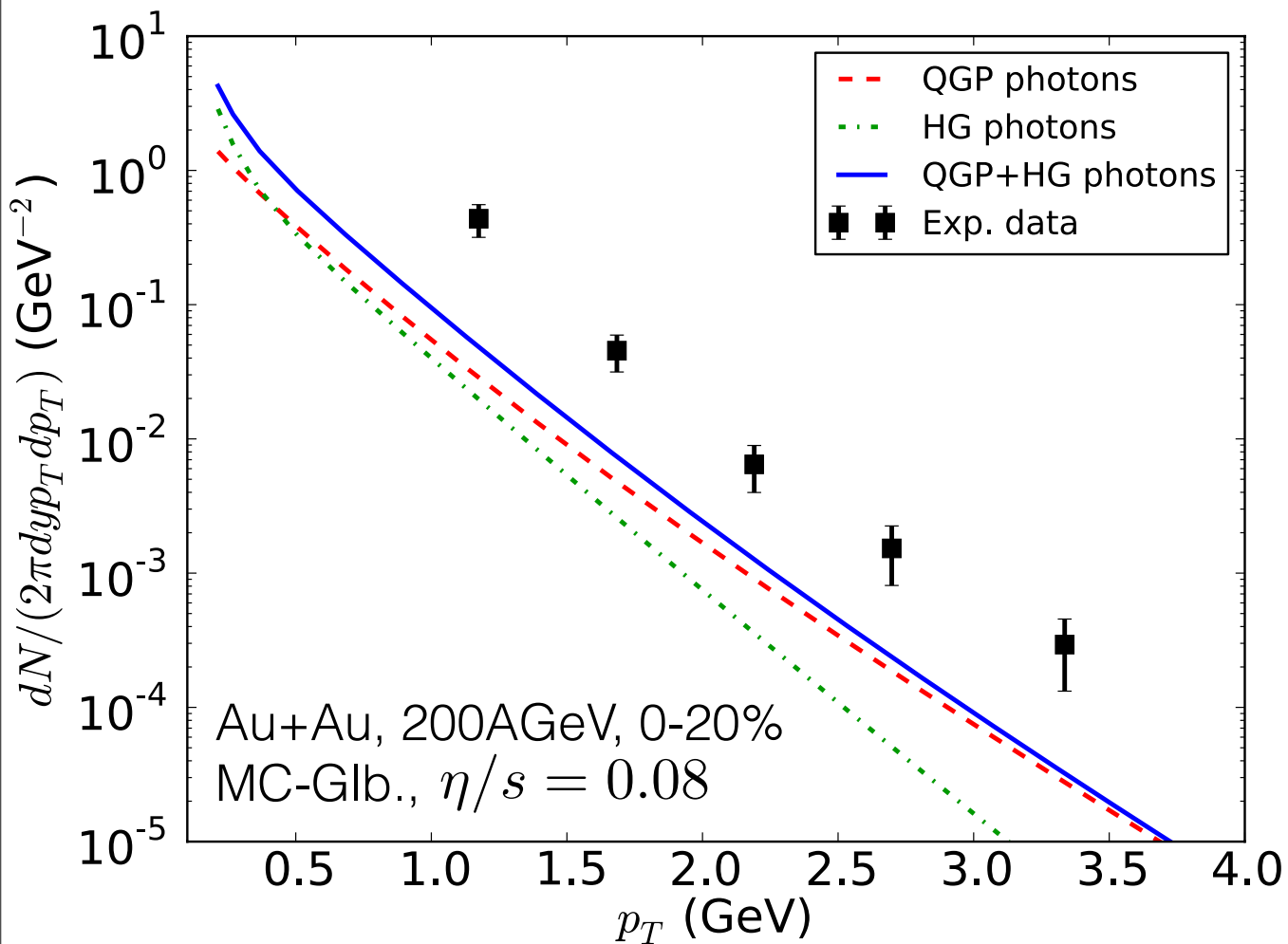
- Total photon spectrum dominated by QGP photons, except at very low  $p_T$ .
- Since QGP photons from early stage of hydrodynamic evolution carry small  $v_2$ , total photon  $v_2$  remains small compared to that of hadrons
- **Net effect of shear viscosity: even smaller photon  $v_2$  !**



