

# Analog pygmy-dipole resonance and low-lying charge-exchange dipole state in neutron-rich nuclei

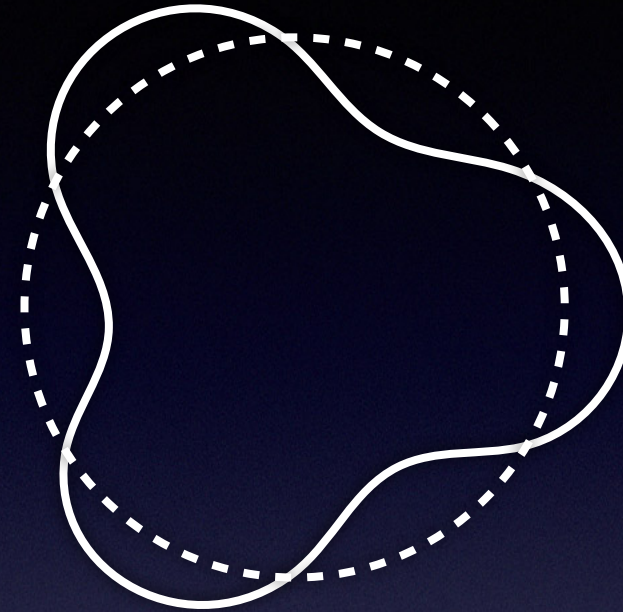
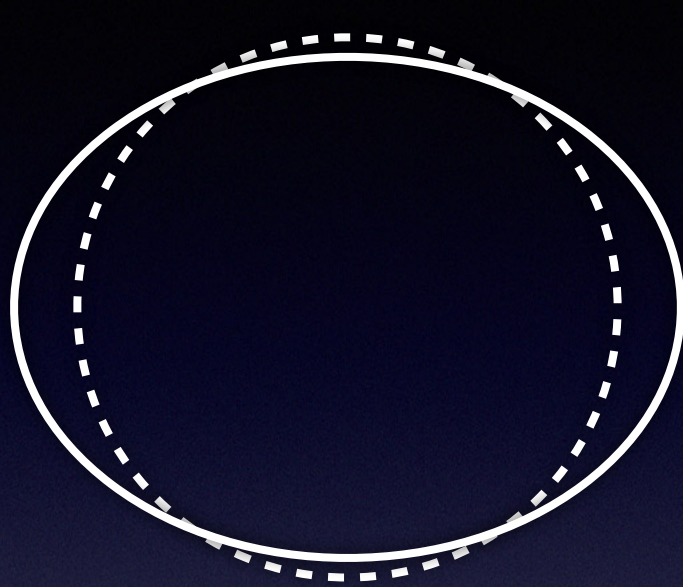


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# Giant resonances: typical collective mode of surface vibration

## classical and intuitive picture



$L=2$ : Giant Quadrupole Resonance (GQR)

$L=3$ : High Energy Octupole Resonance (HEOR)

strongly excited by a one-body operator, exhaust a sum-rule value

$$\hat{F} = \sum_{\sigma, \sigma'} \sum_{\tau, \tau'} \int dr r^L Y_L(\hat{r}) \hat{\psi}^\dagger(r\sigma\tau) \langle \sigma | \begin{Bmatrix} 1 \\ \sigma \end{Bmatrix} | \sigma' \rangle \langle \tau | \begin{Bmatrix} 1 \\ \tau \end{Bmatrix} | \tau' \rangle \hat{\psi}(r\sigma'\tau')$$

space

spin

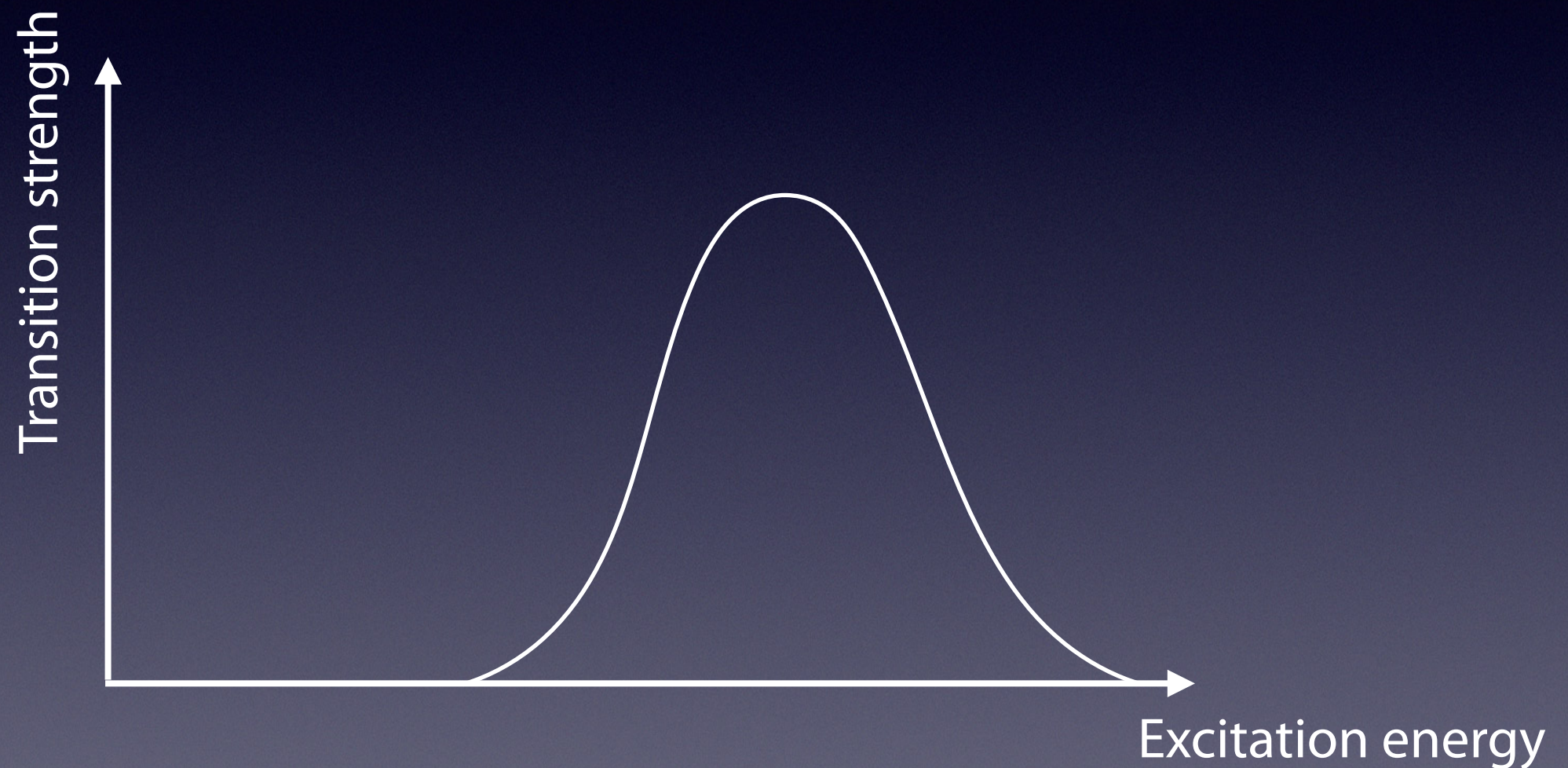
isospin



# Nuclear response: appearance of modes of excitation

rich variety of modes:  $S$  (spin),  $T$  (isospin), and  $L$  (angular mom.)

vibration in spin-space, isospin-space and real-space, and coupling among them  
influenced by many-body correlations (deformation and superfluidity)

