

# Spatially dependent nPDFs and their applications in inclusive pion and prompt photon production Hard Probes

Ilkka Helenius

In collaboration with  
Hannu Paukkunen and Kari J. Eskola

University of Jyväskylä  
Department of Physics

Nov 7 2013

# Outline

## 1 Introduction

- Nuclear PDFs
- Spatially dependent nPDFs

## 2 $\pi^0$ production in p+Pb

- $x_2$  sensitivity
- Centrality dependence

## 3 Prompt $\gamma$ production in p+Pb

- $x_2$  sensitivity
- Centrality dependence
- Isolated  $\gamma$

## 4 Summary & Conclusions

# Nuclear Parton Distribution Functions (nPDFs)

## Collinear Factorization framework

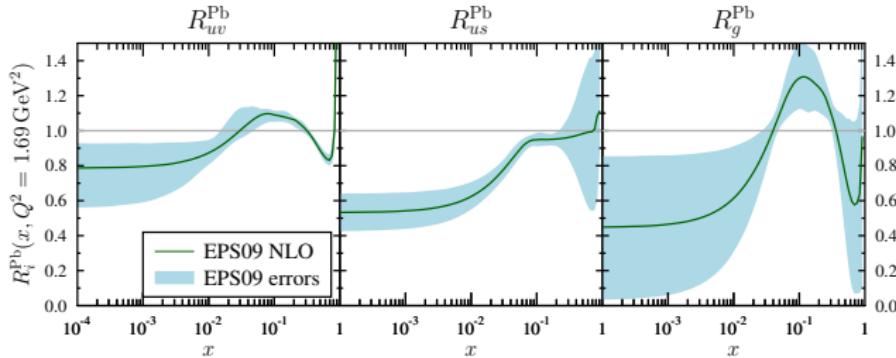
$$d\sigma^{AB \rightarrow k+X} = \sum_{i,j,X'} f_i^A(x, Q^2) \otimes f_j^B(x, Q^2) \otimes d\hat{\sigma}^{ij \rightarrow k+X'} + \mathcal{O}(1/Q^2)$$

- PDFs modified in nuclear collisions  $\Rightarrow$  Nuclear PDFs (nPDFs)

$$f_i^A(x, Q^2) = R_i^A(x, Q^2) \cdot f_i^N(x, Q^2)$$

- Nuclear modifications  $R_i^A(x, Q^2)$  from global analysis
- Here we use EPS09 NLO nPDFs

[Eskola, Paukkunen, Salgado *JHEP* 04 (2009) 065]



- More constraints for gluon nPDF from p+Pb collisions?

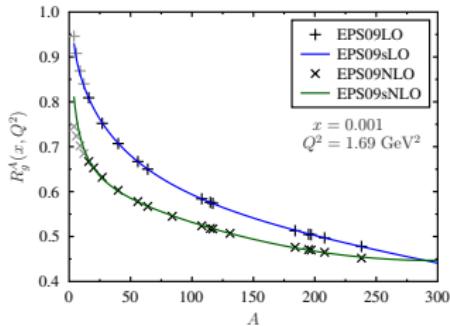
# Spatially dependent nPDFs

We have also published spatially dependent nPDF sets, e.g. **EPS09s**  
[I.H. Eskola, Honkanen, Salgado *JHEP* 07 (2012) 073]

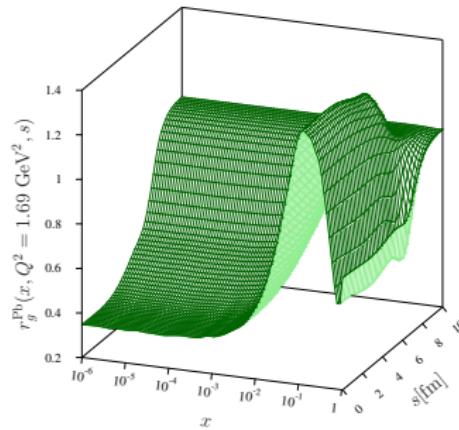
- ① Assume a power series from for  $r_i^A(x, Q^2, s)$ :

$$r_i^A(x, Q^2, s) = 1 + \sum_{j=1}^4 c_j^i(x, Q^2) [T_A(s)]^j$$

- ② Use  $A$  dependence of EPS09 to get values for  $c_j^i(x, Q^2)$



- ④ **Outcome:** Spatially dependent nPDFs



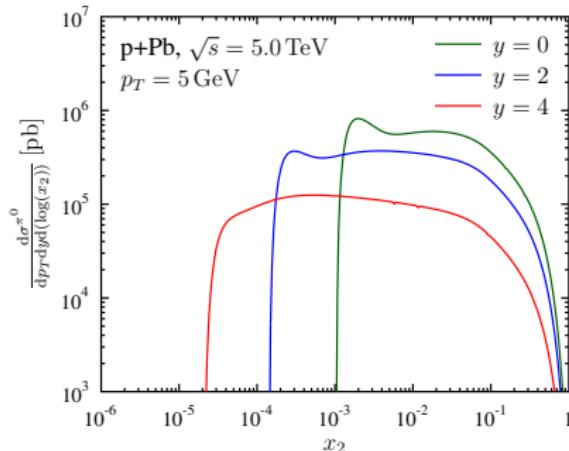
- ③ Repeat the fitting for each parton flavor

## Hadron production

- Involves convolution with fragmentation functions (FFs):

$$d\sigma_{pPb}^{\pi^0} = \sum_k d\sigma_{pPb}^k \otimes D_k^{\pi^0}(z, Q_F^2),$$

$\Rightarrow$  Contribution to  $d\sigma_{pPb}^{\pi^0}$  from broad  $x_2$  range in NLO



- Even at  $y = 4$   $d\sigma_{pPb}^{\pi^0}$  is not sensitive only to small  $x_2$ !