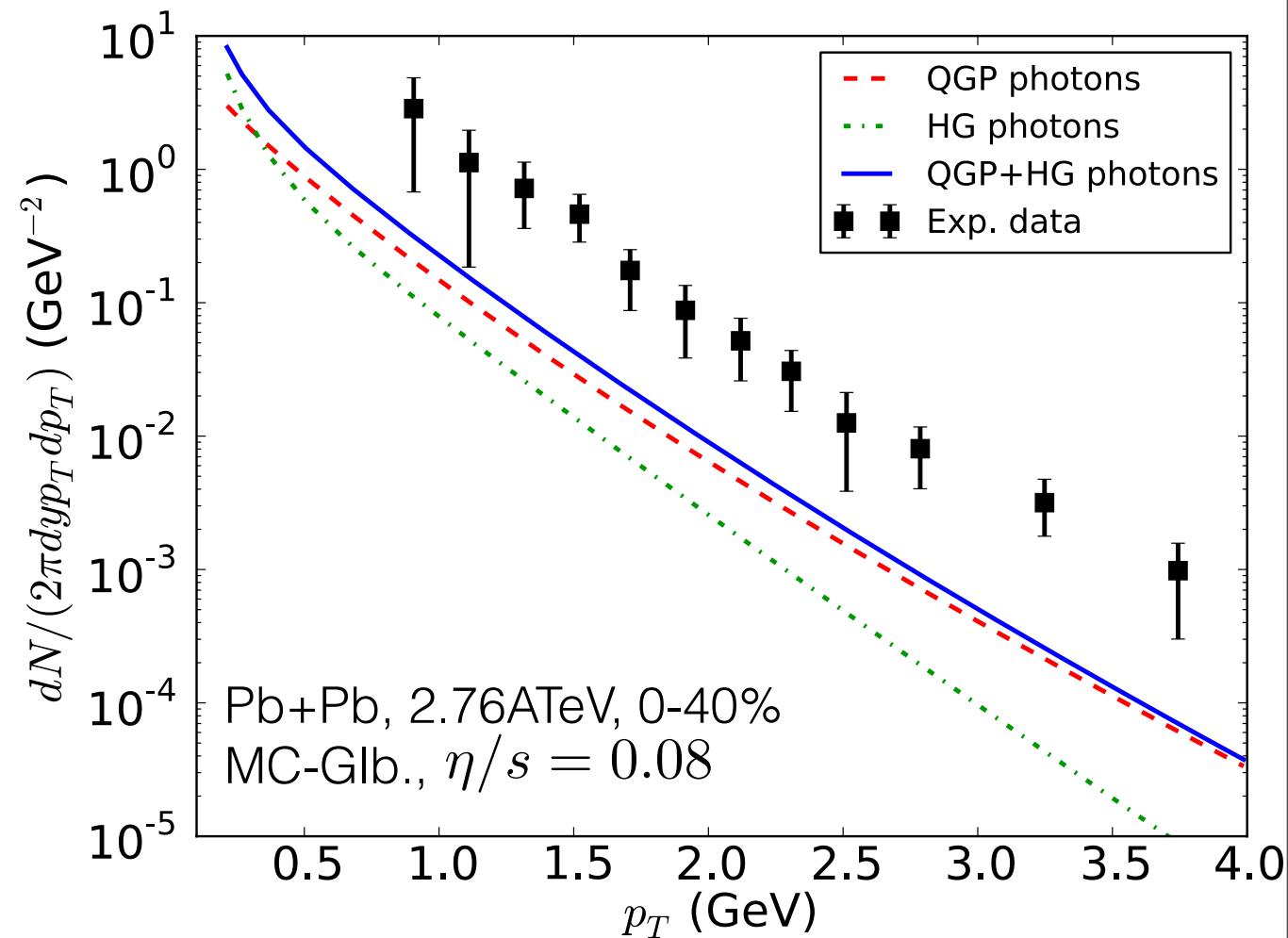
# Comparison with experiment

## I. photon spectra: problems remain

**RHIC (PHENIX)**



**LHC (Alice)**