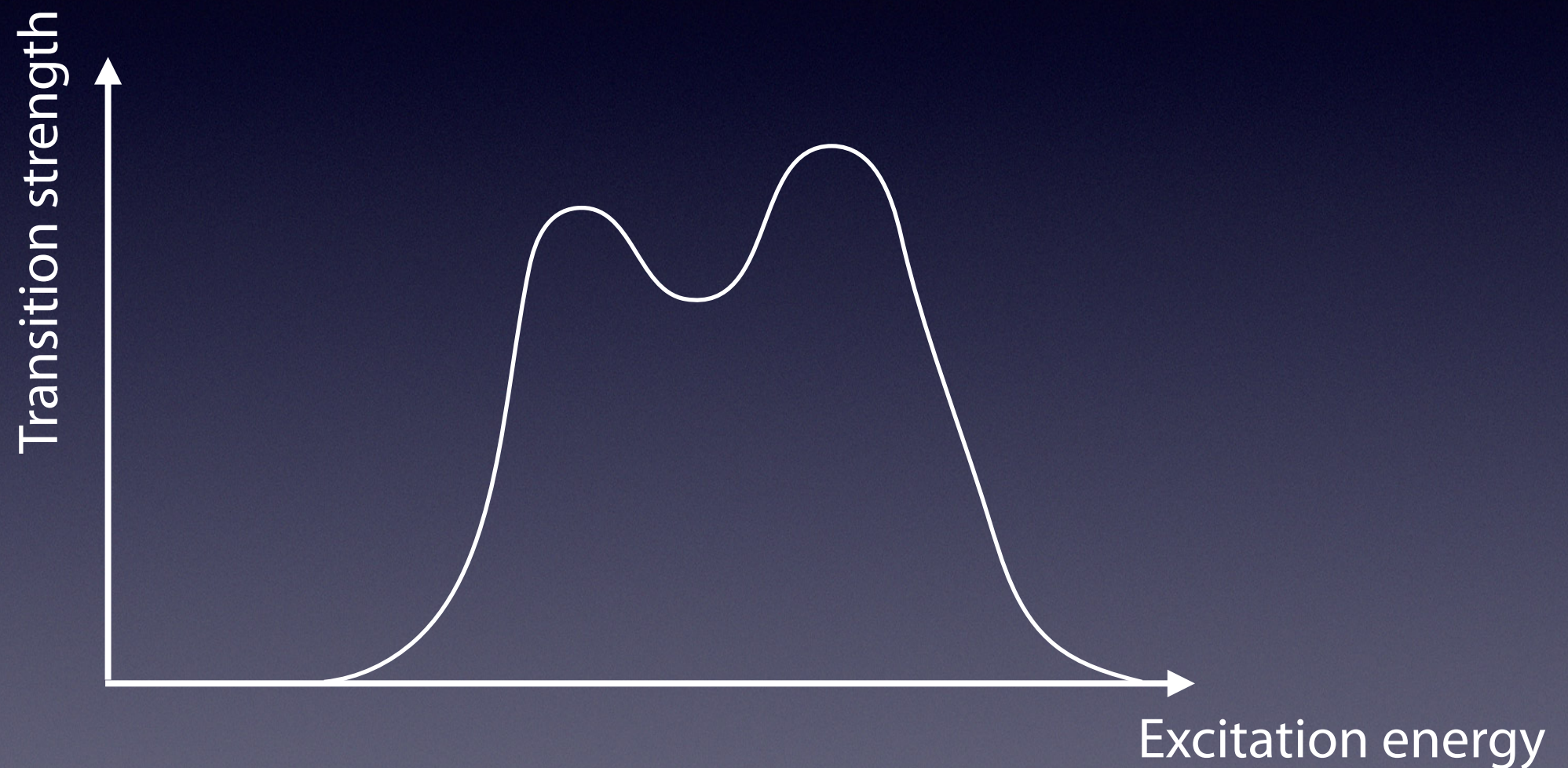




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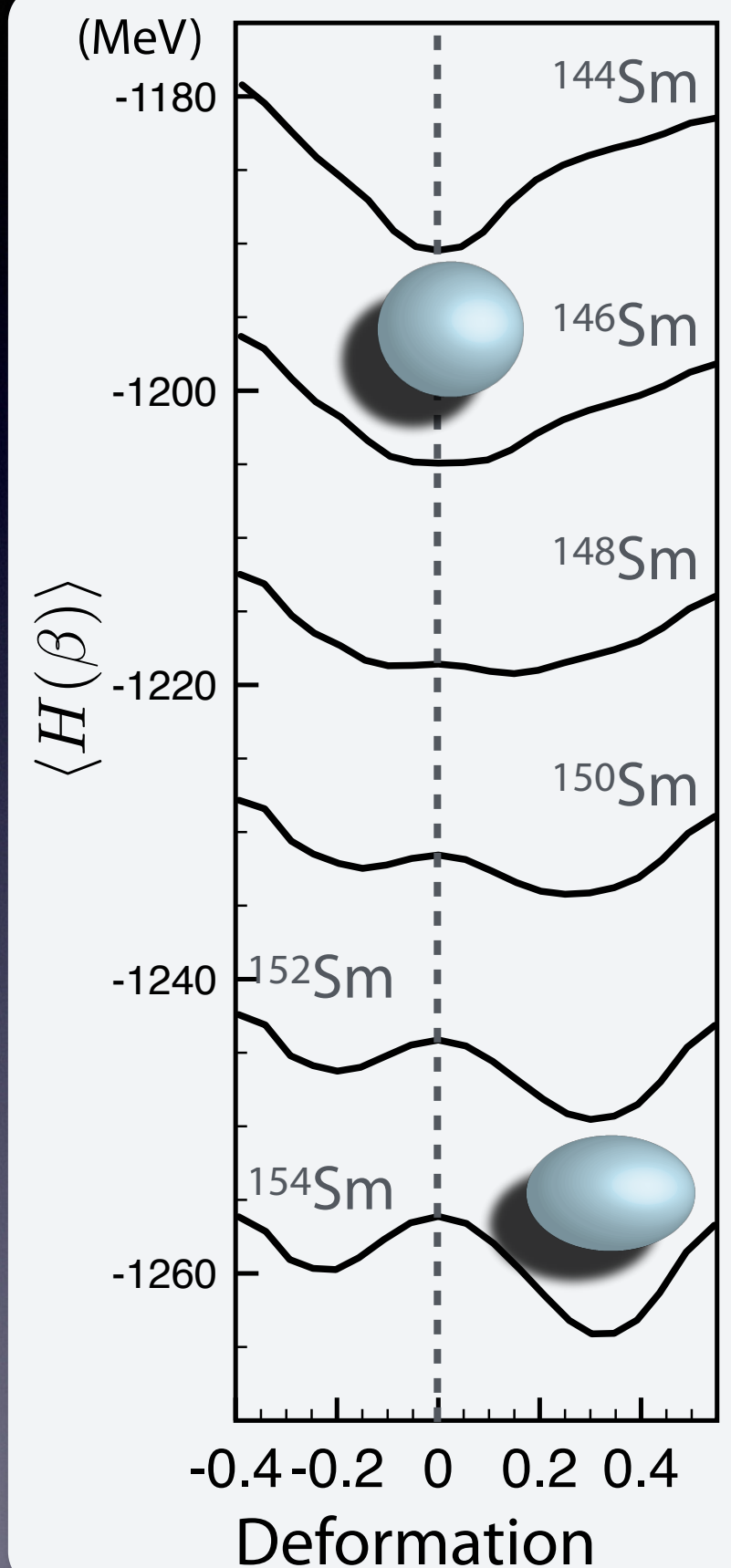
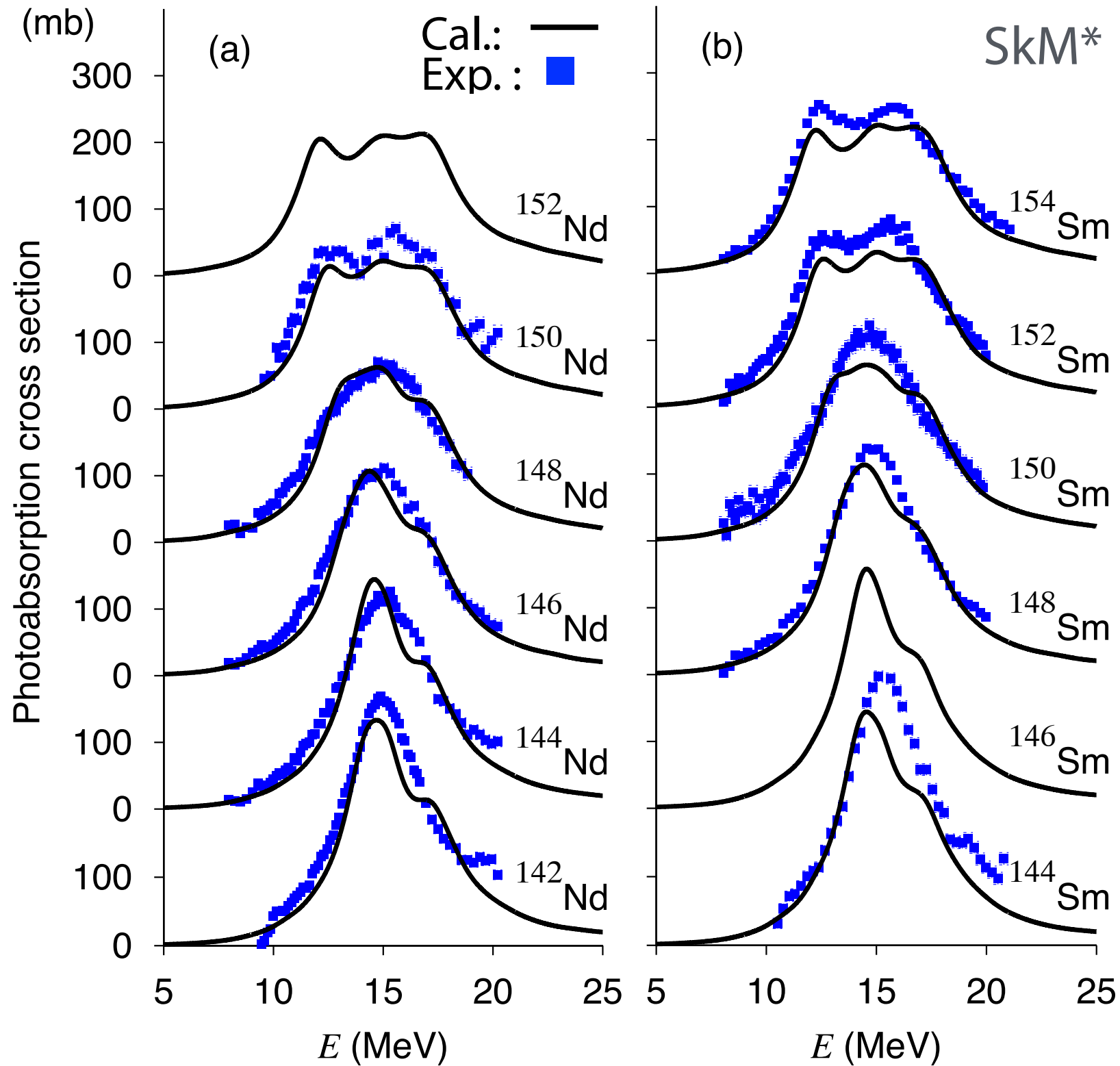
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# Nuclear response: appearance of modes of excitation

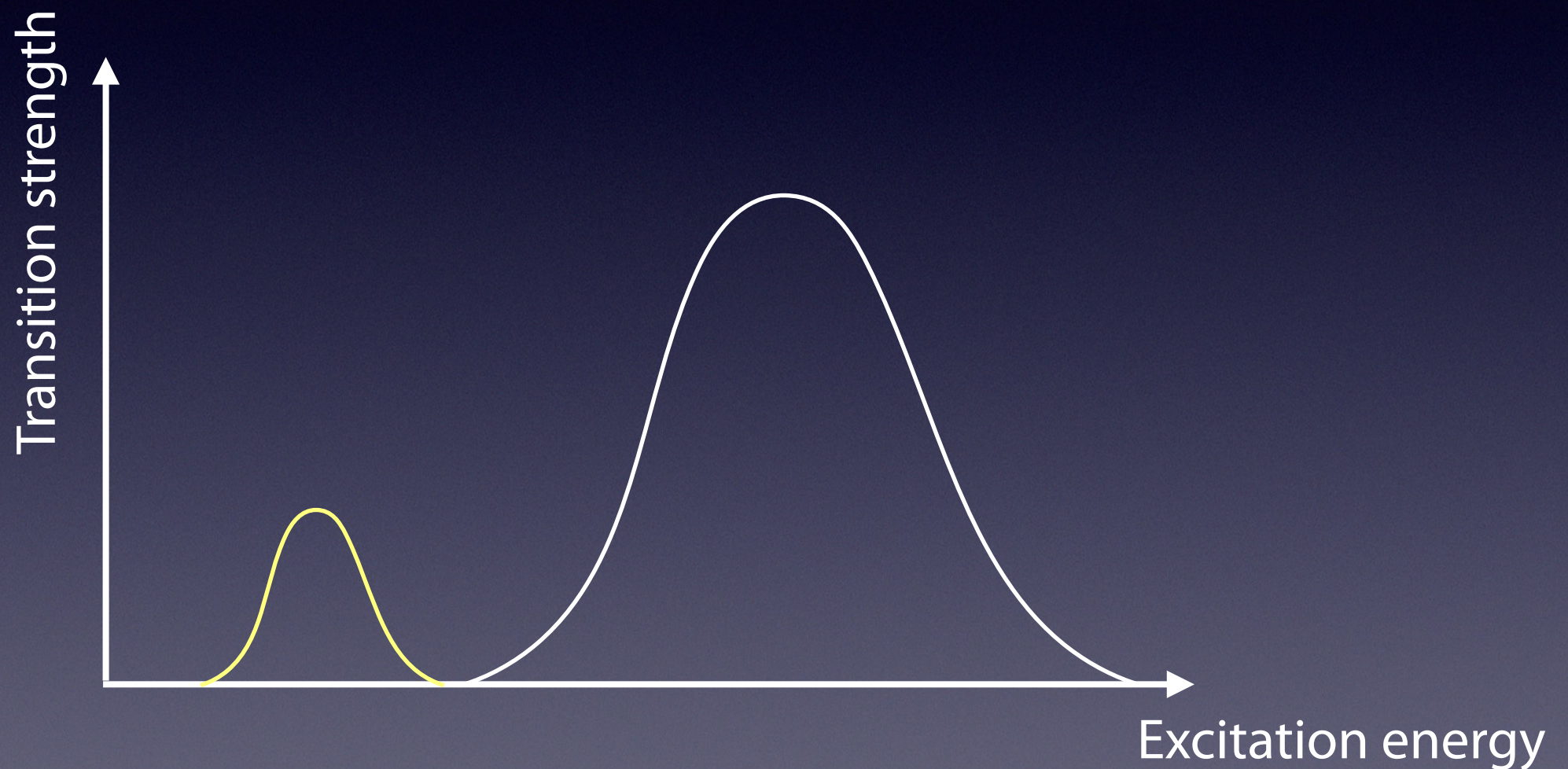




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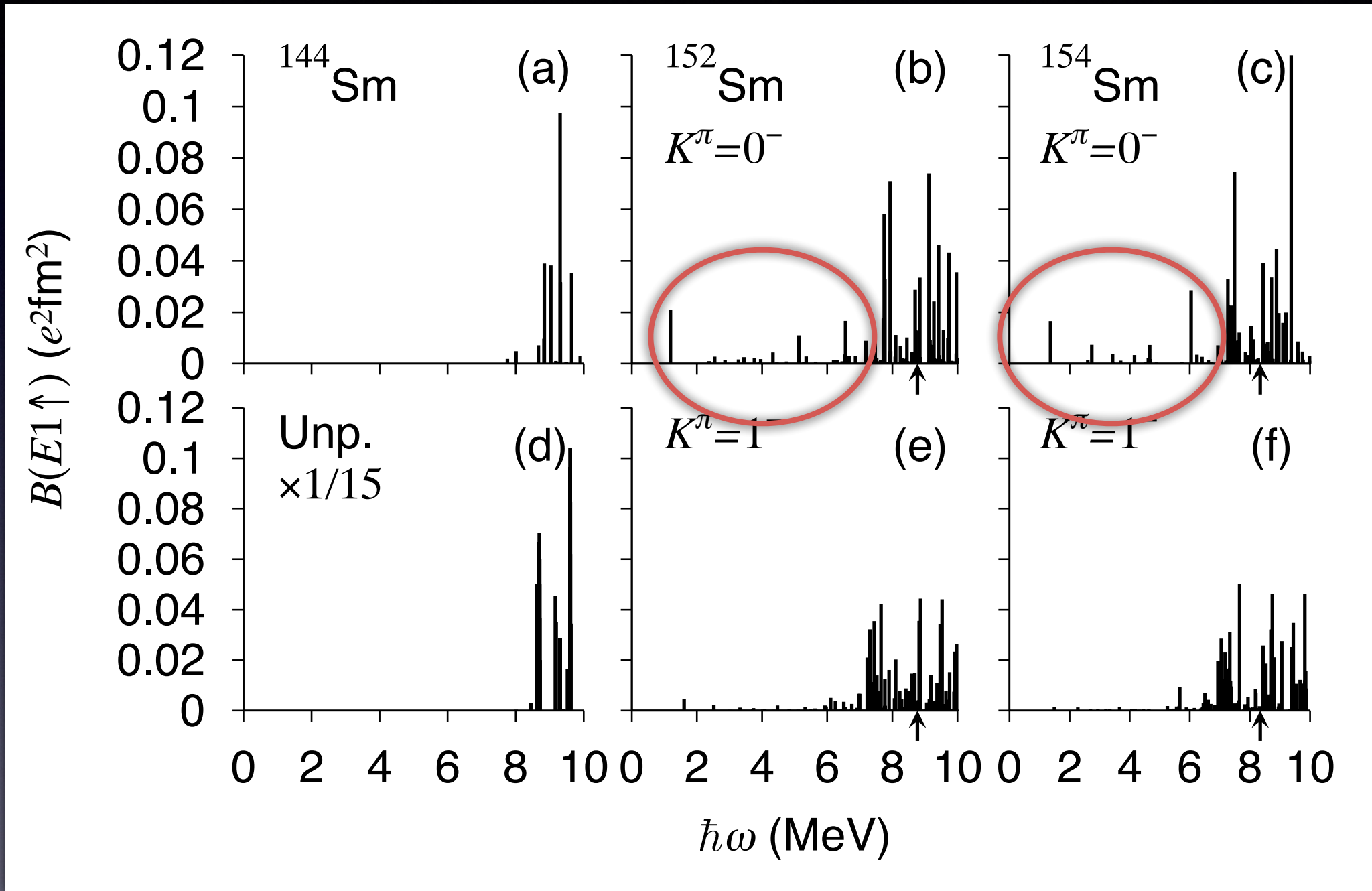
vibration in spin-space, isospin-space and real-space, and coupling among them  
influenced by many-body correlations (deformation and superfluidity)