# Nuclear modification factor

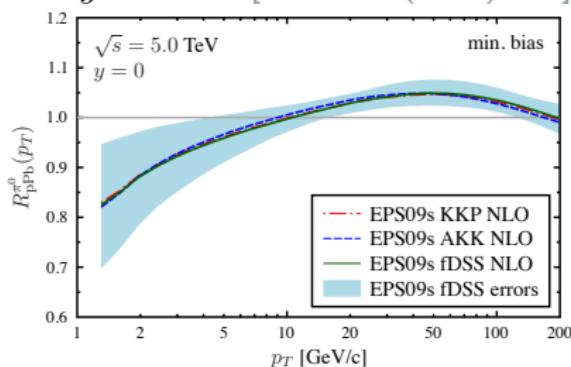
$R_{\text{pPb}}$  quantifies the nuclear modification

$$R_{\text{pPb,MB}}^{\pi^0}(p_T, y) = \frac{1}{A} \frac{d^2\sigma_{\text{pPb,MB}}^{\pi^0}}{dp_T dy} \Big/ \frac{d^2\sigma_{\text{pp}}^{\pi^0}}{dp_T dy},$$

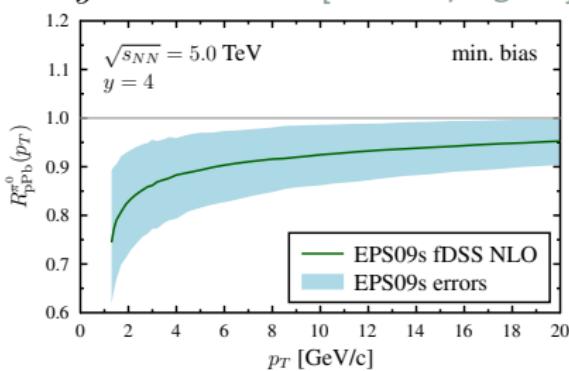
where MB = Average over all centralities

- $R_{\text{pPb}}$  for inclusive  $\pi^0$  at  $\sqrt{s_{NN}} = 5.0 \text{ TeV}$  in NLO (with INCNLO)

$y = 0$ : [JHEP 07 (2012) 073]



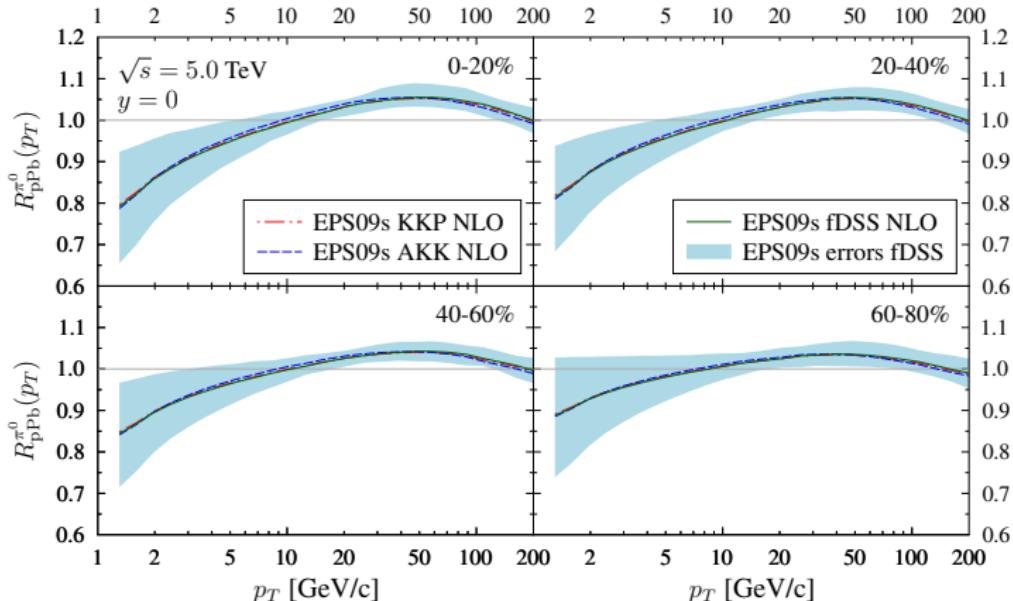
$y = 4$ : [work in progress]



- At  $y = 0$  Suppression due to shadowing at  $p_T < 10 \text{ GeV}$
- At  $y = 4$  suppression also for higher  $p_T$

# Centrality dependence of $\pi^0$ production at $y = 0$

- $R_{\text{pPb}}$  for inclusive  $\pi^0$  at  $\sqrt{s_{\text{NN}}} = 5.0 \text{ TeV}$  and  $y = 0$  in four centrality classes in NLO (with INCNLO) [JHEP 1207 (2012) 073]



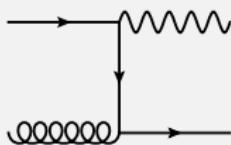
- Centrality classes determined using Optical Glauber model
- Stronger nuclear effects in central collisions

# Prompt $\gamma$ production in pQCD

- Prompt photons consists of two components:

## Direct photon production

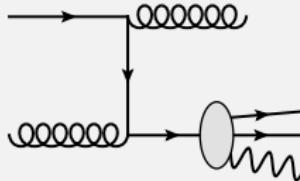
e.g. Compton scattering



- Calculated from pQCD
- Provides a direct probe to the gluon PDFs

## Fragmentation photon production

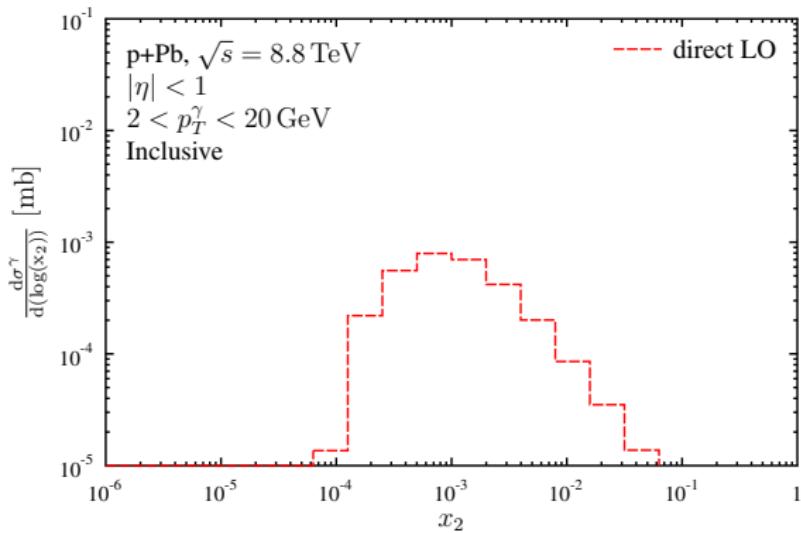
parton fragments into photon, e.g.