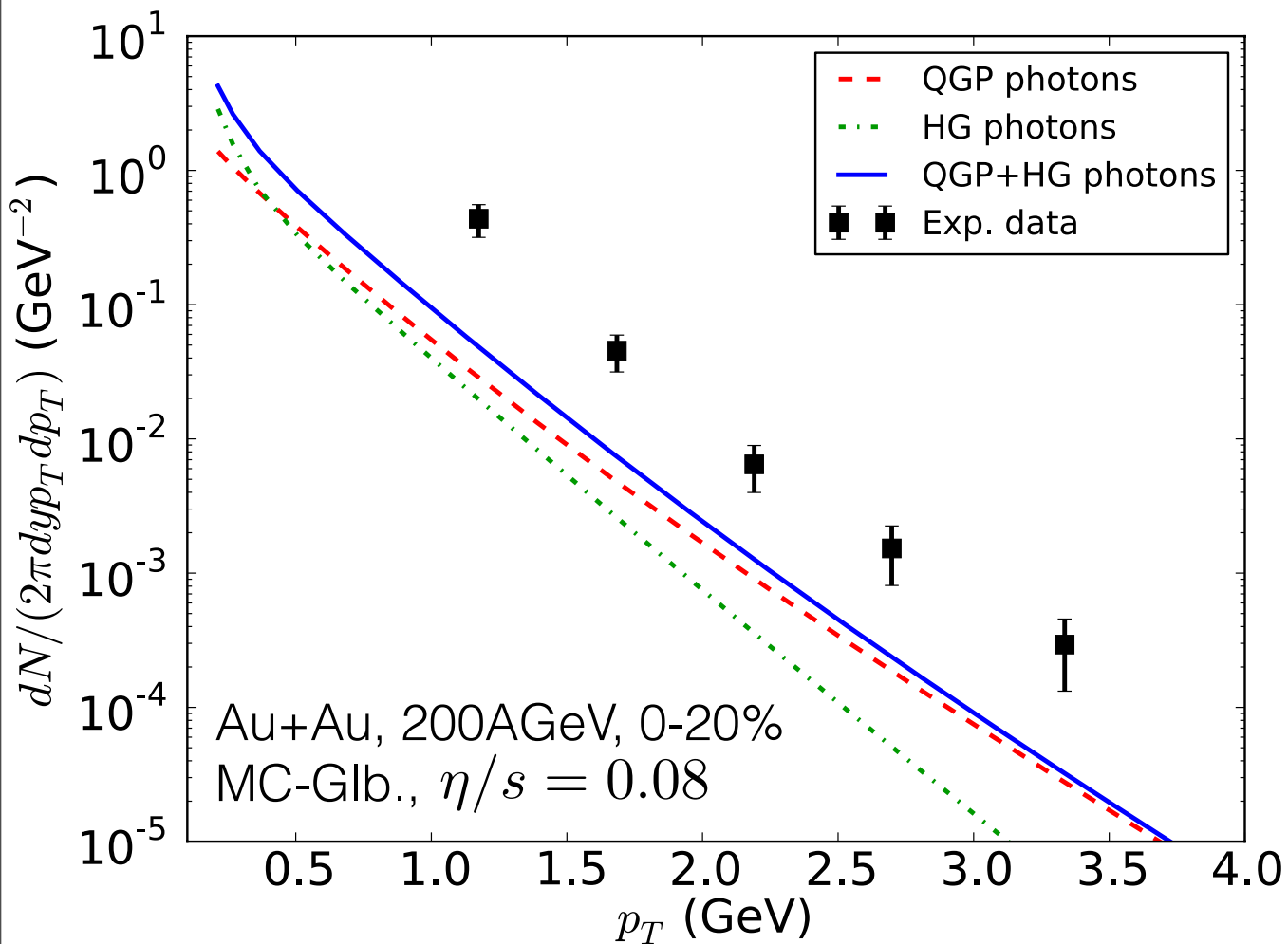


Thermal radiation too weak by factor 10 describe the data

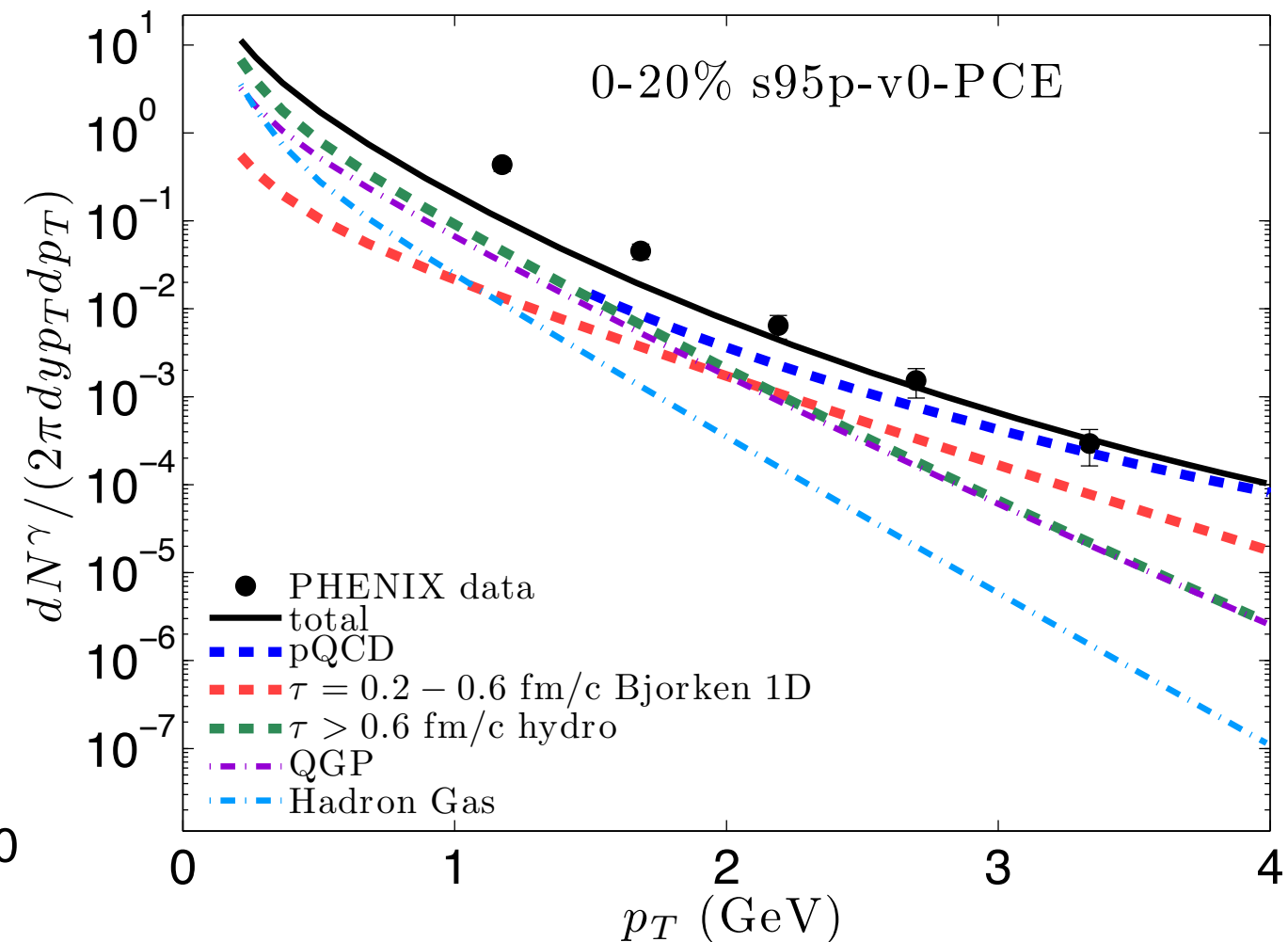