occurrence of low-lying states associated with **new physics**

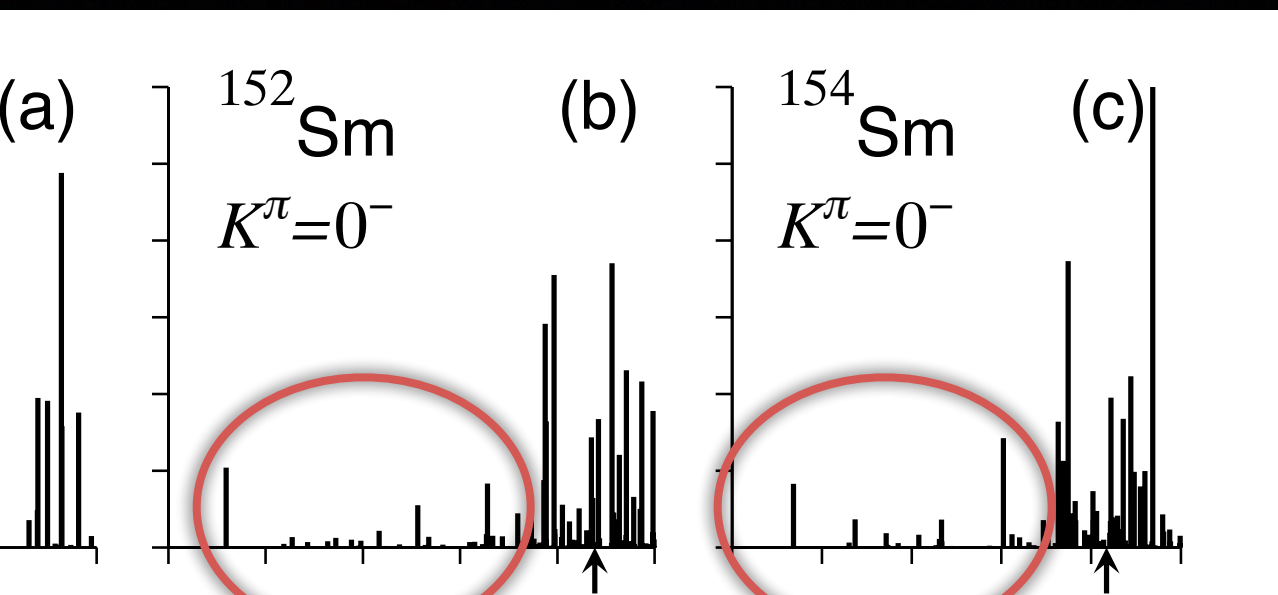


# Nuclear response: appearance of modes of excitation

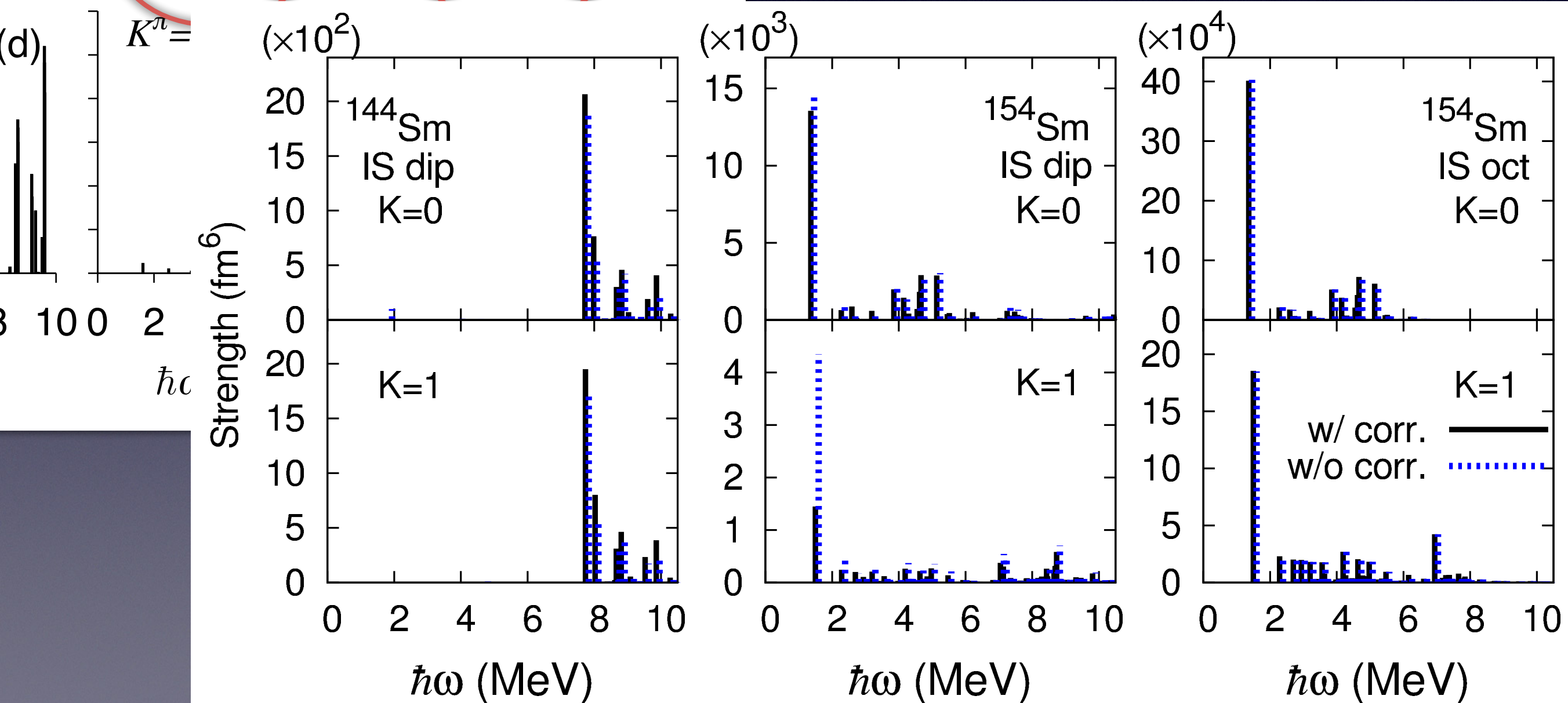




# Nuclear response: appearance of modes of excitation



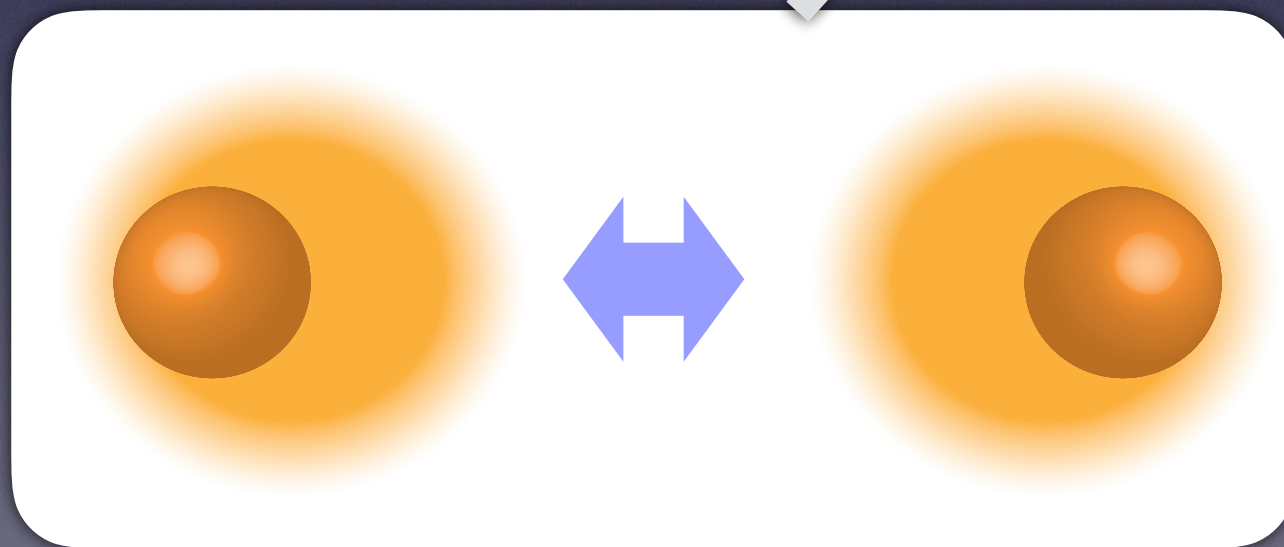
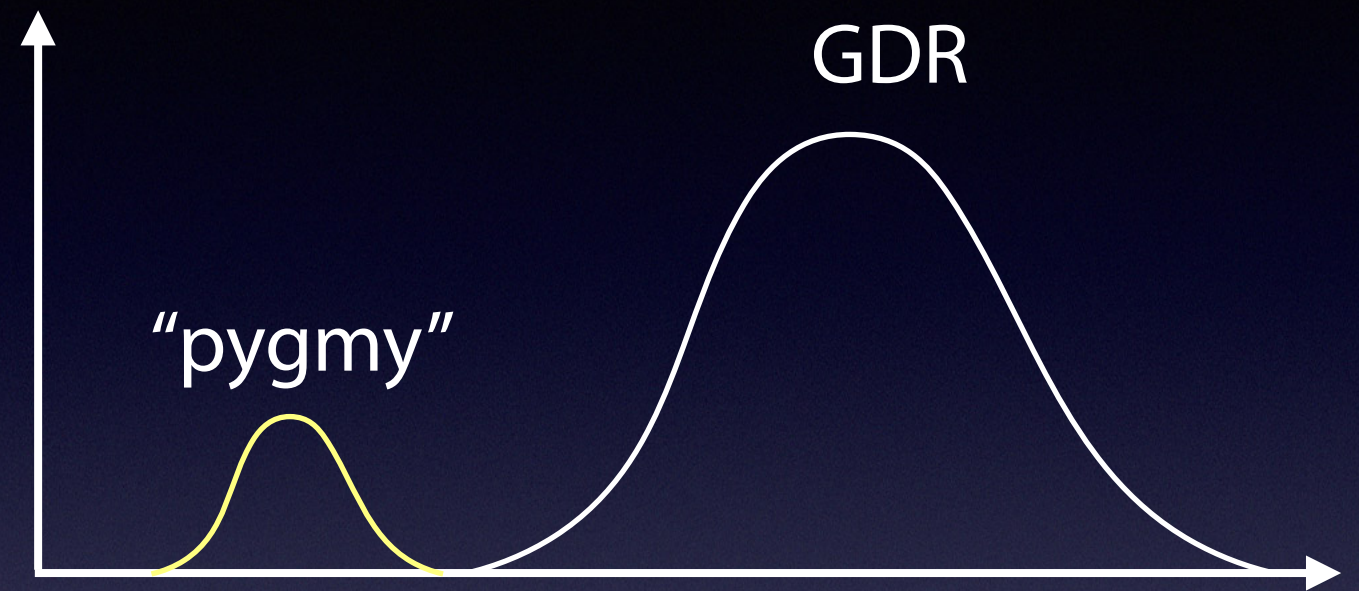
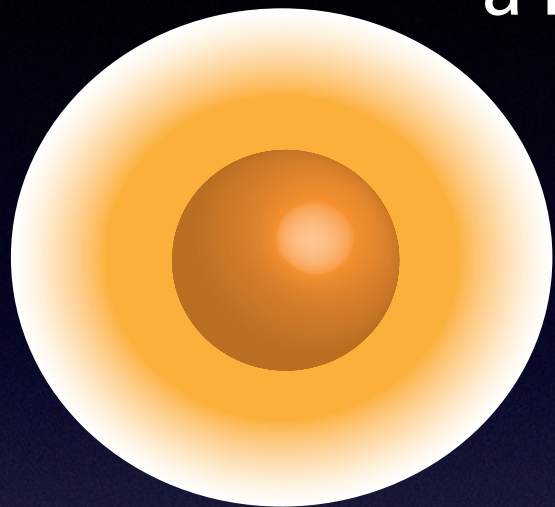
KY, T. Nakatsukasa, PRC88(2013)034309





# Unique modes of excitation in neutron-rich nuclei

neutron-skin structure  
a new degree of freedom



neutron-skin excitation modes ??



# Mysterious PDR

Theoretical calculations predict

PDR appears in neutron-rich nuclei systematically

Its collectivity depends on the nucleus, and the model employed

Unravelling the structure is a big issue in nuclear physics

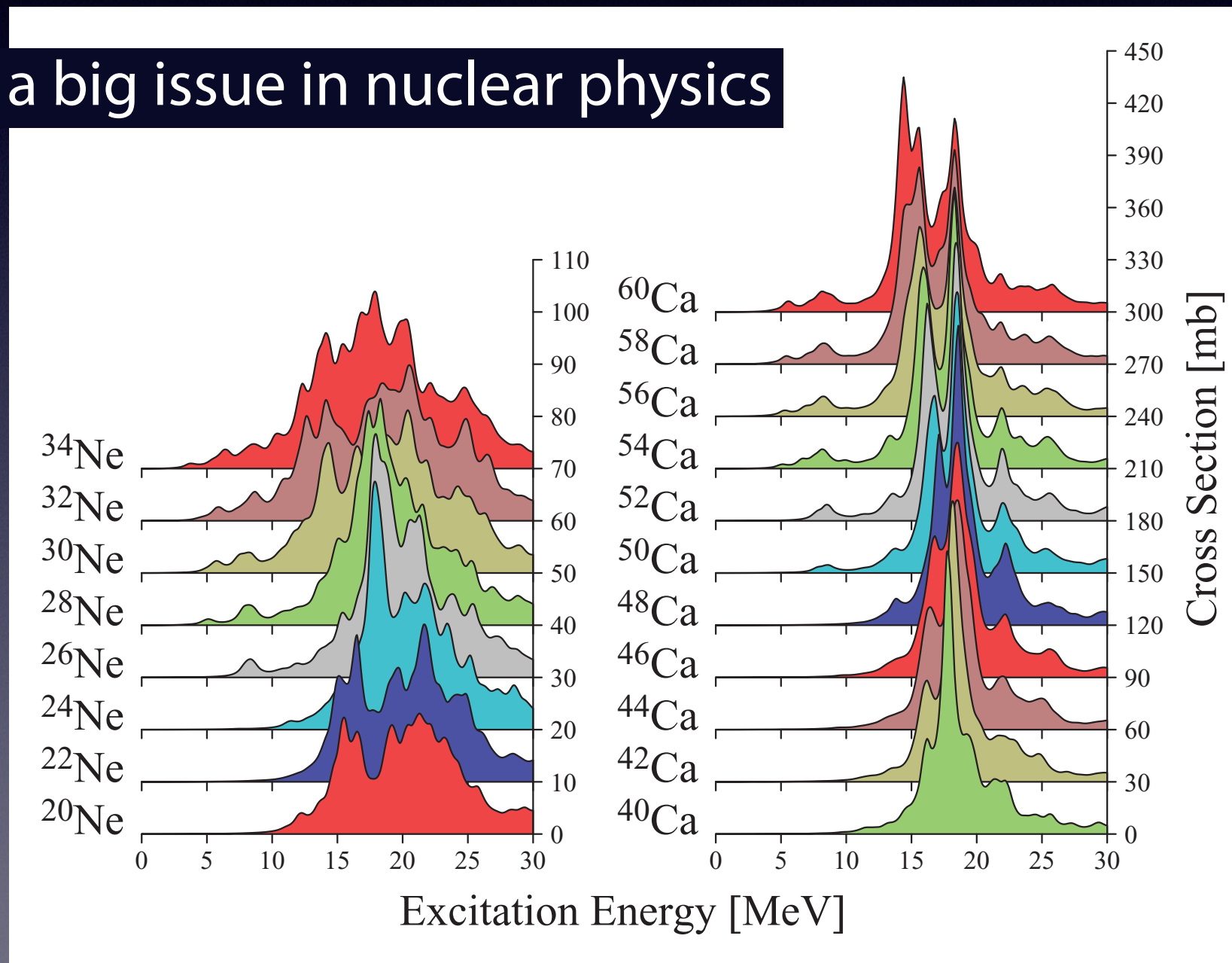
isospin structure

vortical nature

...



Different probes needed





## IV dipole excitations in neutron-rich nuclei

$$\hat{F}_{K\mu} = \int dr \sum_{\sigma\sigma'} \sum_{\tau\tau'} r Y_{1K}(\hat{r}) \delta_{\sigma,\sigma'} \langle \tau | \tau_{\mu} | \tau' \rangle \hat{\psi}^{\dagger}(r\sigma\tau) \hat{\psi}(r'\sigma'\tau')$$

analog of pygmy dipole mode??

understanding of PDR in terms of iso-triplet states

isospin character of PDR

general mechanism for emergence of the PDR

any other types of excitation mode??