- Calculated by convoluting the hard parton spectra with FFs (BFG II)  
⇒ Smears the  $x_2$  distribution

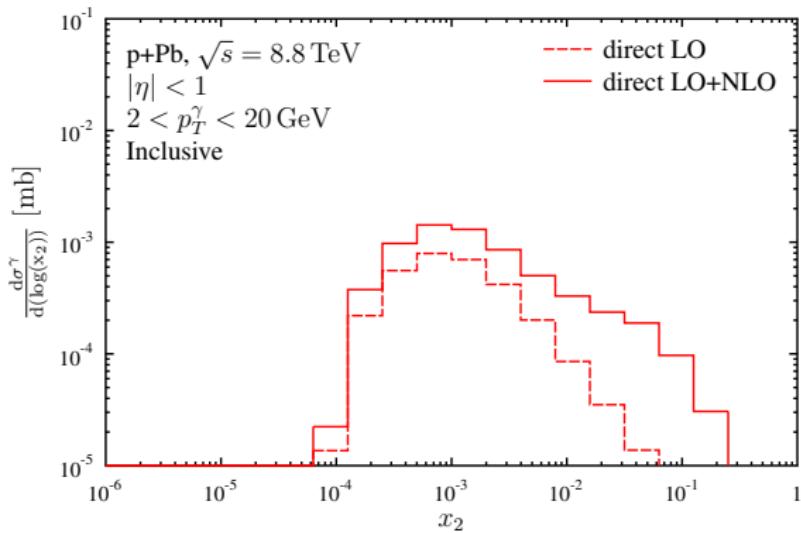
- Two components experimentally indistinguishable
- In NLO the division depends on scale choice  
⇒ Only the sum of these two is a meaningful observable

- The NLO cross section of inclusive prompt  $\gamma$  for p+Pb collisions, calculated using JETPHOX 1.3.1\_1 ( $\mu = p_T$ )



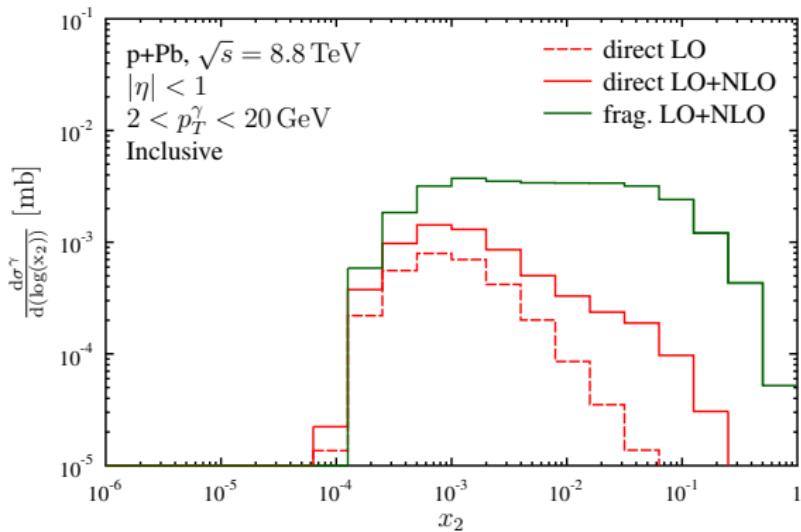
- Direct LO component peaked around  $x_2 = 7 \cdot 10^{-4} \approx \frac{2\langle p_T \rangle}{\sqrt{s_{NN}}} e^{-\eta}$

- The NLO cross section of inclusive prompt  $\gamma$  for p+Pb collisions, calculated using JETPHOX 1.3.1\_1 ( $\mu = p_T$ )



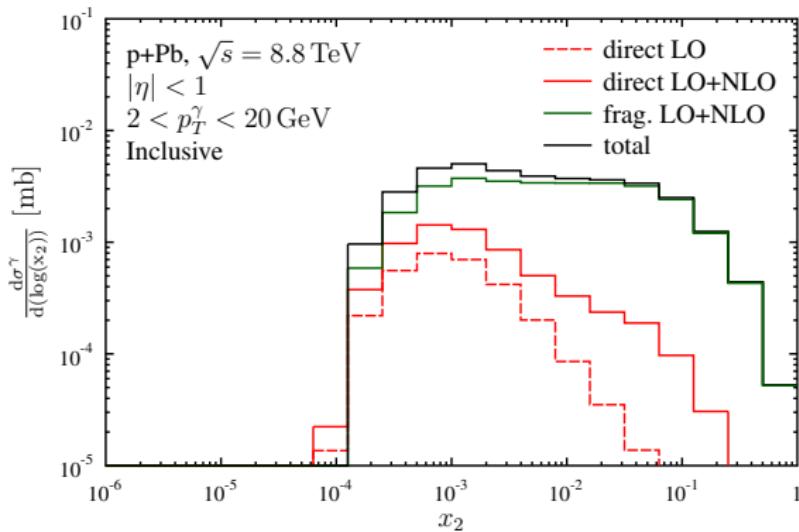
- Direct LO component peaked around  $x_2 = 7 \cdot 10^{-4} \approx \frac{2\langle p_T \rangle}{\sqrt{s_{NN}}} e^{-\eta}$
- Direct NLO component yields a tail to higher  $x_2$  values

- The NLO cross section of inclusive prompt  $\gamma$  for p+Pb collisions, calculated using JETPHOX 1.3.1\_1 ( $\mu = p_T$ )



- Direct LO component peaked around  $x_2 = 7 \cdot 10^{-4} \approx \frac{2\langle p_T \rangle}{\sqrt{s_{NN}}} e^{-\eta}$
- Direct NLO component yields a tail to higher  $x_2$  values
- Fragmentation component dominant, sensitive to broad  $x_2$  range

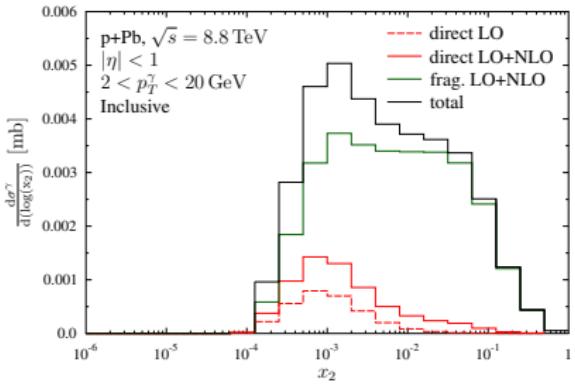
- The NLO cross section of inclusive prompt  $\gamma$  for p+Pb collisions, calculated using JETPHOX 1.3.1\_1 ( $\mu = p_T$ )