# Comparison with experiment

## I. photon spectra: problems remain

**thermal only**



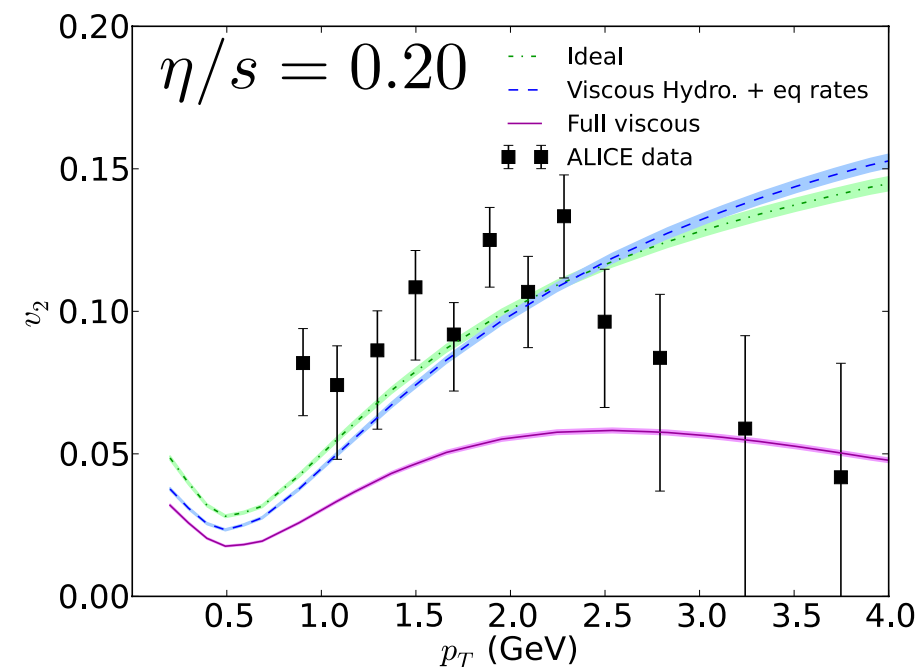