# IV dipole excitations in neutron-rich nuclei

## systematic calculation based on nuclear DFT

fully-selfconsistent calculation

Skyrme-HFB + proton-neutron QRPA

Ca:  $N = 28-56$

Ni:  $N = 50-66$

Sn:  $N = 82-110$

spherical systems for simplicity

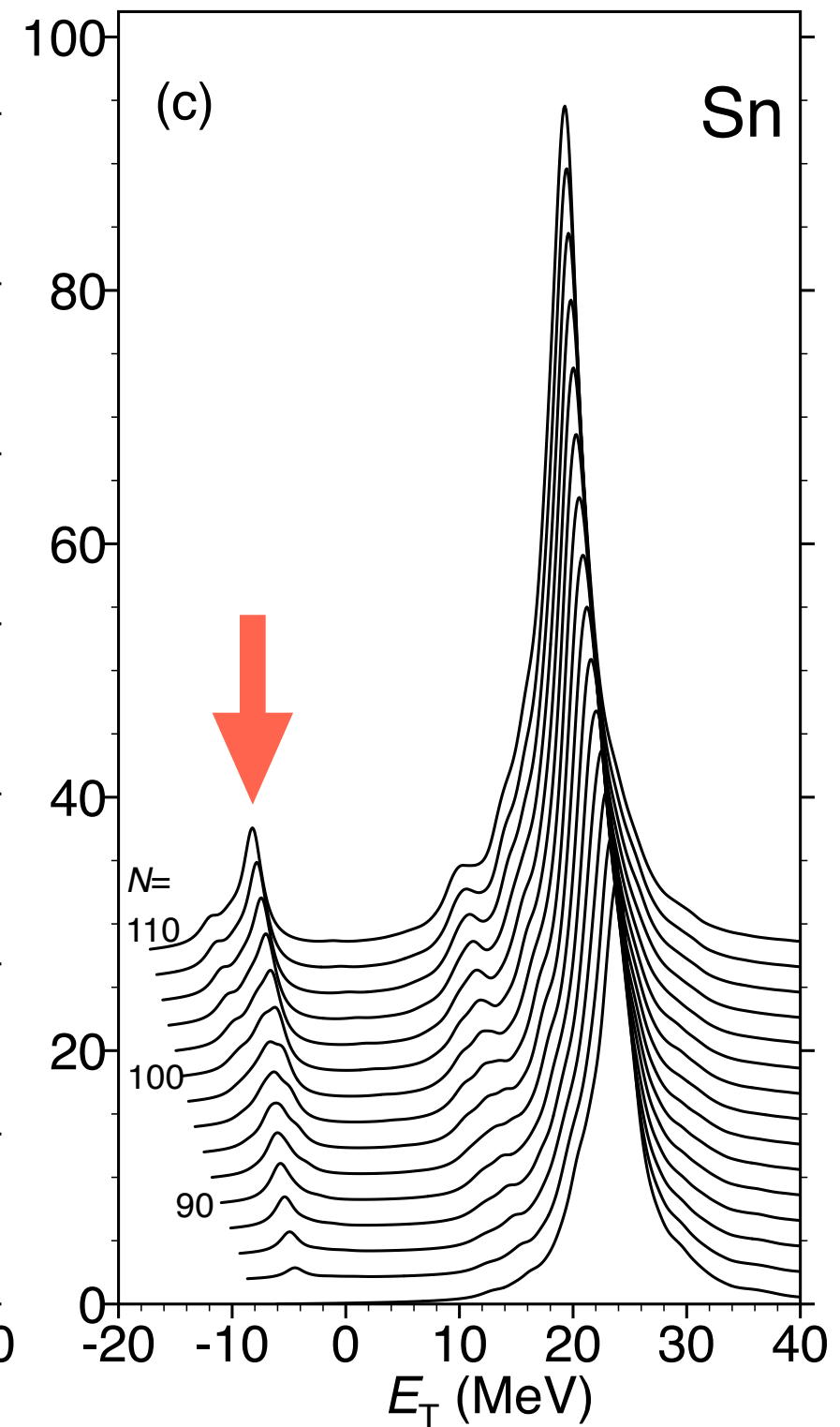
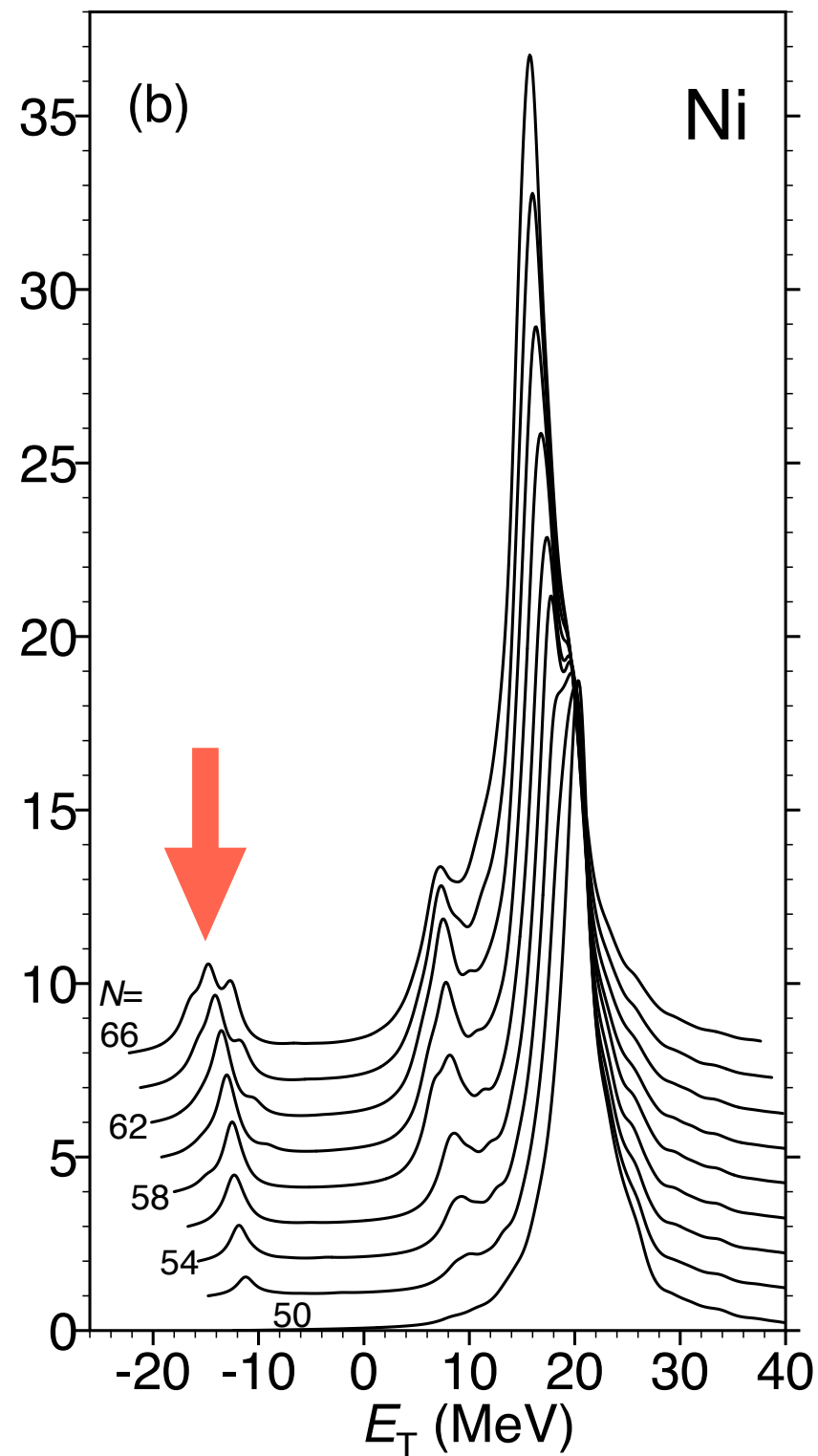
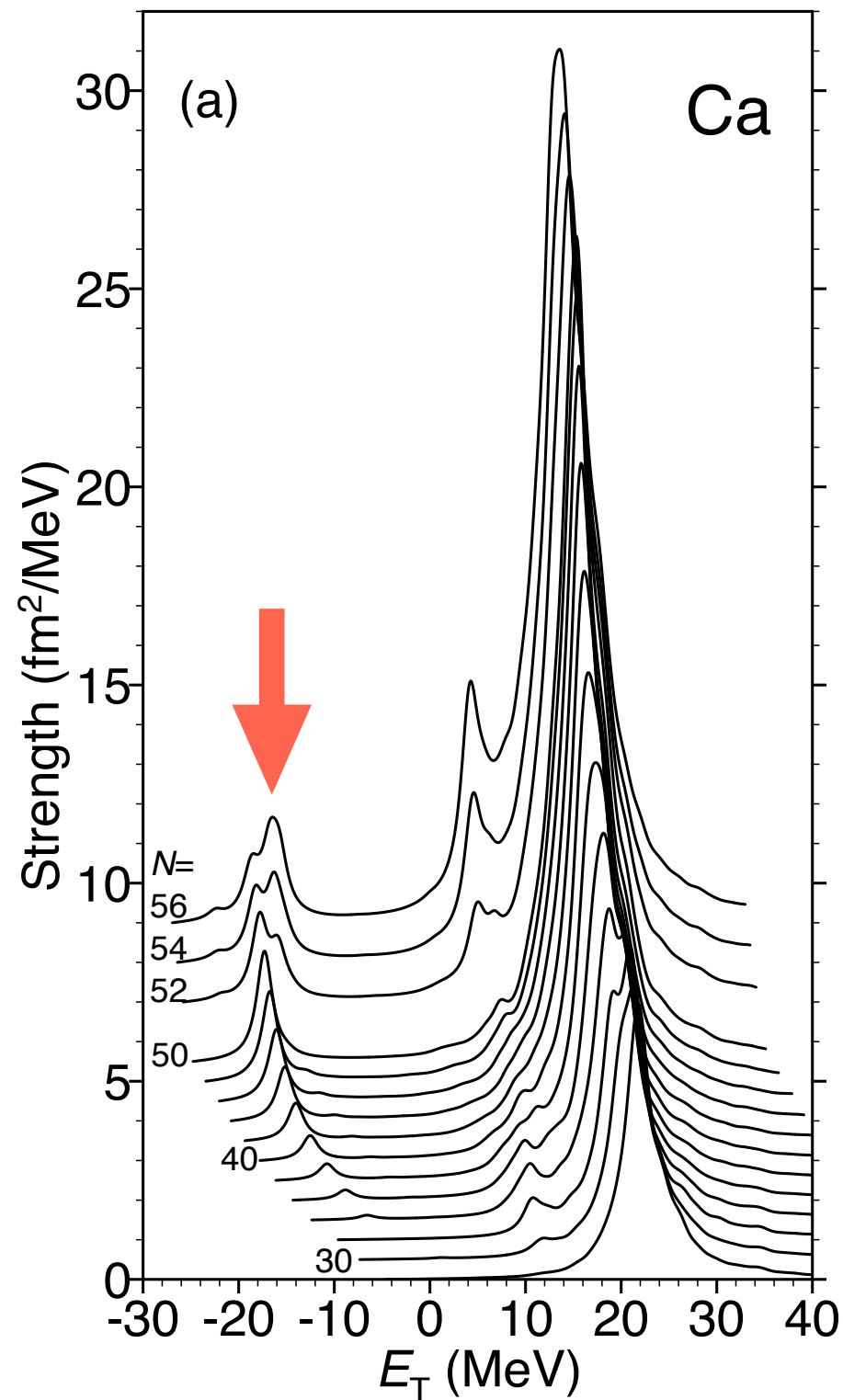
cf.  $T=0$  pairing does not affect the following discussions



# IV dipole strength distributions ( $\tau = -1$ )

KY, PRC96(2017)051302R

SkM\*,  $\Gamma=2.0$  MeV





# Mechanism for occurrence of the low-lying states

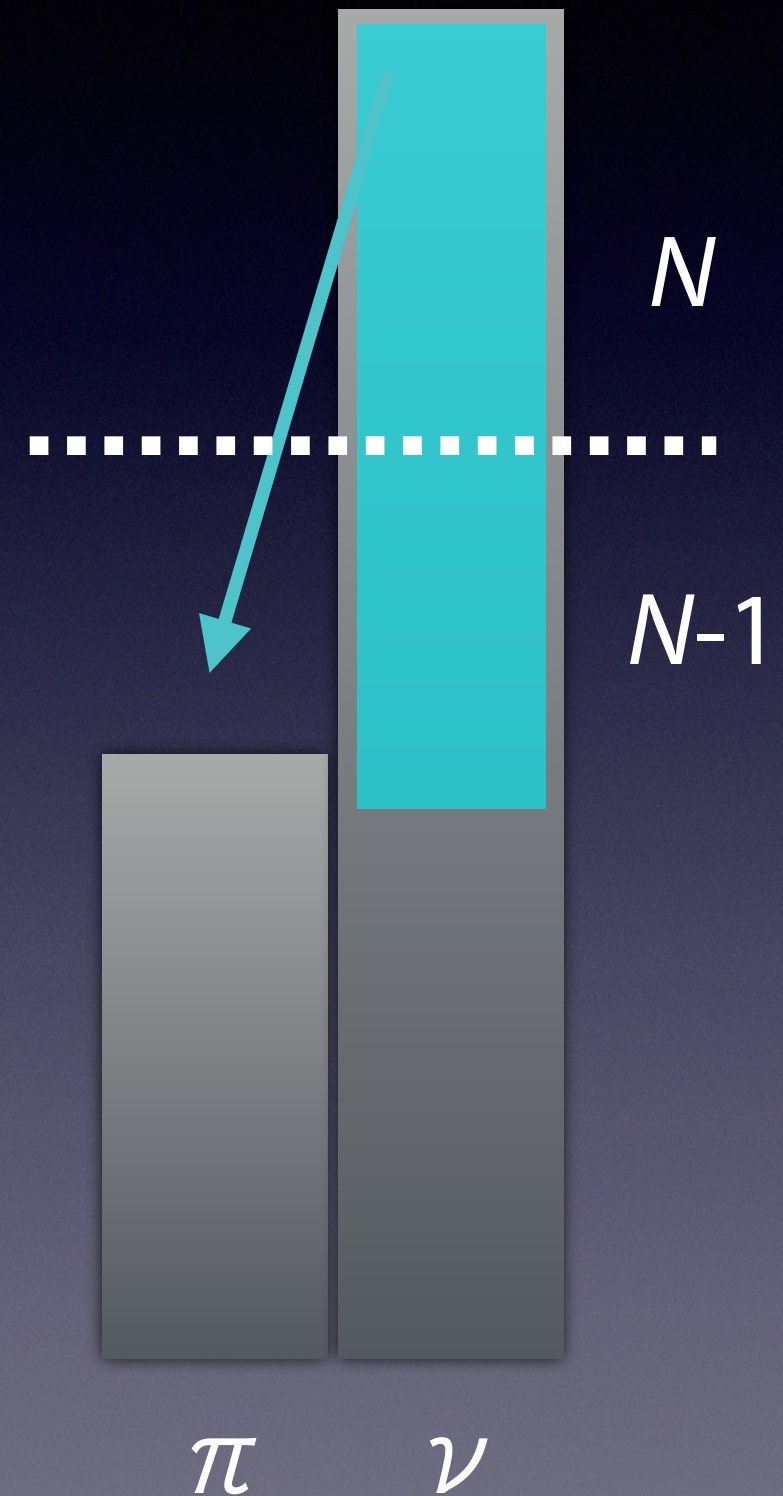
cross-shell ( $N \rightarrow N-1$ ) excitation in low-energy

$-1\hbar\omega$  excitation

neutrons are weakly bound/  
(quasi)neutrons are in the continuum when  $|\lambda| \approx 0$