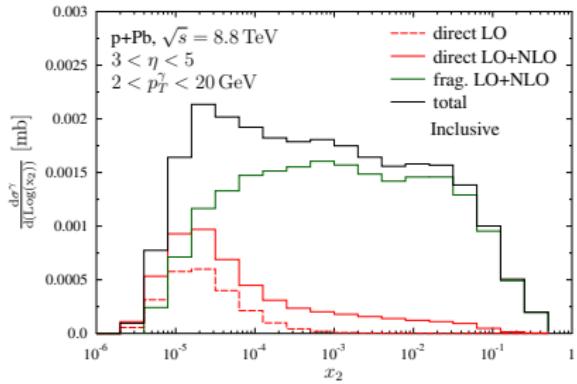
- Direct LO component peaked around  $x_2 = 7 \cdot 10^{-4} \approx \frac{2\langle p_T \rangle}{\sqrt{s_{NN}}} e^{-\eta}$
- Direct NLO component yields a tail to higher  $x_2$  values
- Fragmentation component dominant, sensitive to broad  $x_2$  range

- The NLO cross section of inclusive prompt  $\gamma$  for p+Pb collisions, calculated using JETPHOX 1.3.1\_1 ( $\mu = p_T$ )

Mid-rapidity:



Forward rapidity:

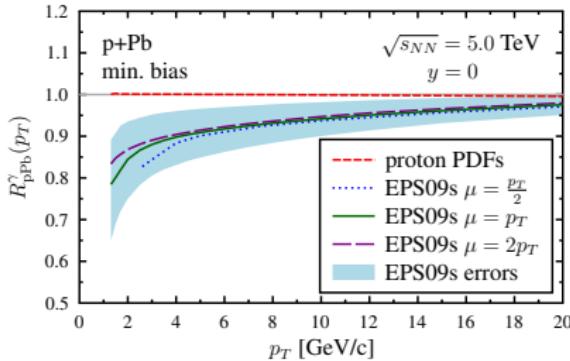


- In forward rapidities contribution from smaller  $x_2$  values
- The fragmentation component dominant also at large  $\eta$   
⇒ Not very sensitive to small  $x_2$

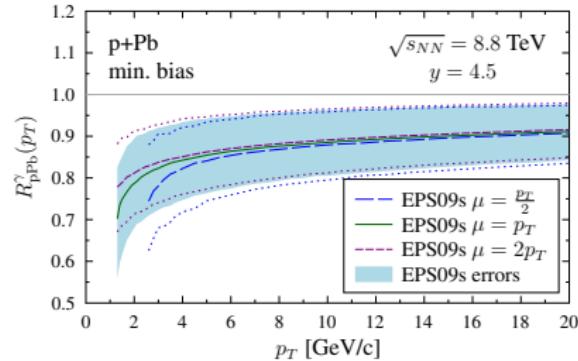
# $R_{\text{pPb}}$ for inclusive prompt $\gamma$

- $R_{\text{pPb}}$  for inclusive prompt  $\gamma$  (with INCNLO) for min. bias collisions ( $y = \eta$  for  $\gamma$ )

$\sqrt{s_{NN}} = 5.0 \text{ TeV}$  and  $y = 0$   
[JHEP 1305 (2013) 030]



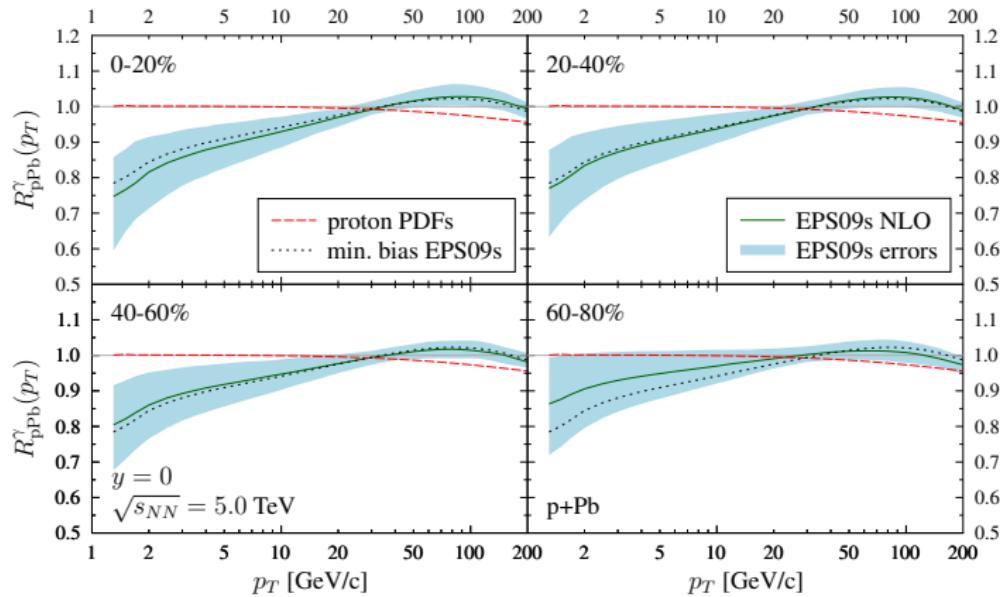
$\sqrt{s_{NN}} = 8.8 \text{ TeV}$  and  $y = 4.5$   
[Work in progress]



- Isospin effect negligible (red dashed line)
- Some scale dependence in  $p_T < 5 \text{ GeV}$
- At  $y = 0$  suppression below  $p_T \sim 20 \text{ GeV}$  due to shadowing
- Larger suppression at  $y = 4.5$

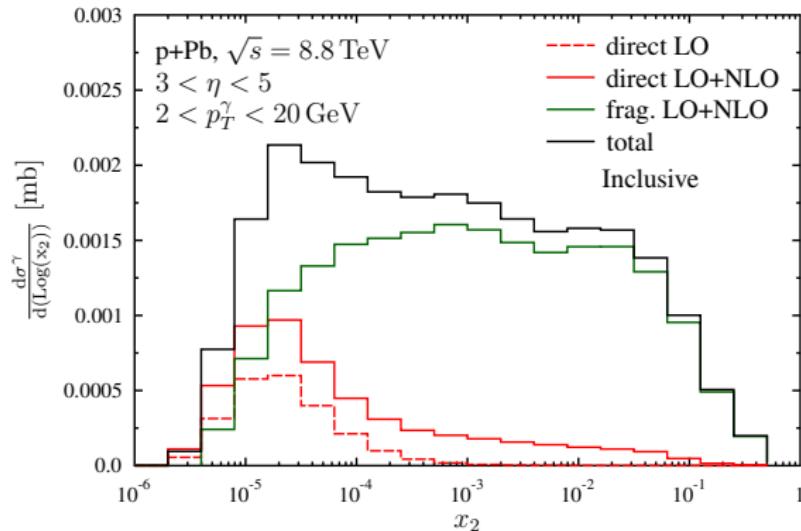
# Centrality dependent $R_{\text{pPb}}$ at $y = 0$