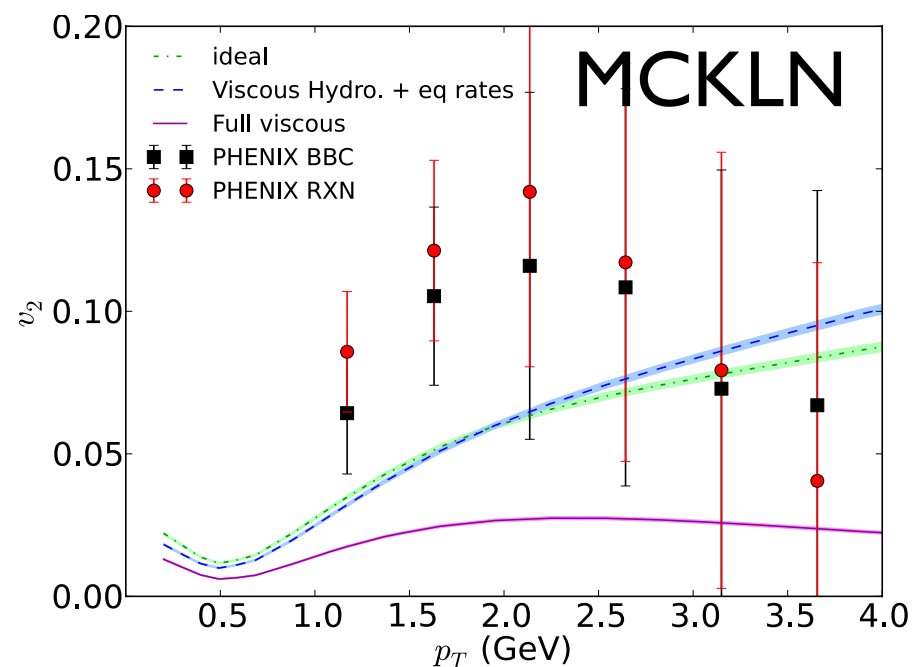
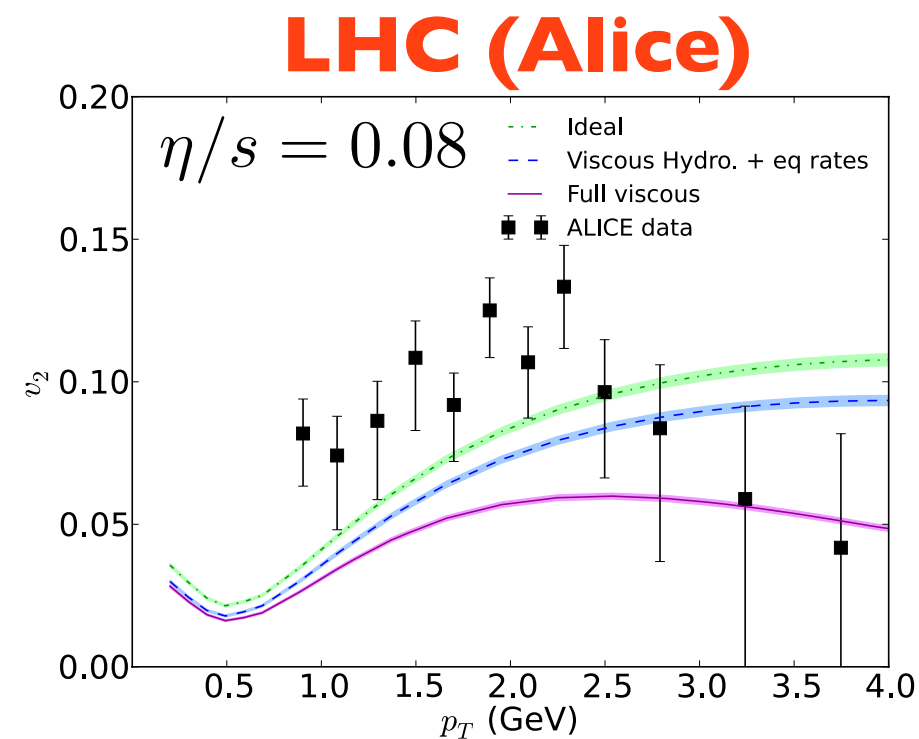
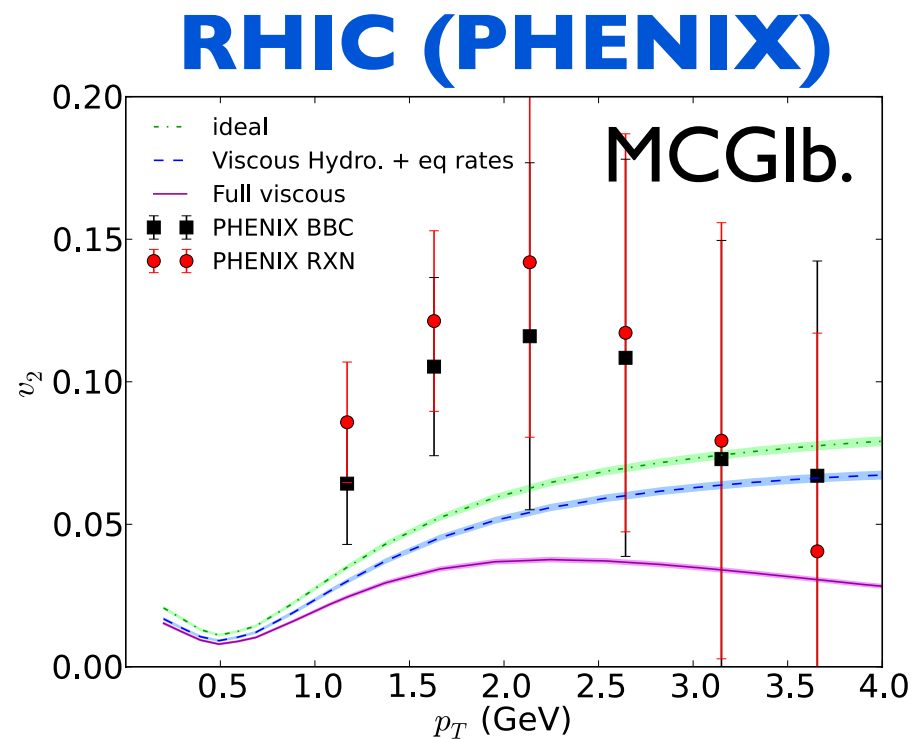
**adding prompt+pre-eq**