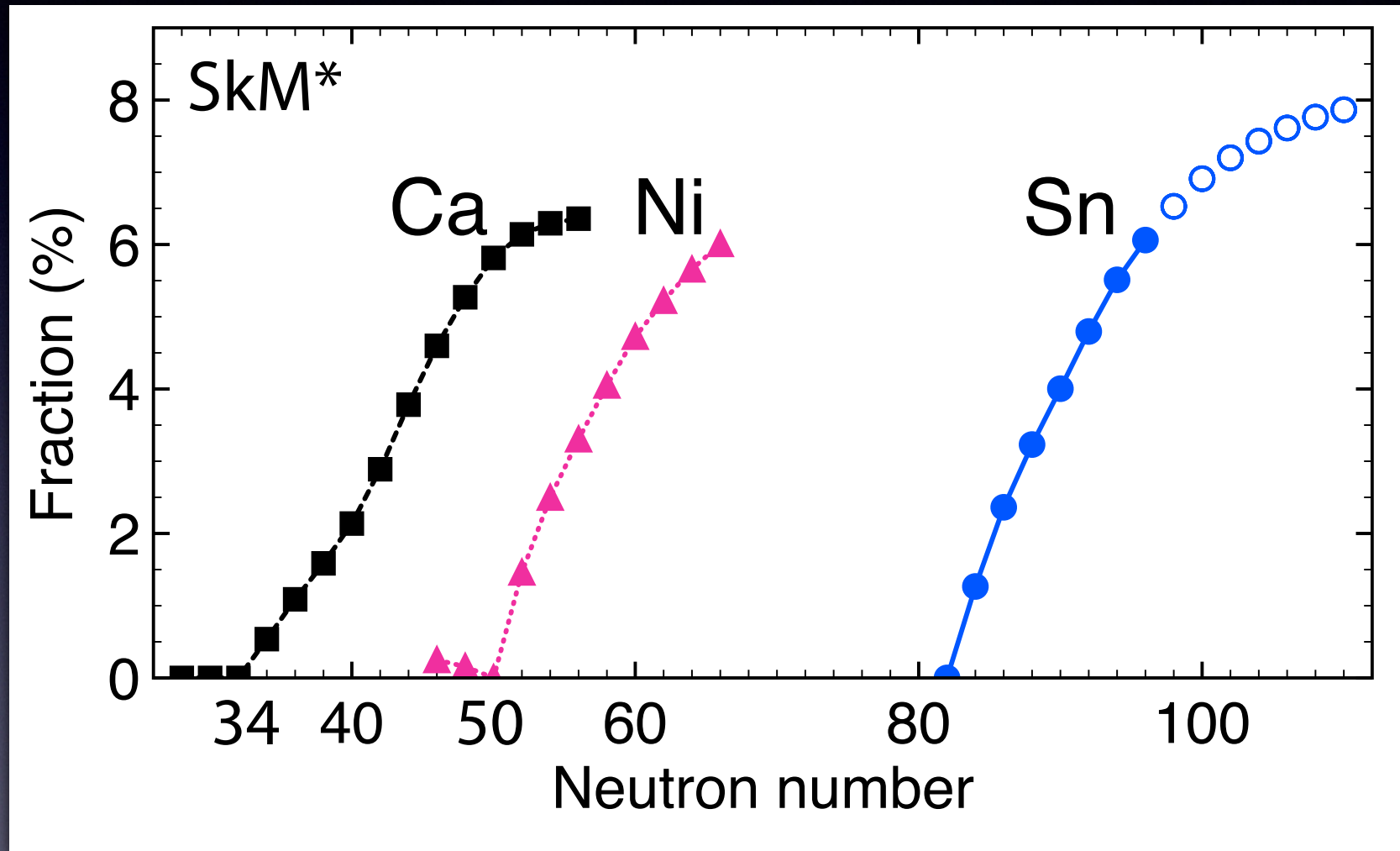
protons are deeply bound





# Onset of the low-lying states: strong shell effect

summed strength in low-energy ( $\omega < 15$  MeV,  $E_T < 0$  MeV)