$R_{\text{pPb}}$  for inclusive prompt  $\gamma$  at  $\sqrt{s_{NN}} = 5.0 \text{ TeV}$  and  $y = 0$  in four centrality classes in NLO (with INCNLO) [JHEP 1305 (2013) 030]



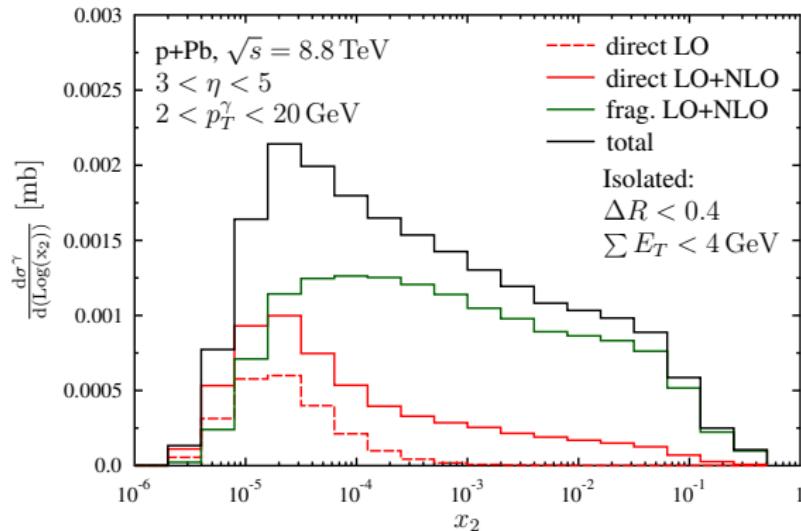
- Slightly more suppression than for  $\pi^0$   
⇒ Also the centrality dependence more visible

- The NLO cross section of prompt  $\gamma$  for p+Pb collisions, calculated using JETPHOX 1.3.1\_1 ( $\mu = p_T$ )



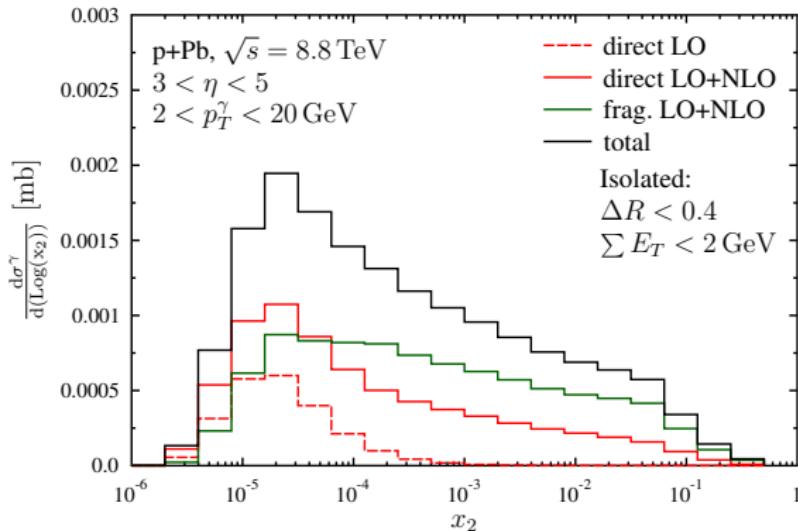
- Fragmentation component dominant for inclusive  $\gamma$

- The NLO cross section of prompt  $\gamma$  for p+Pb collisions, calculated using JETPHOX 1.3.1\_1 ( $\mu = p_T$ )



- Fragmentation component dominant for inclusive  $\gamma$
- Isolation suppress the fragmentation component at large  $x_2$

- The NLO cross section of prompt  $\gamma$  for p+Pb collisions, calculated using JETPHOX 1.3.1\_1 ( $\mu = p_T$ )



- Fragmentation component dominant for inclusive  $\gamma$
- Isolation suppress the fragmentation component at large  $x_2$
- Further suppression with tighter isolation cut  
⇒ Sensitive to small  $x_2$ !

## Summary

- p+Pb at the LHC collisions can be used
  - to constrain the nPDF uncertainties at small  $x_2$
  - to constrain the centrality dependence of the nPDFs
- We have calculated the  $R_{p\text{Pb}}$  at mid- and forward rapidities for
  - inclusive  $\pi^0$  production
  - prompt  $\gamma$  production
- Studied the  $x_2$  distributions for different observables
- Studied the centrality dependence of  $R_{p\text{Pb}}$  with EPS09s

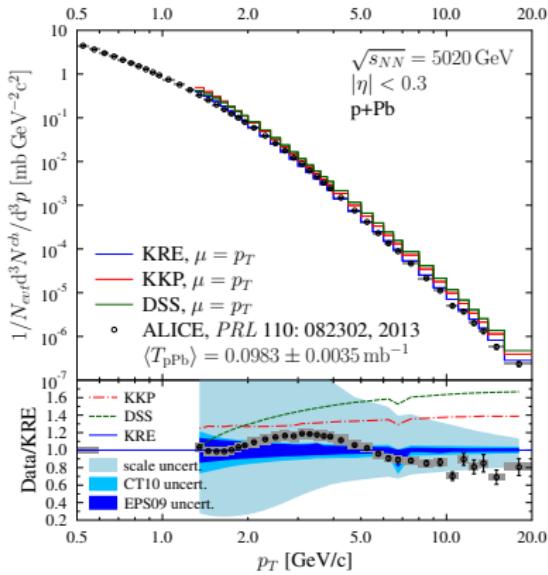
## Conclusions

- Convolution with FFs makes the  $x_2$  distribution wide
- Isolated  $\gamma$  at large  $\eta$  most sensitive to small  $x$  physics!
- Centrality dependence more prominent with large nuclear modifications (e.g. at small  $x$ )