Still missing a large factor at  $p_T < 2 \text{ GeV}$   $\Rightarrow$  need additional late-stage photon emission

see also new PHENIX data (Banner Tue 13:30)

# Comparison with experiment: $v_2$ worse than before! (note: theory does not include prompt photons)

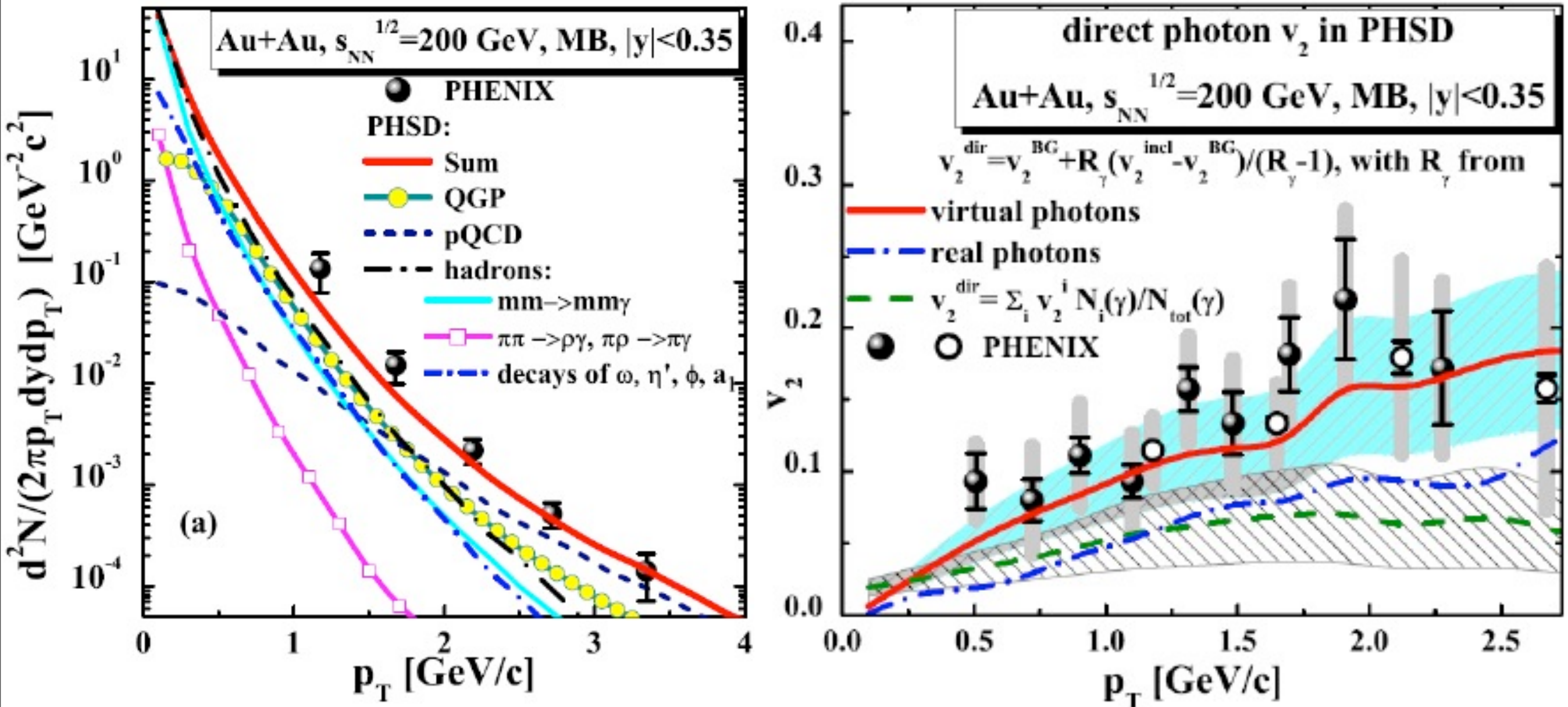


**Missing rate at late times where  $v_2$  is large!**



# Another approach: PHSD (Giessen)

O. Lynn timer et al., PRC88 (2013) 034904



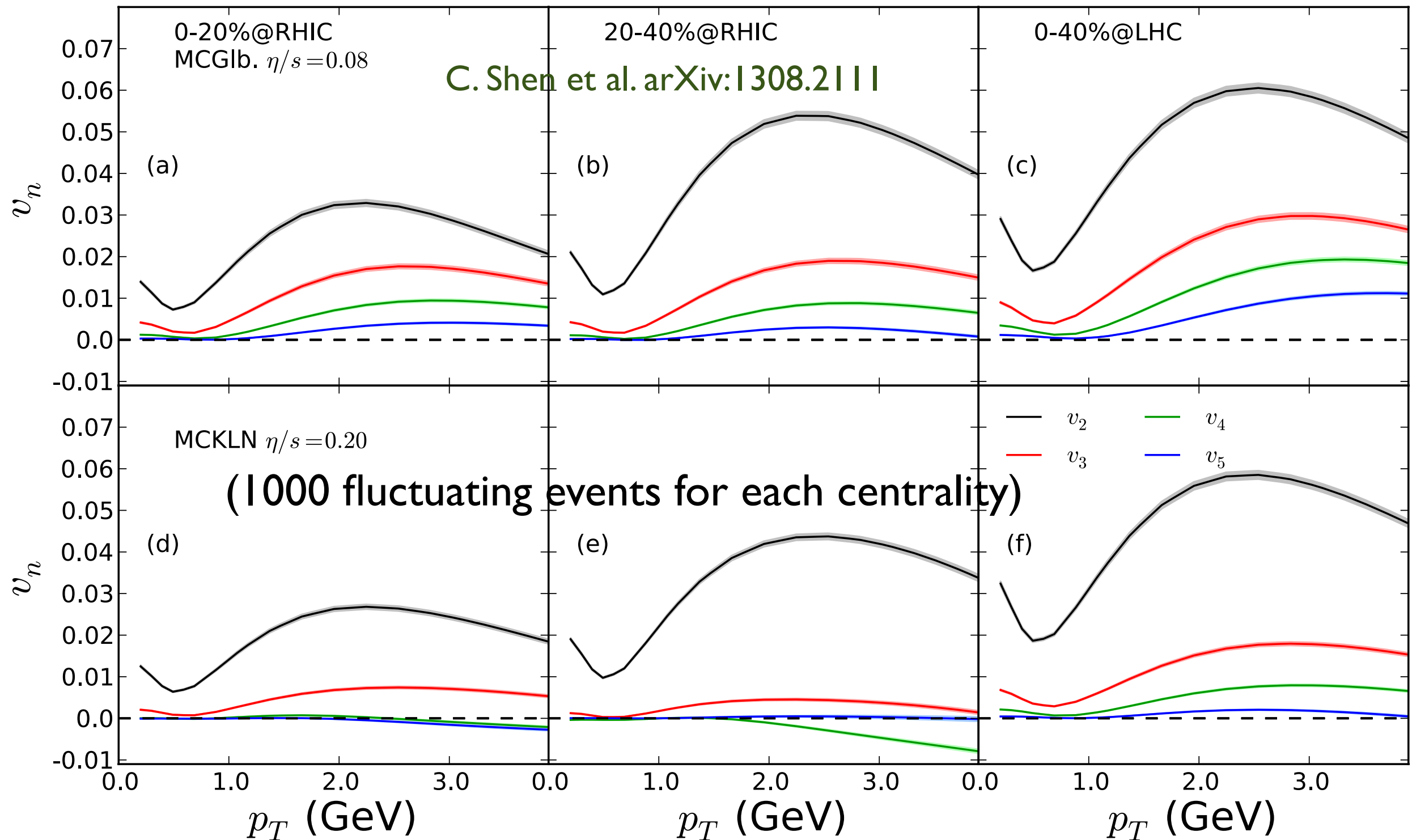
More hadronic radiation, steeper QGP and HG spectra at low  $p_T$  than in hydro