40	$g_{9/2}$
34	$f_{5/2}$
32	$p_{1/2}$
28	$p_{3/2}$
20	$f_{7/2}$

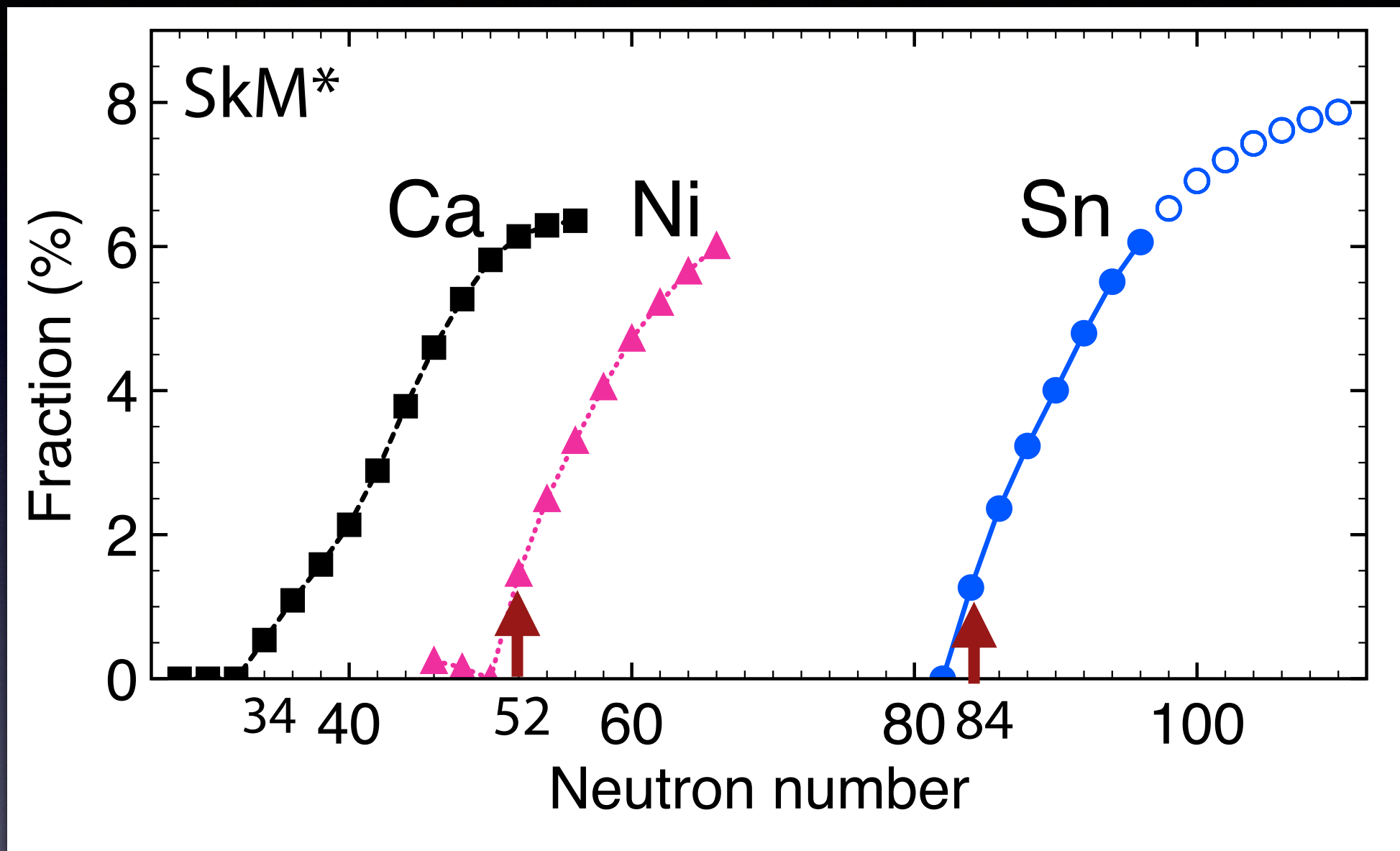
$\nu g_{9/2} \rightarrow \pi f_{7/2}$

due to neutron pairing

gradual development



# Onset of the low-lying states: strong shell effect



occupation of  $2d_{5/2}$

$\nu d_{5/2} \rightarrow \pi p_{3/2}$

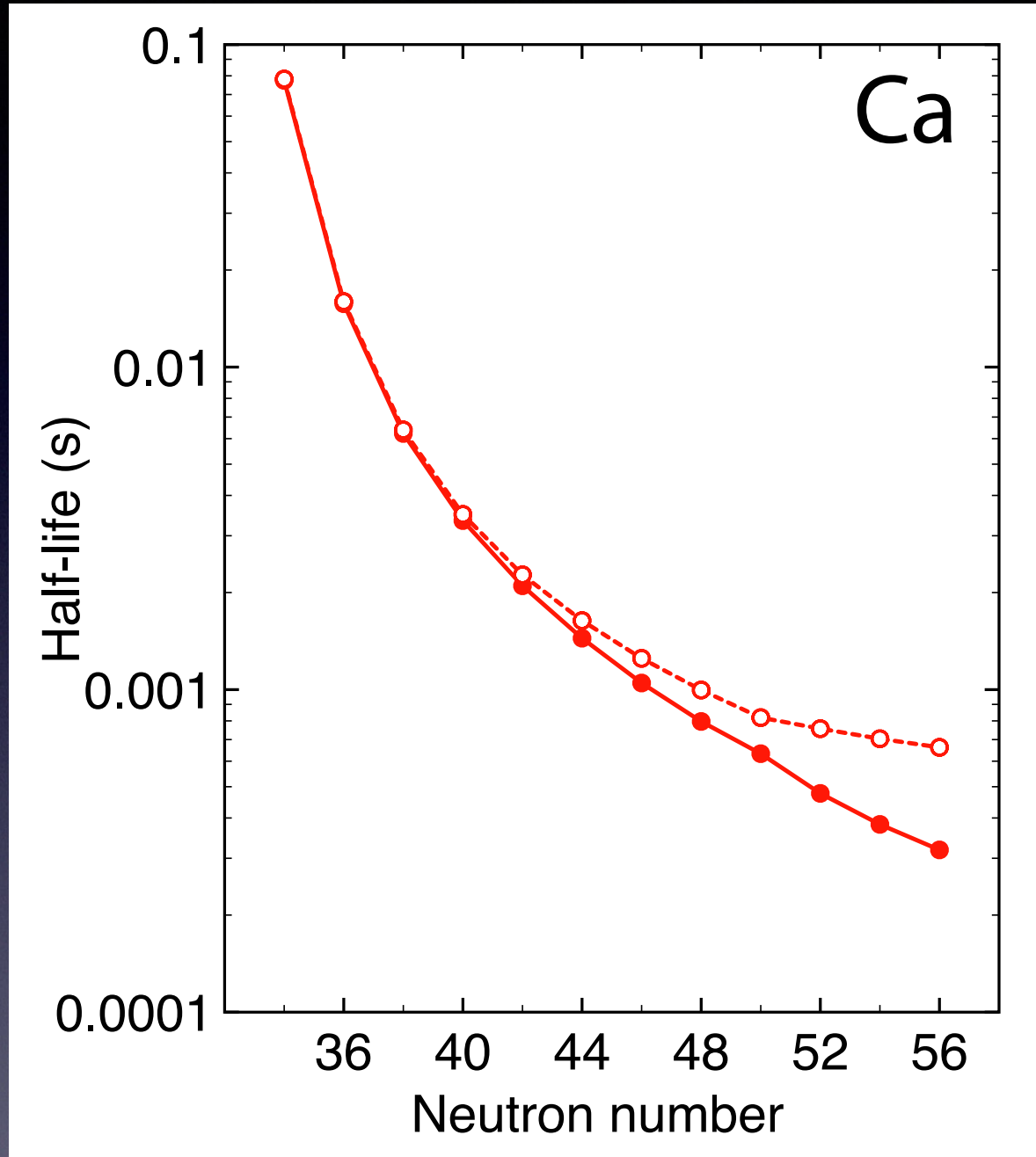
occupation of  $2f_{7/2}$

$\nu f_{7/2} \rightarrow \pi d_{5/2}$

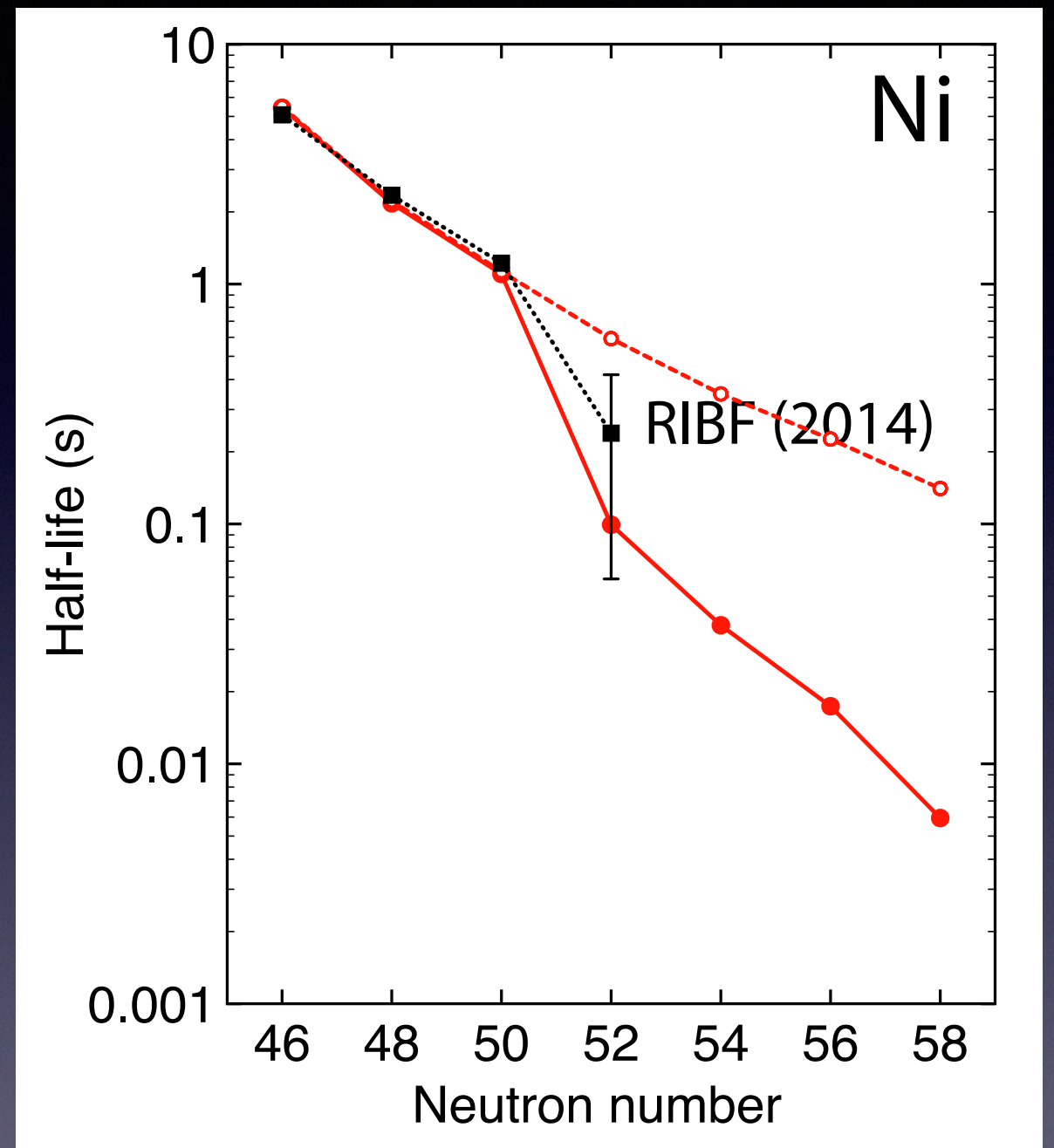


# Effect of the low-lying dipole states on $\beta$ -decay rate

Allowed + FF transitions



gradually dominating



suddenly dominating

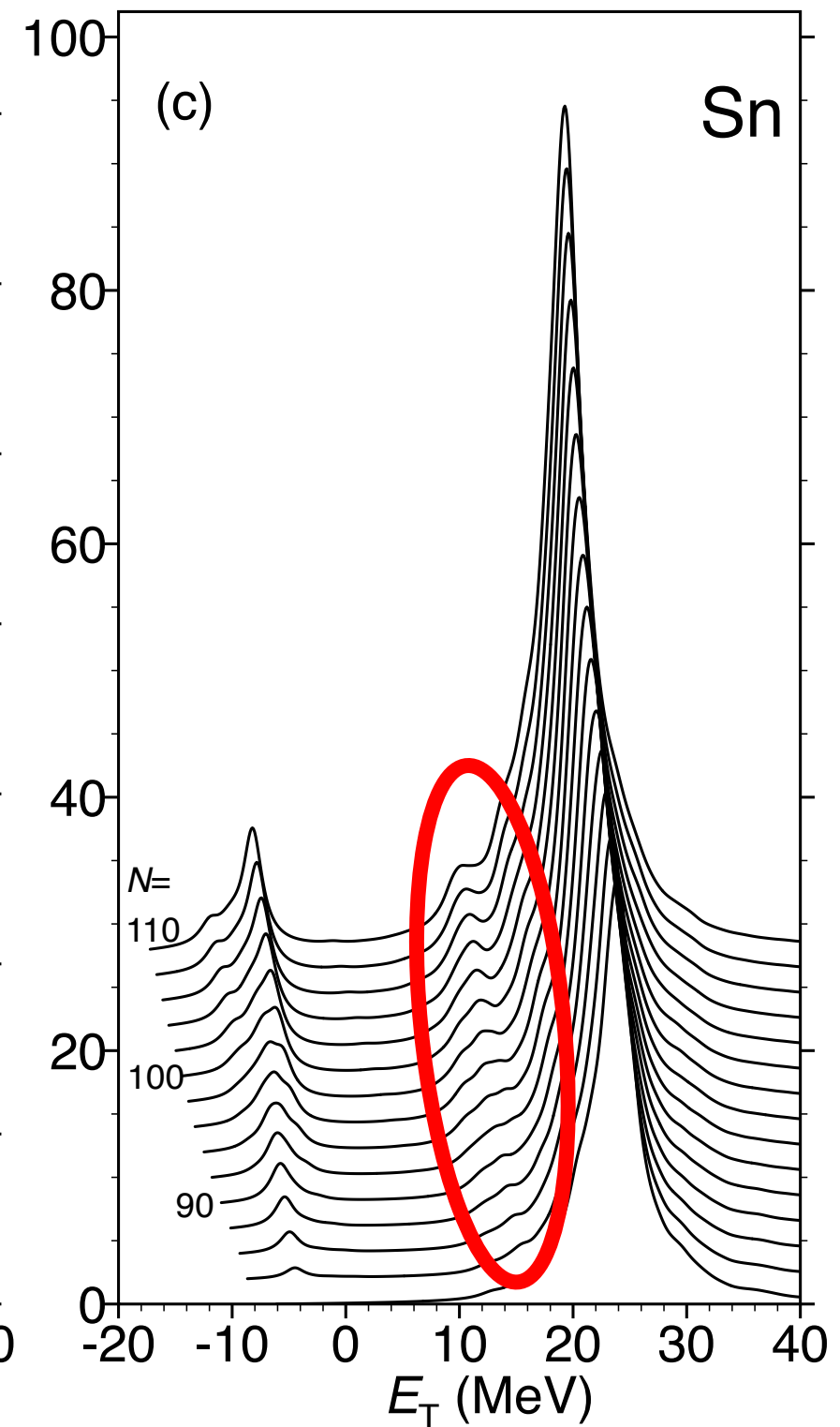
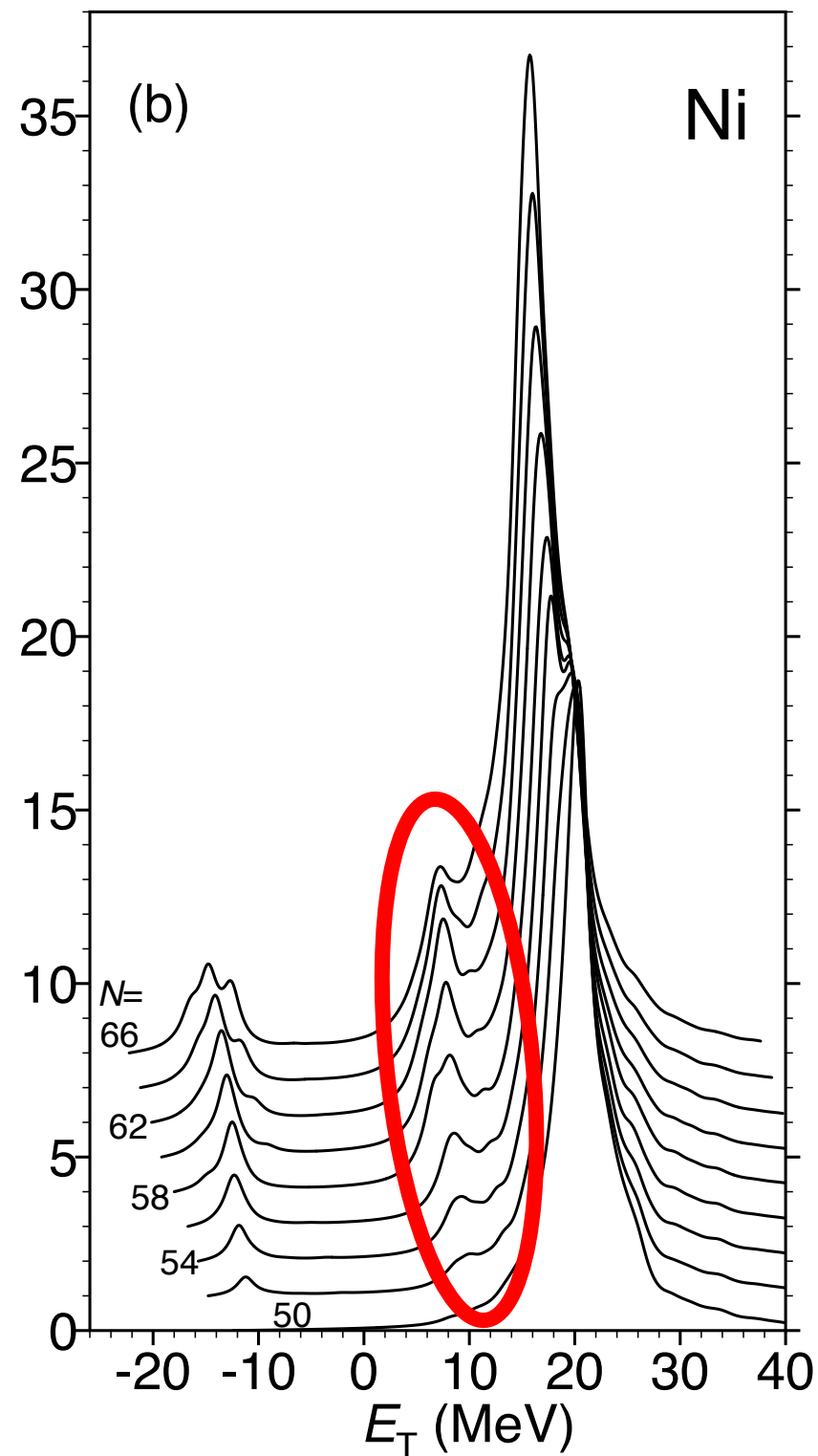
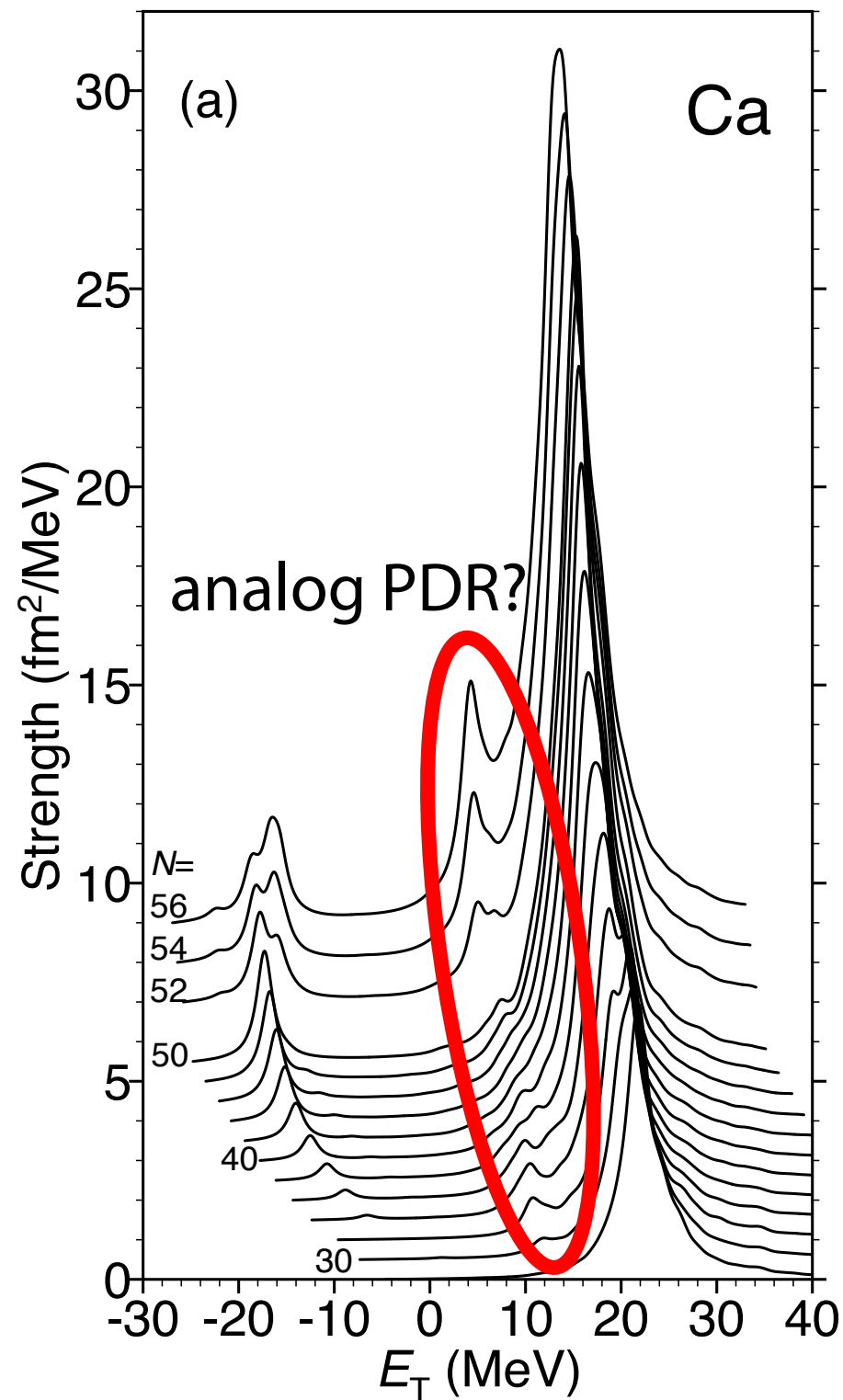
at  $N > 50$