## Backup

# p+Pb collisions at the LHC

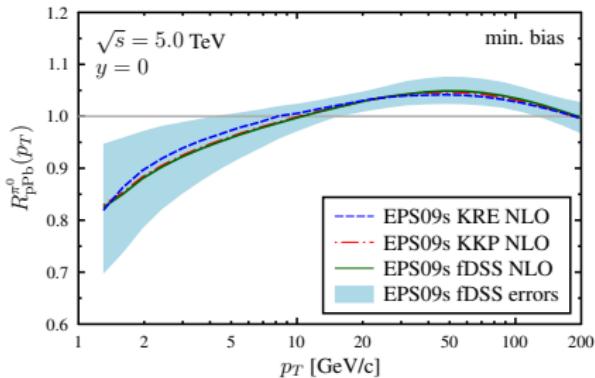
## Charged particle yield in p+Pb:



I.H., H.Paukkunen., D. d'Enterria

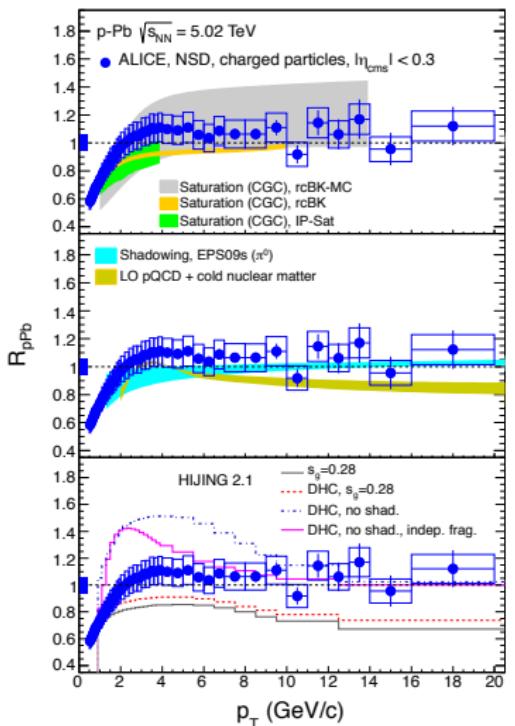
Work in progress

## Nuclear modification factor:



- Data best described with Kretzer fragmentation functions
- Differences in  $dN$  cancel out in ratio  $R_{\text{pPb}}$   
⇒  $R_{\text{pPb}}$  not sensitive to FFs

# p+Pb collisions at the LHC



## p+Pb pilot run in 2012

- ALICE measurement for charged particles
- Minimum bias result = averaged over all centralities

Our  $\pi^0$  prediction (*JHEP 07 (2012) 073*) consistent with the data

HIJING with scale independent strong gluon shadowing not supported by the data

Phys. Rev. Lett., 110: 082302, 2013

# Centrality dependent $R_{AB}$

## Nuclear Modification Factor

$$R_{AB}^k(b_1, b_2) = \frac{\left\langle \frac{d^2 N_{AB}^k}{dp_T dy} \right\rangle_{b_1, b_2}}{\langle N_{bin} \rangle_{b_1, b_2} \frac{d^2 \sigma_{pp}^k}{dp_T dy}} = \frac{\int_{b_1}^{b_2} d^2 \mathbf{b} \frac{d^2 N_{AB}^k(\mathbf{b})}{dp_T dy}}{\int_{b_1}^{b_2} d^2 \mathbf{b} T_{AB}(\mathbf{b}) \frac{d^2 \sigma_{pp}^k}{dp_T dy}}$$

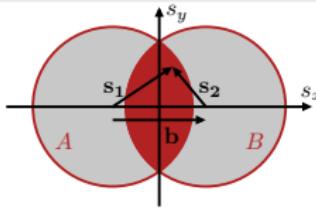
The yield depends on  $\mathbf{b}$  also via nPDFs:

$$\begin{aligned} dN^{AB \rightarrow k+X}(\mathbf{b}) &= \int d^2 \mathbf{s} T_A(\mathbf{s}_1) T_B(\mathbf{s}_2) \sum_{i,j,X'} r_i^A(x, Q^2, \mathbf{s}_1) f_i^N(x, Q^2) \\ &\quad \otimes r_j^B(x, Q^2, \mathbf{s}_2) f_j^N(x, Q^2) \otimes d\hat{\sigma}^{ij \rightarrow k+X'} \end{aligned}$$

where

$$\mathbf{s}_1 = \mathbf{s} + \mathbf{b}/2$$

$$\mathbf{s}_2 = \mathbf{s} - \mathbf{b}/2$$



# Centrality classes

## Optical Glauber Model

- Probability for inelastic collision

$$p_{inel}^{AB}(\mathbf{b}) \approx 1 - e^{-T_{AB}(\mathbf{b})\sigma_{inel}^{NN}}$$

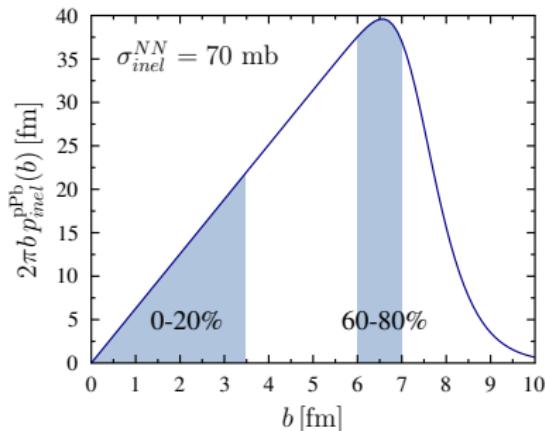
- Inelastic cross section for  $[b_1, b_2]$

$$\sigma_{inel}^{AB}(b_1, b_2) = \int_{b_1}^{b_2} d^2\mathbf{b} p_{inel}^{AB}(\mathbf{b})$$

- For p+A we assume a point-like proton  $\Rightarrow T_{pA}(\mathbf{b}) = T_A(\mathbf{b})$
- $T_A(\mathbf{s})$  from Woods-Saxon density:

$$\rho_A(\mathbf{s}, z) = \frac{n_0}{1 + \exp[\frac{\sqrt{s^2 + z^2} - R_A}{d}]}$$