Still, not enough  $v_2$  for direct photons

W. Cassing Thu 15:40

**Finally, some good news:**

# Event-by-event full viscous photon $v_n$

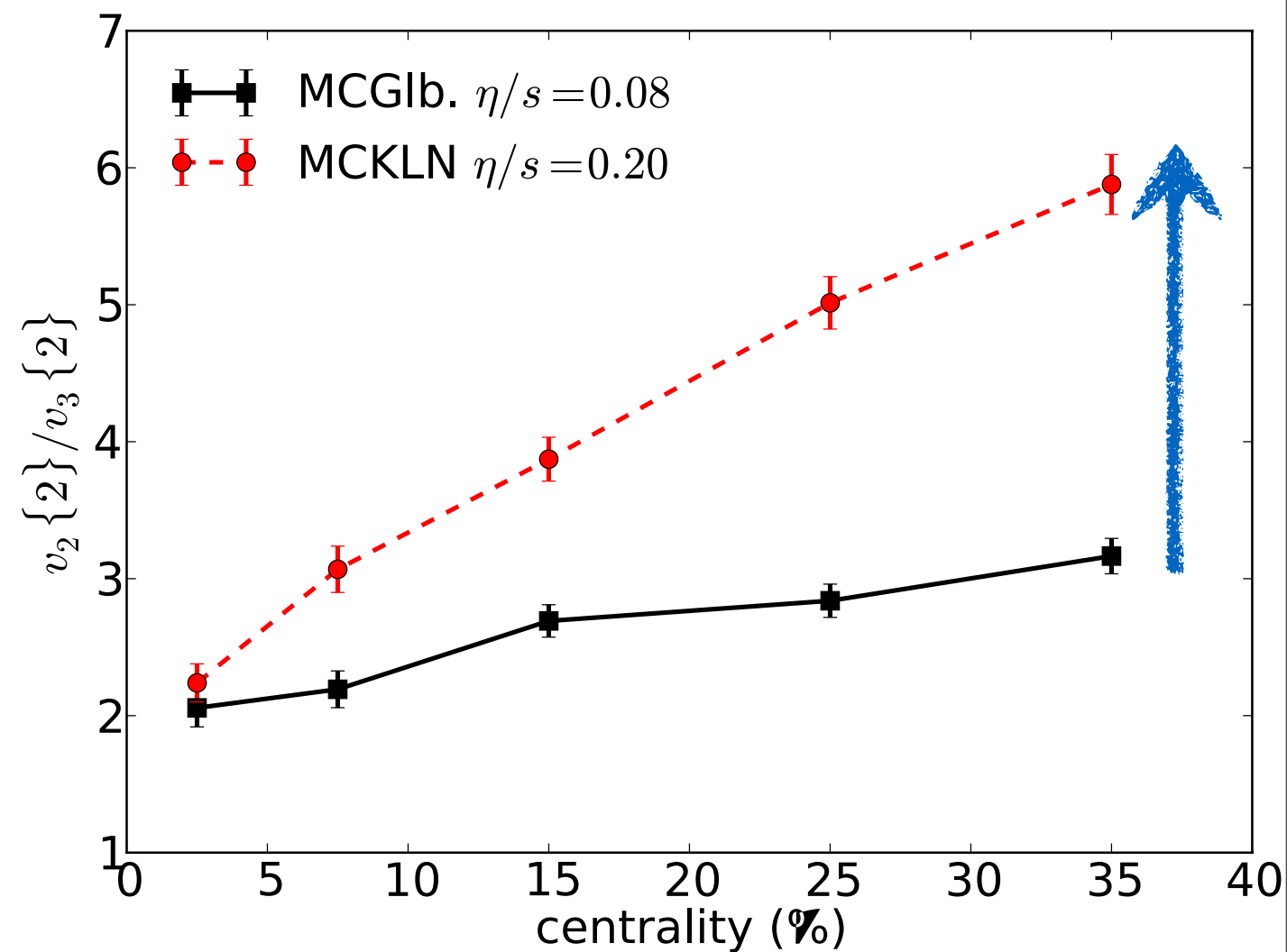
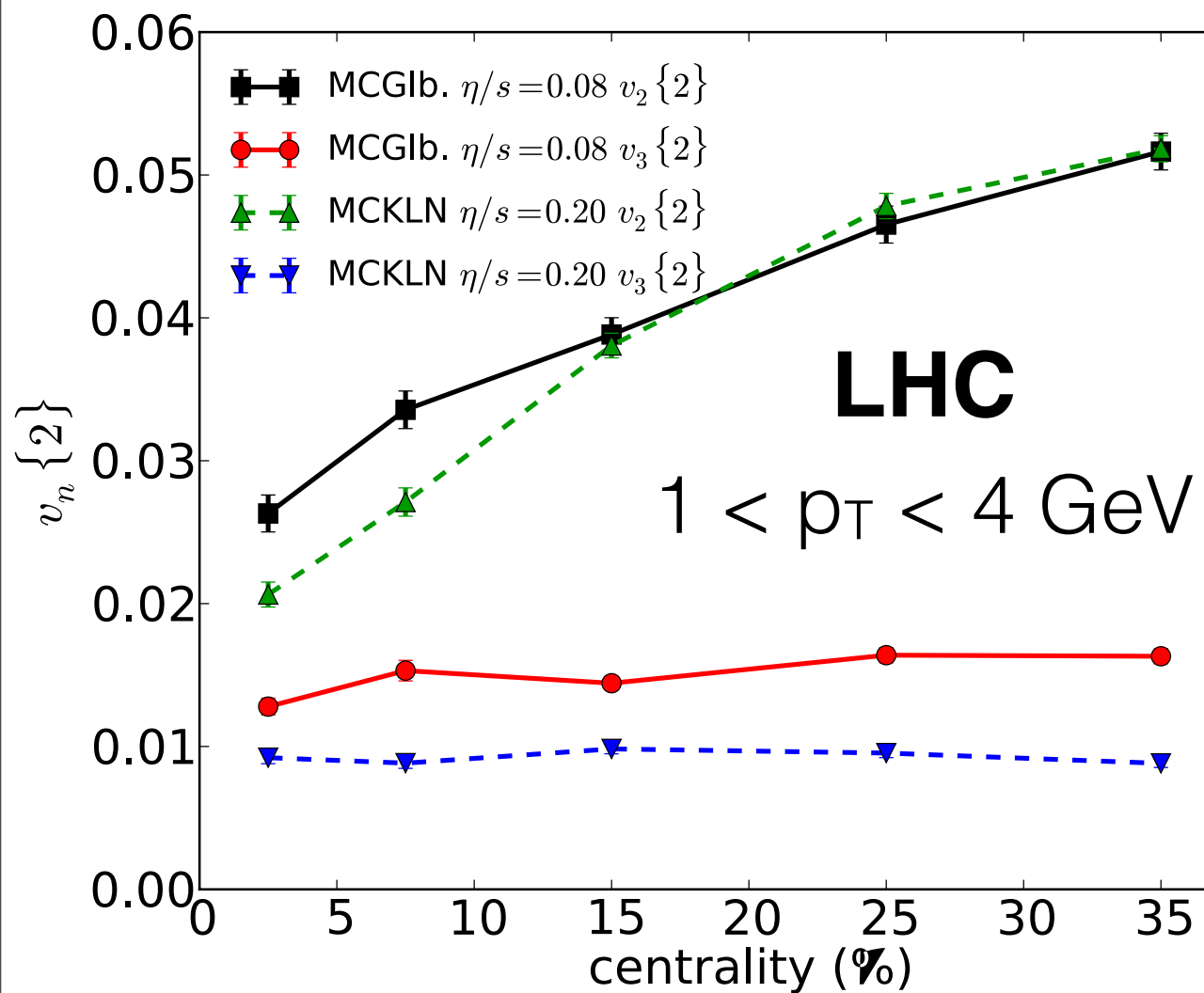