# IV dipole strength distributions ( $\tau = -1$ )

KY, PRC96(2017)051302R

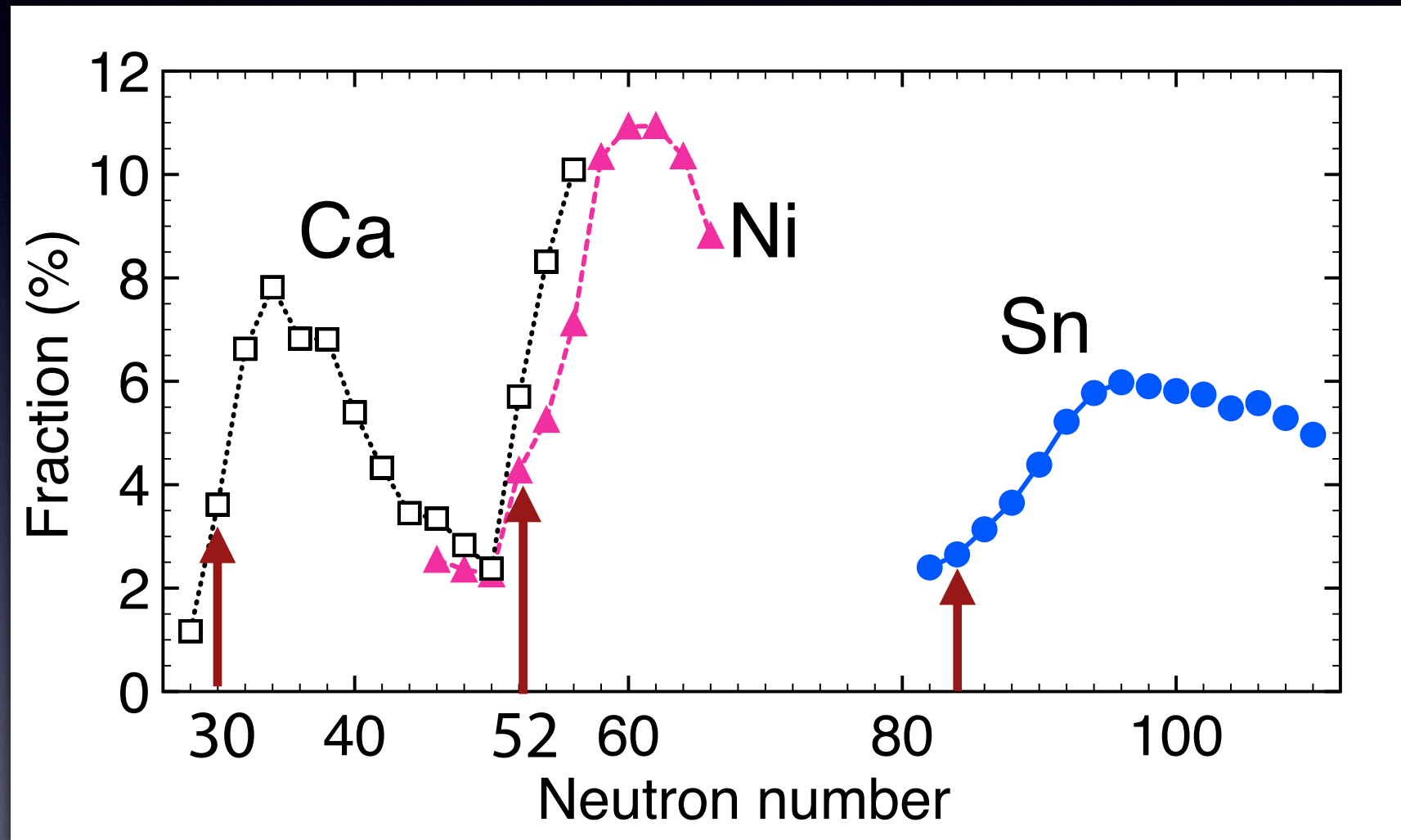
SkM\*,  $\Gamma=2.0$  MeV





# Appearance of the analog PDR

summed strength below the GR  
excluding  $-1\hbar\omega$  type states

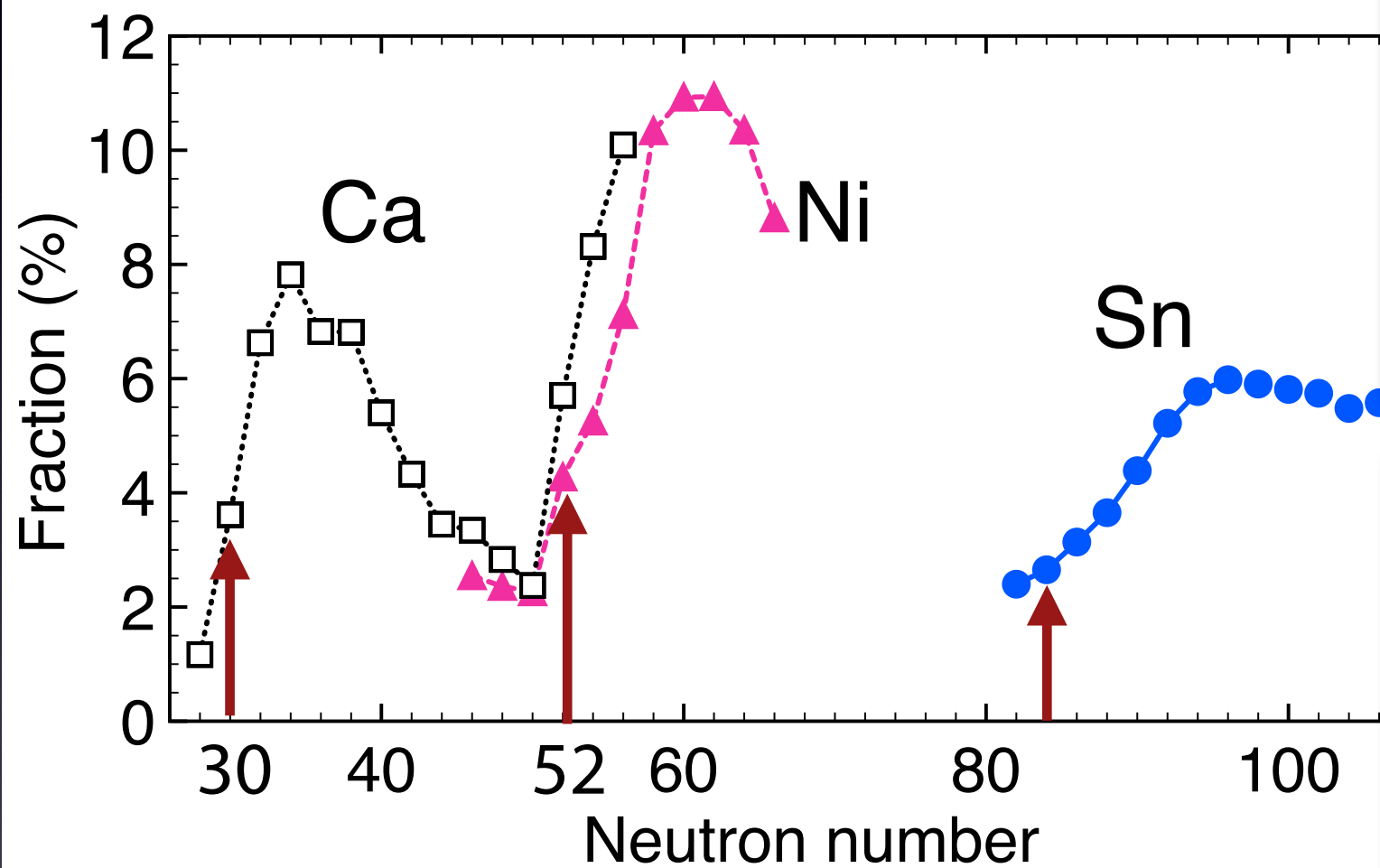


occupation of weakly-bound  $p_{3/2}$  ( $N > 28$ ),  
 $d_{5/2}$  ( $N > 50$ ), and  $f_{7/2}$  and  $f_{5/2}$  ( $N > 82$ )

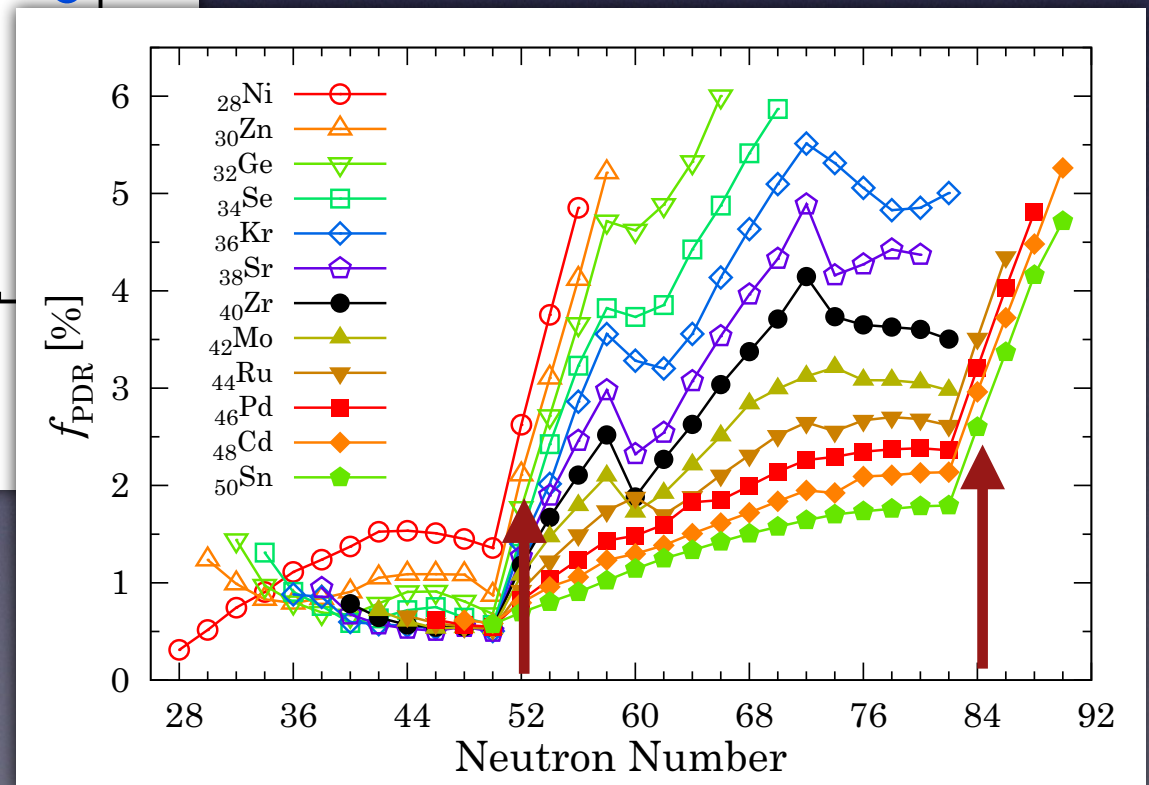
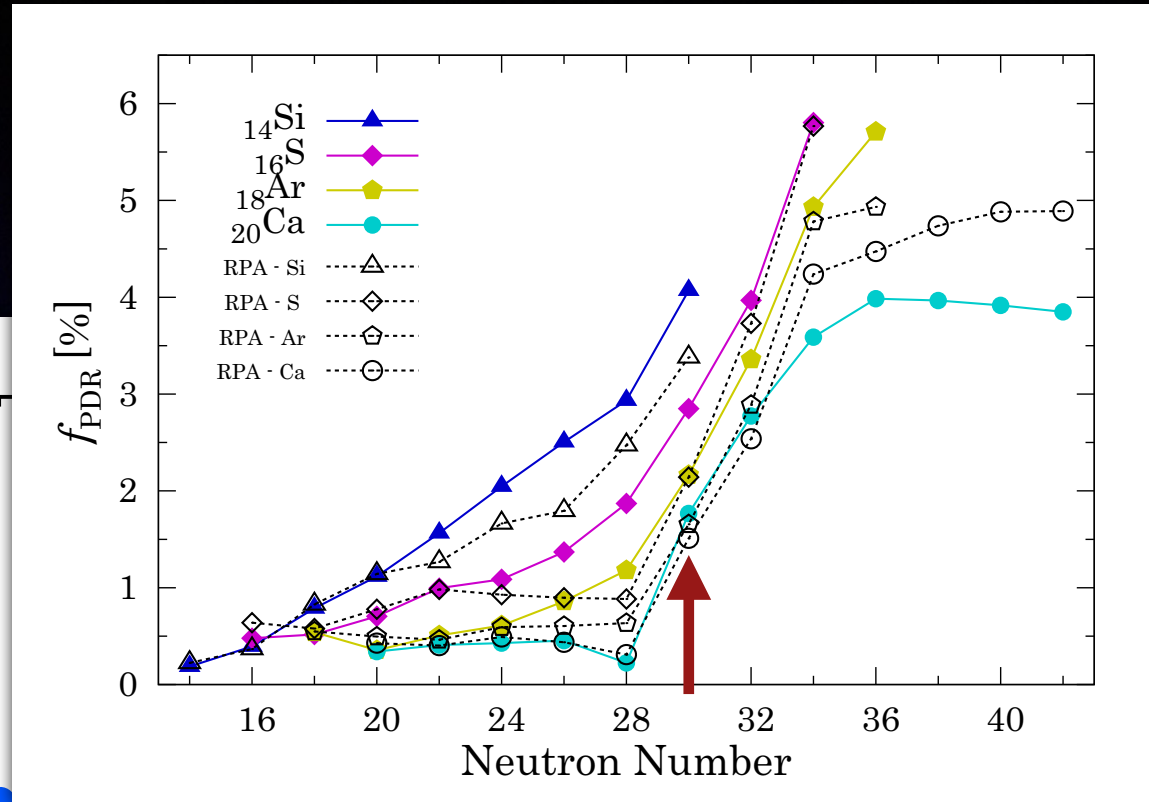


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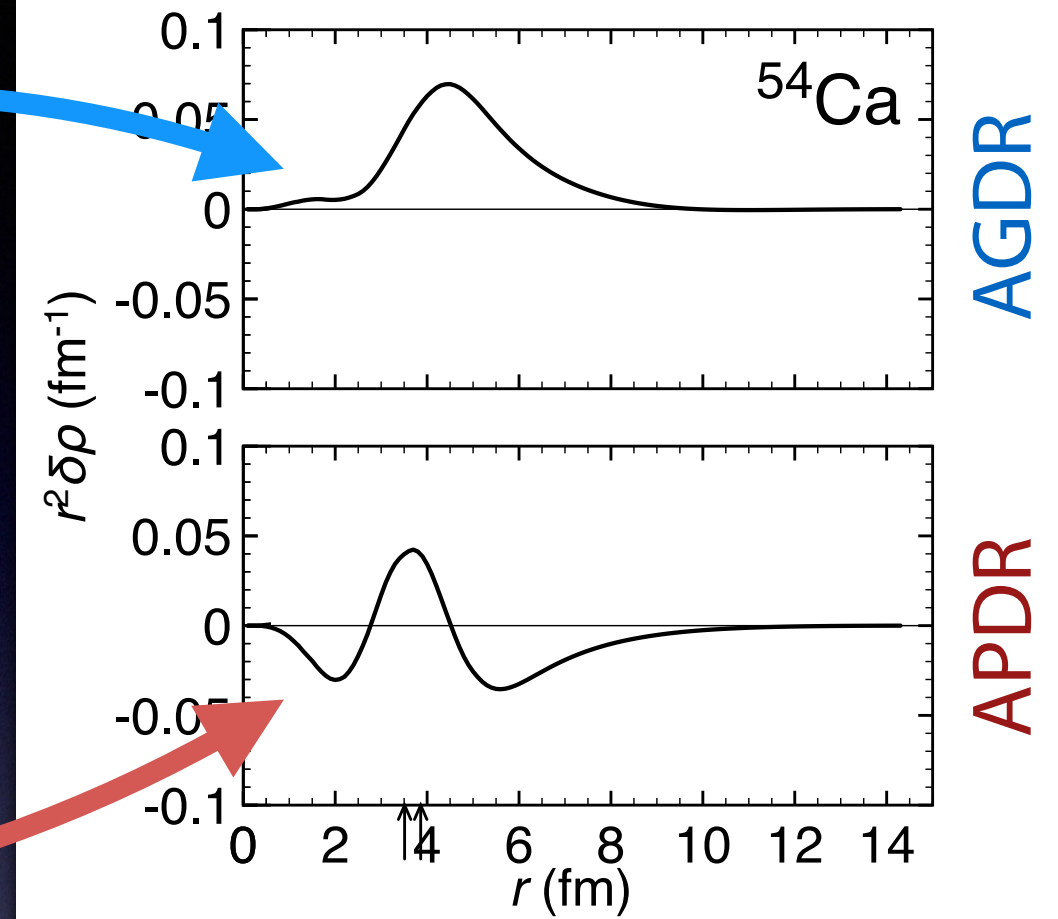
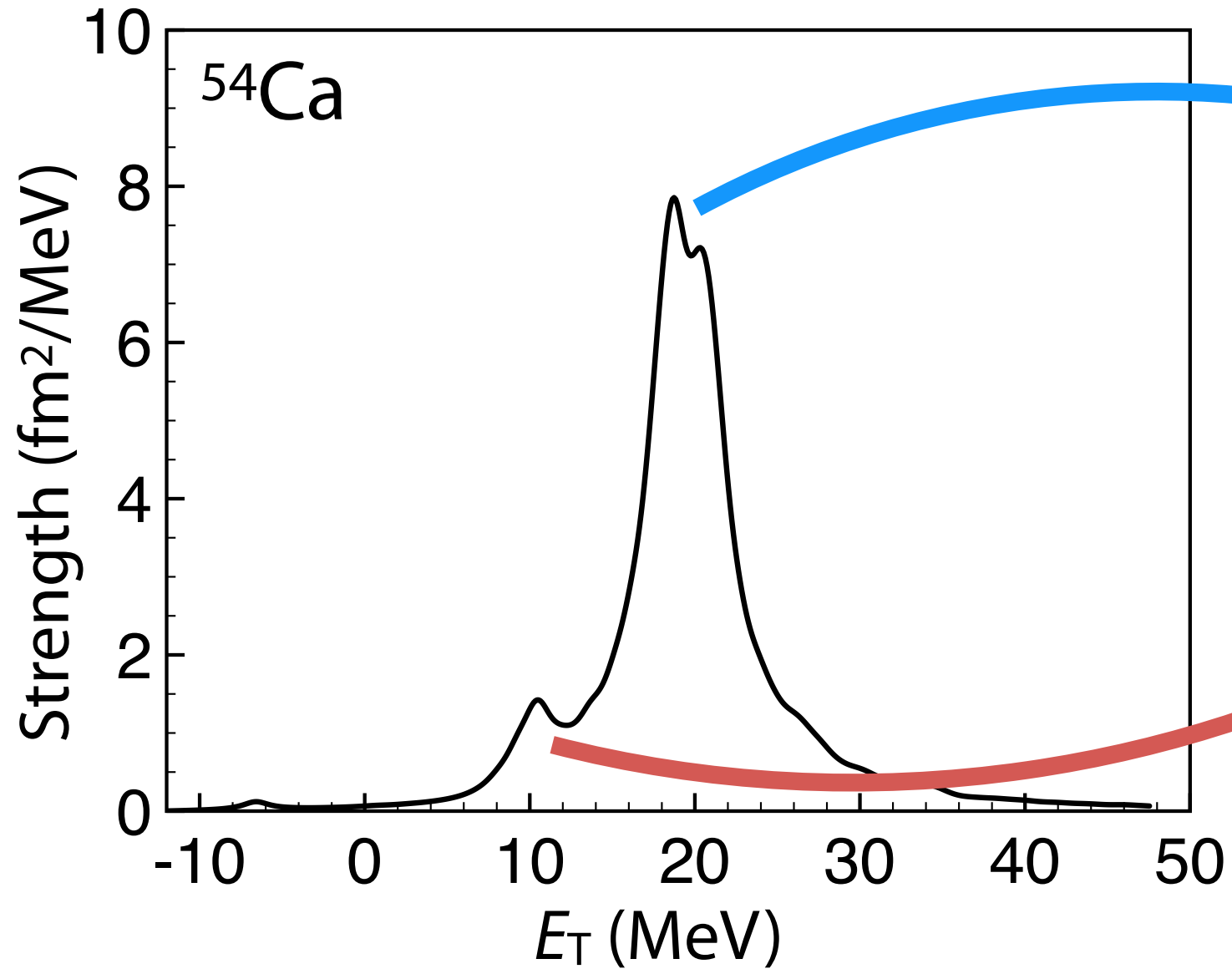