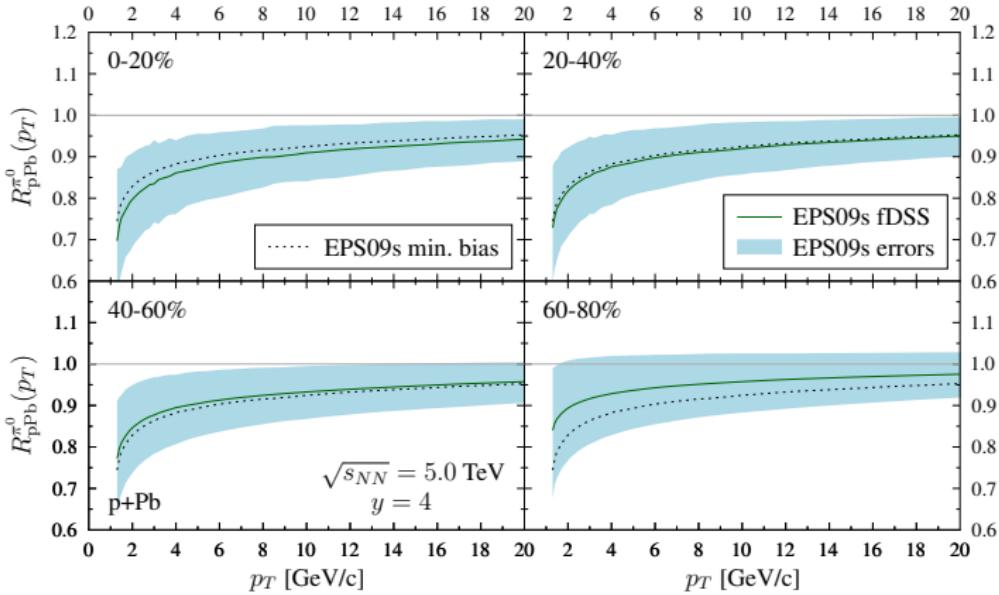
- Example: p+Pb at the LHC  
 $\sqrt{s_{NN}} = 5.0 \text{ TeV}, \sigma_{inel}^{NN} = 70 \text{ mb}$



	$b_1$ [fm]	$b_2$ [fm]	$\langle N_{bin} \rangle$
0-20%	0.0	3.471	14.24
20-40%	3.471	4.908	11.41
40-60%	4.908	6.012	7.663
60-80%	6.012	6.986	3.680

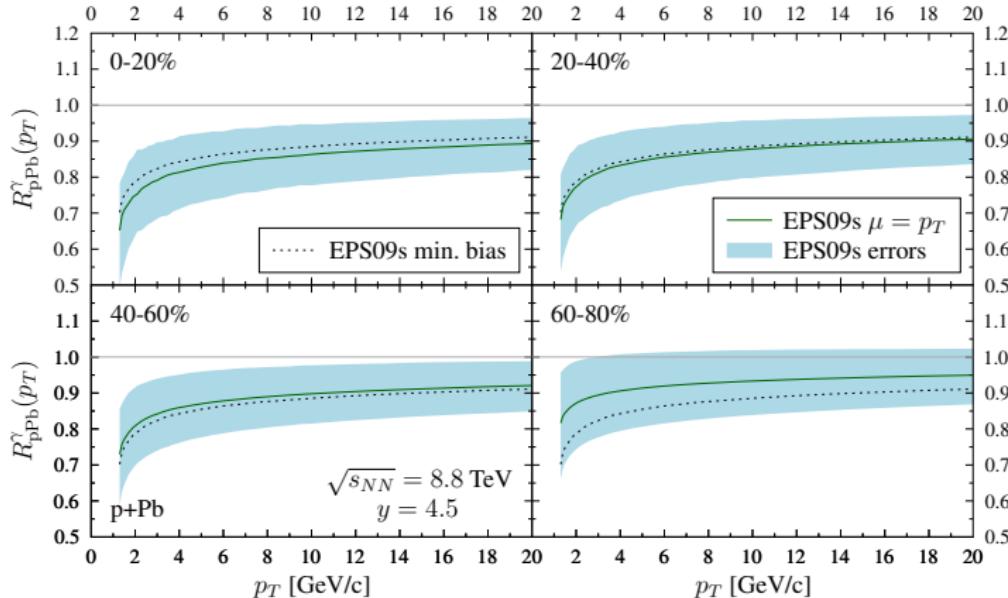
# Centrality dependence of $\pi^0$ production at $y = 4$

- $R_{\text{pPb}}$  for inclusive  $\pi^0$  at  $\sqrt{s_{NN}} = 5.0 \text{ TeV}$  and  $y = 4$  in four centrality classes in NLO (with INCNLO) [Work in progress]



# Centrality dependent $R_{\text{pPb}}$ at $y = 4.5$

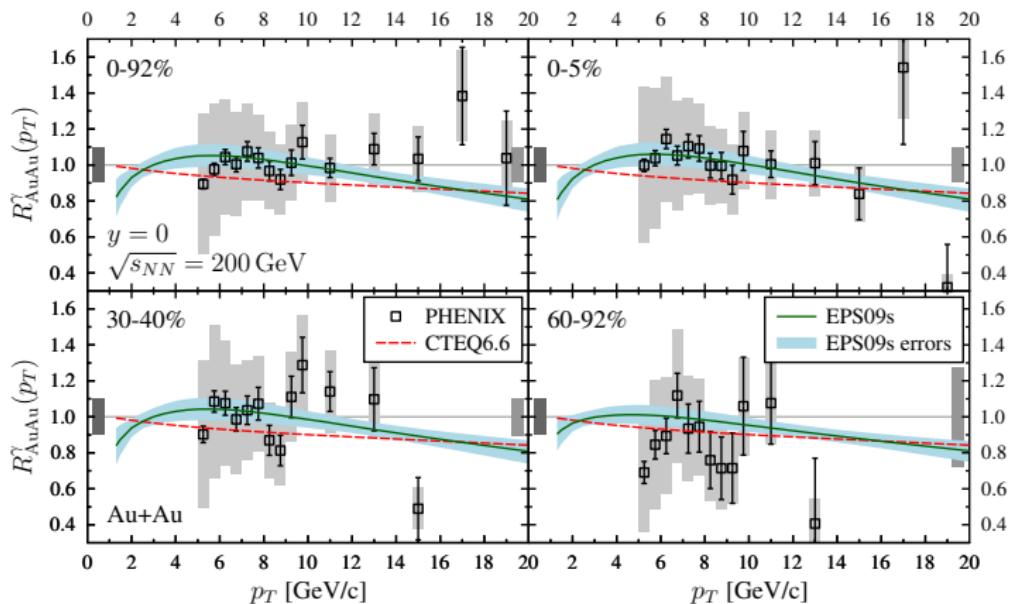
$R_{\text{pPb}}$  for prompt  $\gamma$  at  $\sqrt{s_{\text{NN}}} = 8.8 \text{ TeV}$  and  $y = 4.5$  in four centrality classes in NLO (with INCNLO) *Work in progress*