- E-by-e hydro allows to predict  $v_3, v_4, v_5, \dots$
- $v_3$  measurement can kill exotic production mechanisms for large  $v_2$
- Size of photon  $v_3/v_2$  can constrain shear viscosity at early times

Shen Mo17:20

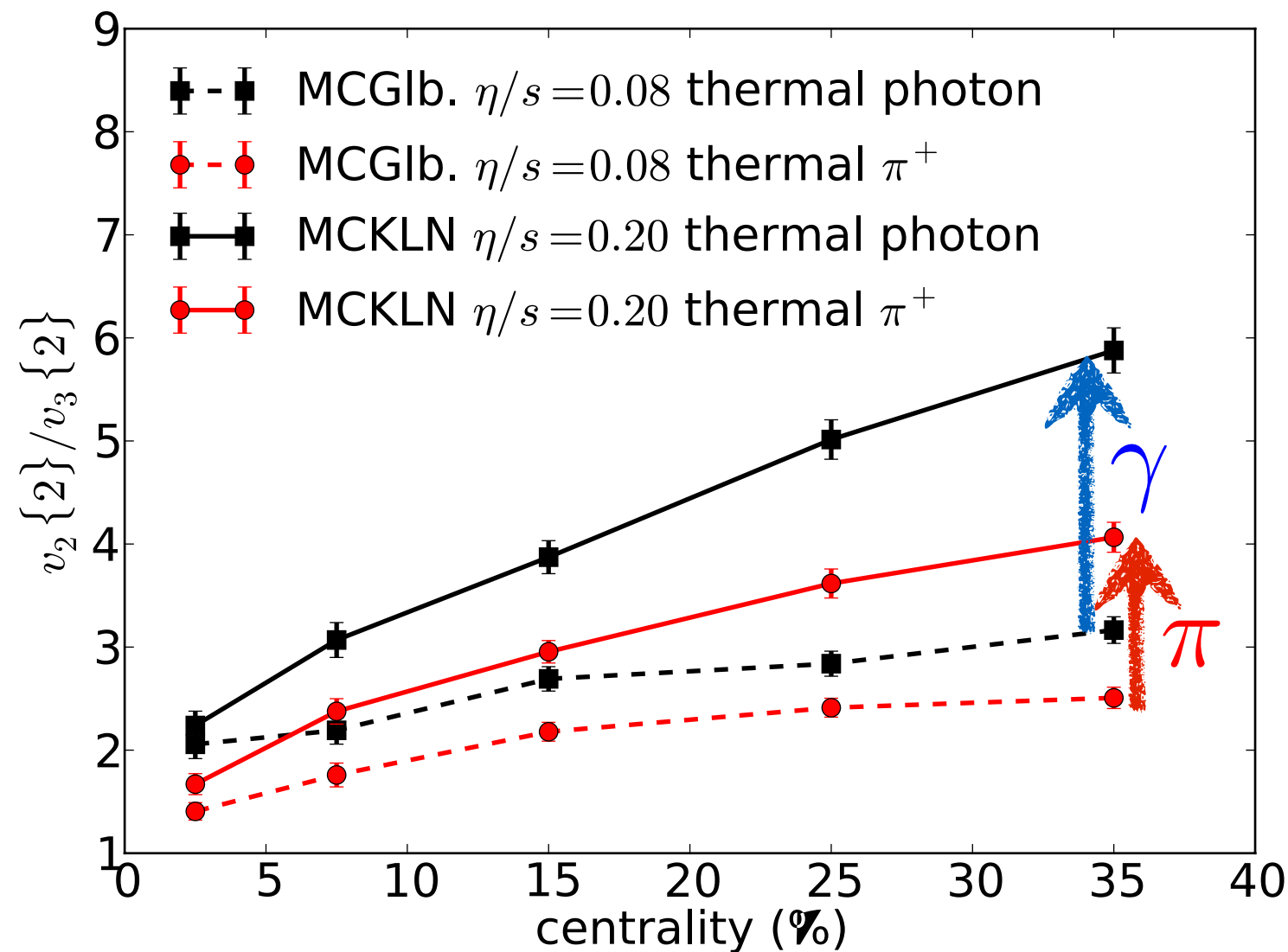


# Event-by-event full viscous photon $v_n$



- Anisotropic photon flows show qualitatively similar centrality dependence as hadron flows
- The ratio  $v_2/v_3$ , and its slope as a function of centrality, increase with shear viscosity.

# Event-by-event full viscous photon $v_n$



C. Shen

- Anisotropic photon flows show qualitatively similar centrality dependence as hadron flows
- The ratio of  $v_2/v_3$ , and its slope as a function of centrality, increase with shear viscosity.
- The centrality dependence of this ratio is stronger for photons than for hadrons, **due to stronger viscous effects at early times!**

# Conclusions

- The large measured photon  $v_2$  continues to be a challenge for theory
- Hydrodynamic models produce too much radiation at early times and too little at late times to reproduce measured photon spectra and  $v_2$  at low  $p_T$  -- are our emission rates wrong?
- Photons are more susceptible to shear viscosity than hadrons, and shear viscosity further reduces  $v_2$
- Can use centrality dependence of photon vs. hadron  $v_2/v_3$  ratio to constrain shear viscosity at early times



**Thanks to:**

Chun Shen,  
Jean-Francois Paquet,  
Evan Frodermann,  
Zhi Qiu,  
Rupa Chatterjee,  
Dinesh Srivastava  
Charles Gale

# Back up