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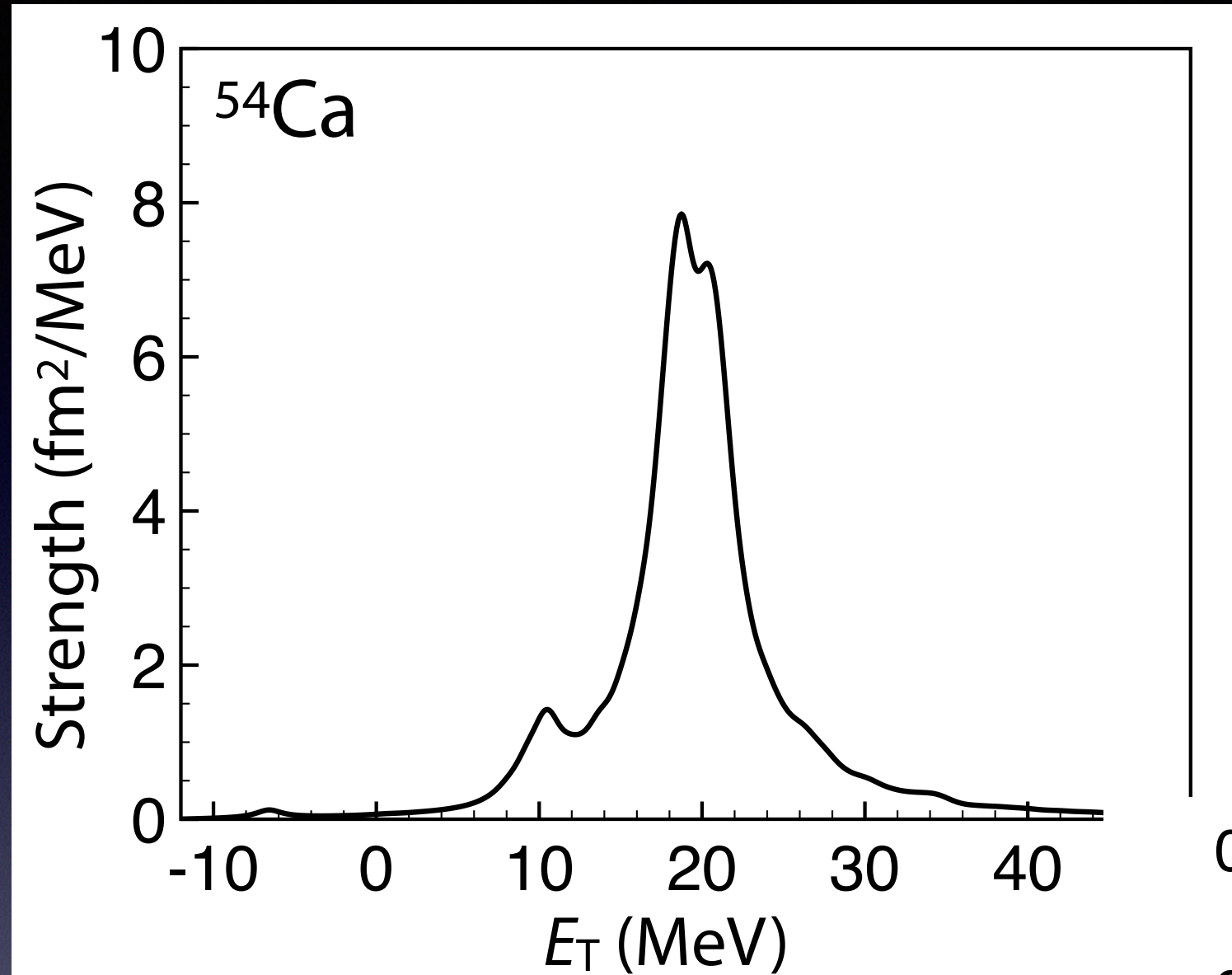


# Microscopic structure of the analog PDR





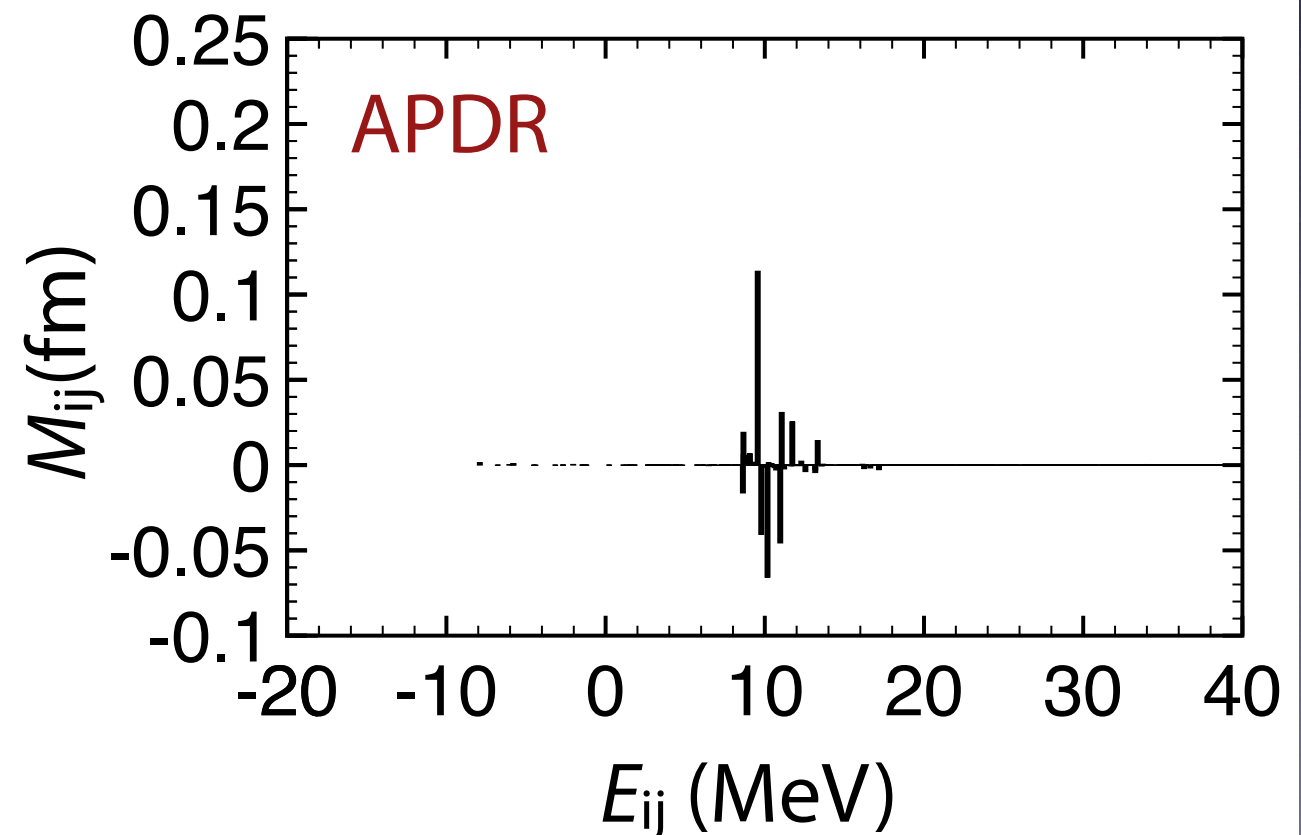
# Microscopic structure of the analog PDR



$$\text{strength} = |\langle \lambda | \hat{F} | 0 \rangle|^2$$

$$\langle \lambda | \hat{F} | 0 \rangle = \sum_{ij} (X_{ij} + Y_{ij}) F_{ij} = \sum_{ij} M_{ij}$$

NOT a single-particle excitation  
 superposition of 2qp excitations  
 $\sim 10$   
 NOT coherent for a dipole operator





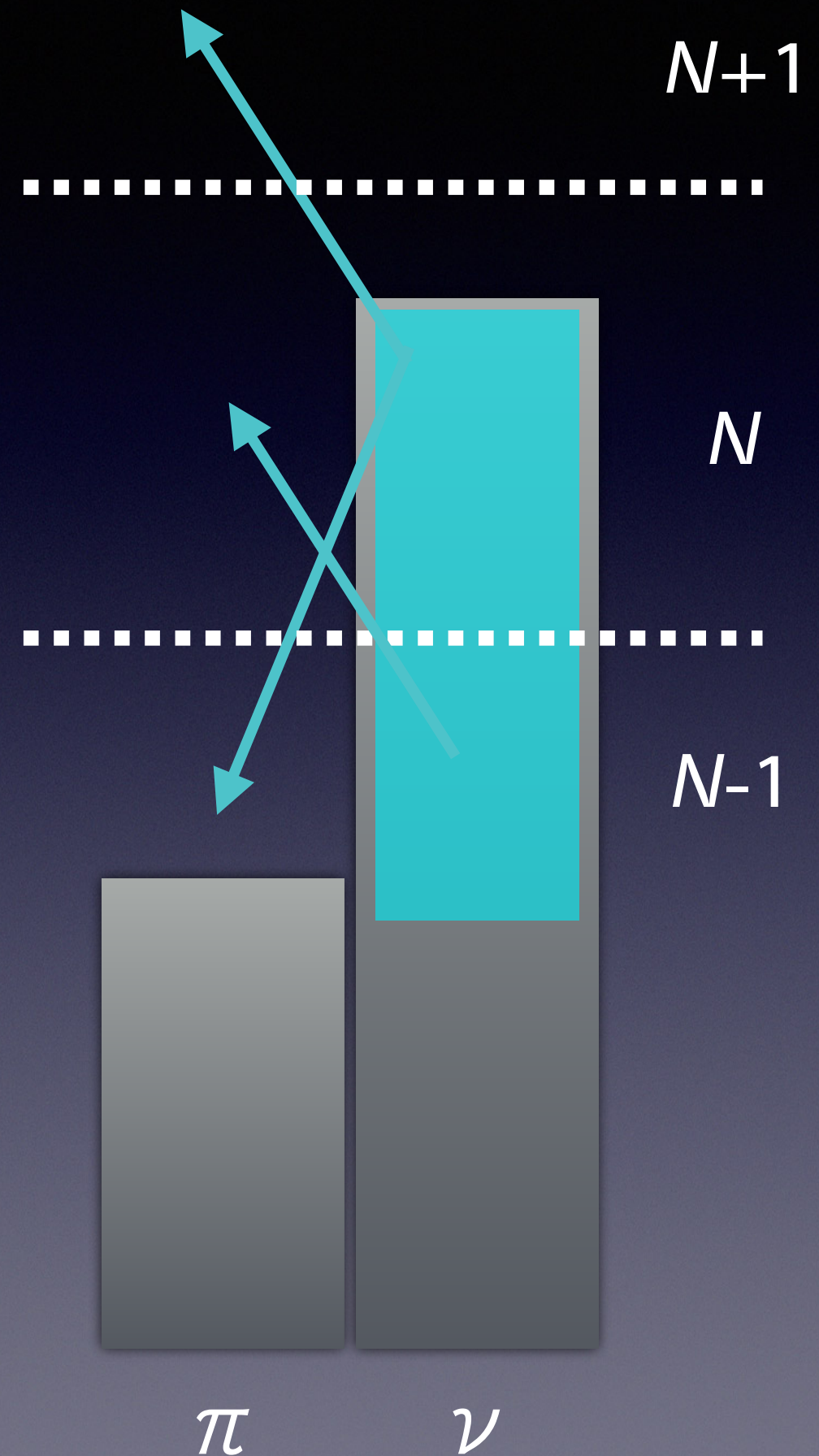
# Occurrence of the CE dipole states in n-rich nuclei

- ✓ cross-shell ( $N \rightarrow N-1$ ) excitation  
neutrons are weakly bound



protons are deeply bound:  
low-lying  $-1\hbar\omega$  excitation

- ✓ cross-shell ( $N \rightarrow N+1$ ) excitation  
protons are in the continuum:  
giant and pygmy resonances
- ✓ cross-shell ( $N-1 \rightarrow N$ ) excitation  
deeply-bound neutrons:  
giant resonance





# Summary

- ✓ low-lying dipole state appears uniquely in very n-rich nuclei
  - $1\hbar\omega$  excitation
- ✓ strong shell effect
  - steady selection rule due to the deeply-bound proton orbitals
  - single-particle type excitation
    - # of neutron hole states satisfying the selection rule is limited
- ✓ affects the half-life substantially
  - together with the axial-vector (spin-flip) dipole excitations
- ✓ emergence of analog PDR below the giant resonance peak
  - ✓ loosely-bound neutrons with low-angular momentum play an important role
  - ✓ destructive for a dipole operator, while several 2qp excitations are involved