- Larger suppression than at  $y = 0$  for  $p_T < 20 \text{ GeV}$   
⇒ Centrality dependence more apparent

# Prompt $\gamma$ production in Au+Au at $y = 0$

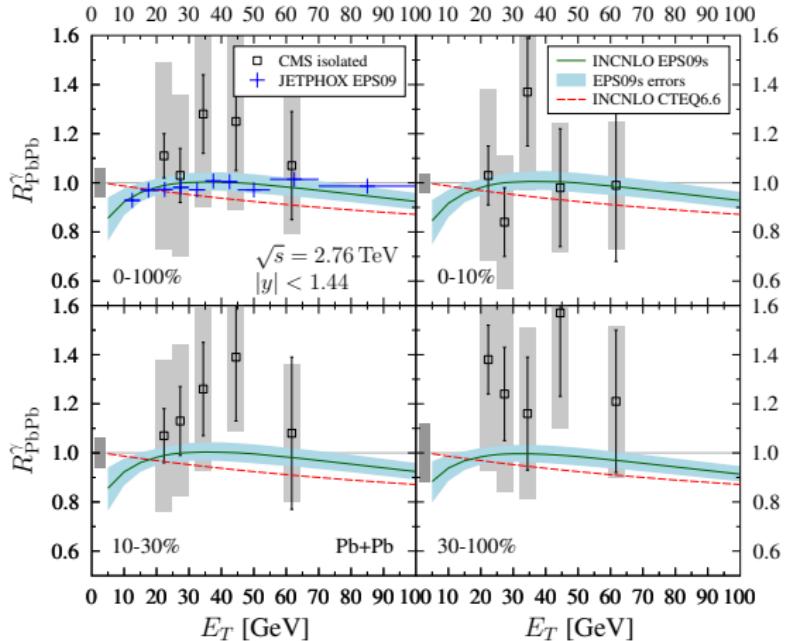
- $R_{\text{AuAu}}$  for prompt  $\gamma$  at  $\sqrt{s_{NN}} = 200 \text{ GeV}$  and  $y = 0$  in four centrality classes in NLO (with INCNLO) [JHEP 1305 (2013) 030]



- At  $p_T < 4 \text{ GeV}/c$  contribution from thermal photons also

# Prompt $\gamma$ production in Pb+Pb

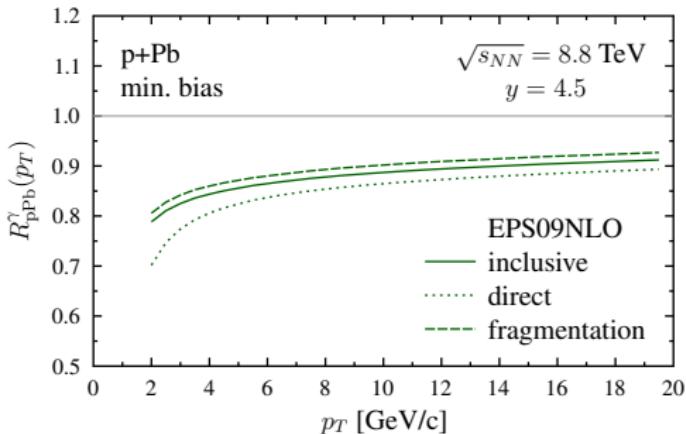
$R_{\text{PbPb}}$  for inclusive  $\gamma$  at  $\sqrt{s_{NN}} = 2.76 \text{ TeV}$  and  $|y| < 1.44$  in different centrality classes in NLO [JHEP 1305 (2013) 030]



- CMS data for isolated and calculation for inclusive photons
- Isolated (JETPHOX) and inclusive (INCNLO)  $R_{\text{PbPb}}^\gamma$  compatible in min. bias
  - ⇒ Comparison ok
- Note smaller nPDF uncertainties than in CMS paper [Phys.Lett. B710 (2012) 256-277]

# Isolated $R_{\text{pPb}}$ ?

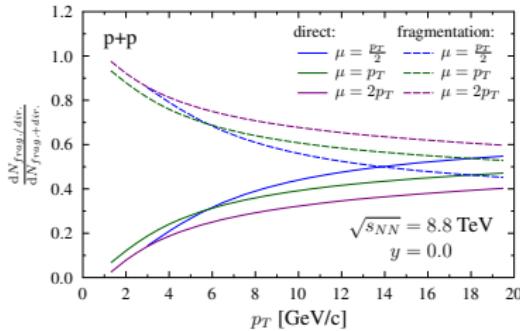
- $R_{\text{pPb}}$  for inclusive prompt  $\gamma$  at  $\sqrt{s_{NN}} = 8.8 \text{ TeV}$  and  $y = 4.5$  in NLO [I.H., K.J. Eskola, H. Paukkunen *work in progress*]



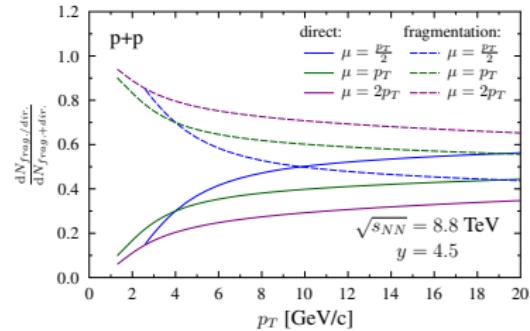
- Isolation increase the relative contribution from direct photons  
⇒ Isolated  $R_{\text{pPb}}$  closer to  $R_{\text{pPb}}$  with direct component only
- Work in progress...

# Direct vs. fragmentation photons

- The relative contribution from direct and fragmentation
- At mid-rapidity



- At forward rapidity



- In NLO the division scale dependent
- At low  $p_T$  the fragmentation photons dominate
- Similar behaviour in mid- and forward rapidities
- Calculated with BFGII FFs for photons and CT10 proton PDFs