

ν -nucleus reactions on ^{13}C and ^{16}O at supernova energies

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ν -detection

Scintillator (CH, ...), H₂O, Liquid-Ar, Fe

ν -¹²C, ν -¹³C, ν -¹⁶O, ν -⁵⁶Fe, ν -⁴⁰Ar

Cross sections for various γ and particle emission channels

Detection of SN ν and nucleosynthesis

ν -oscillation effects (MSW oscillations in SNe): dependence of charged-current reaction cross sections on ν mass hierarchy

ν -¹³C reactions

Suzuki, Balantekin, Kajino, and Chiba

J. Phys. G 46, 075103 (2019)

ν -¹⁶O reactions

Suzuki, Chiba, Yoshida, Takahashi, and Umeda,

Phys. Rev. C98, 034613 (2018)

Neutrino oscillations in ν -¹⁶O reactions

Nakazato, Suzuki, and Sakuda, PTEP 2018, 123E02 (2018)

● ν -nucleus reactions with new shell-model Hamiltonians

$\nu\text{-}^{12}\text{C}$, $\nu\text{-}^{13}\text{C}$: SFO (p-shell; space p-sd)

Suzuki, Fujimoto, Otsuka, PR C69, (2003),

- * important roles of tensor force → proper shell evolutions and change of magic numbers toward drip-lines

Otsuka, Suzuki, Fujimoto, Grawe, Akaishi, PRL 69 (2005)

- Spin responses of nuclei are quite well described.

GT strength in ^{12}C , ^{14}C ; $O = g_A \sigma t$

Mag. mom. of p-shell nuclei; $\mu = g_s s + g_\ell \ell$

- ν -nucleus reactions

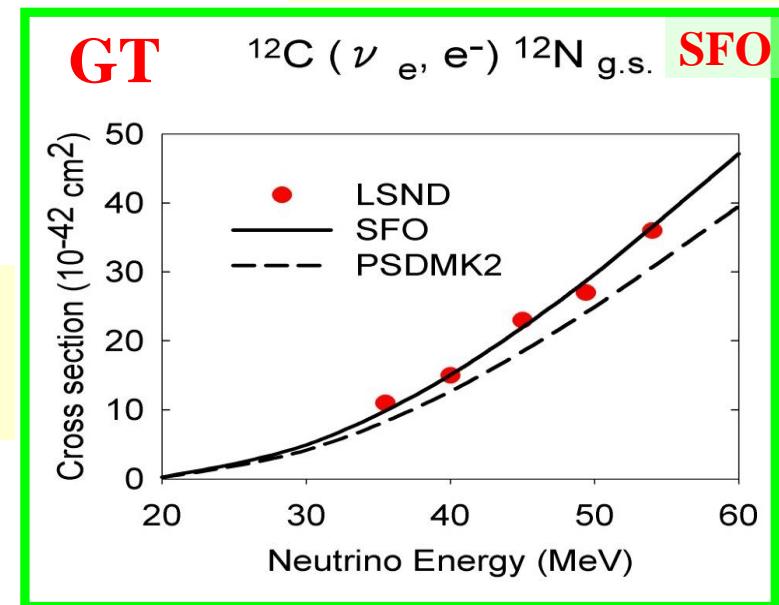
SFO: $g_A^{\text{eff}}/g_A = 0.95$

B(GT: ^{12}C)_cal = experiment

(ν, ν') , (ν_e, e^-) exclusive & inclusive
SFO reproduces DAR cross sections

Suzuki, Chiba, Yoshida, Kajino, Otsuka,
PR C74, 034307, (2006).

LSND: PR C55, 2078 (1997)



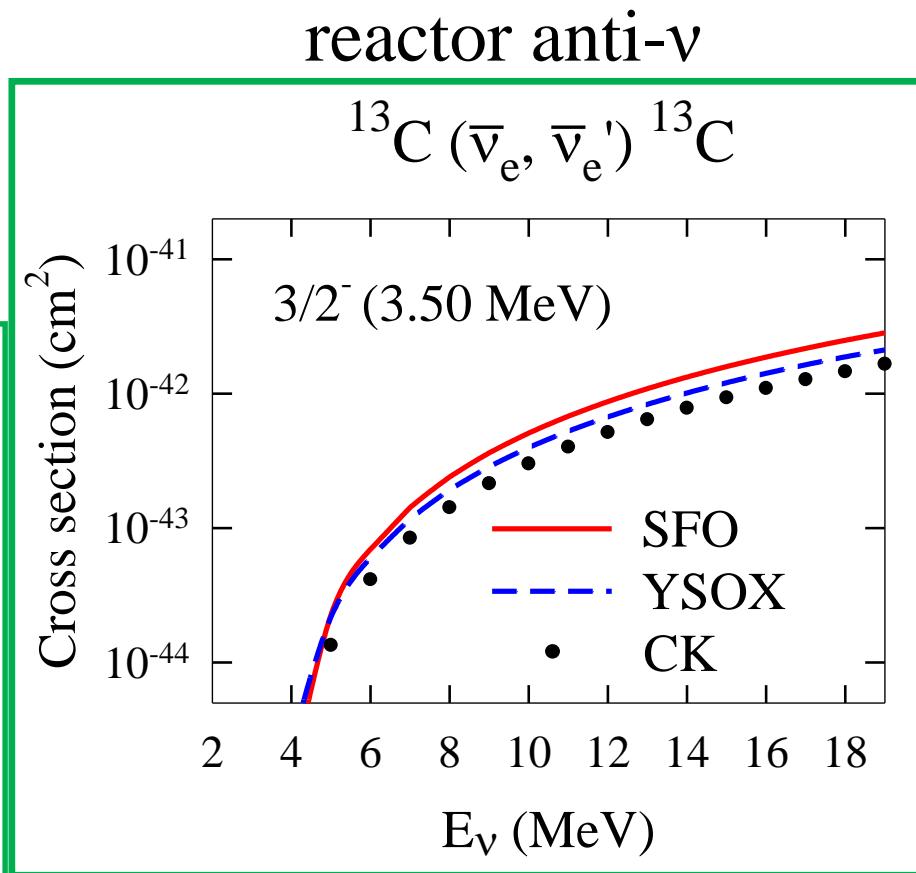
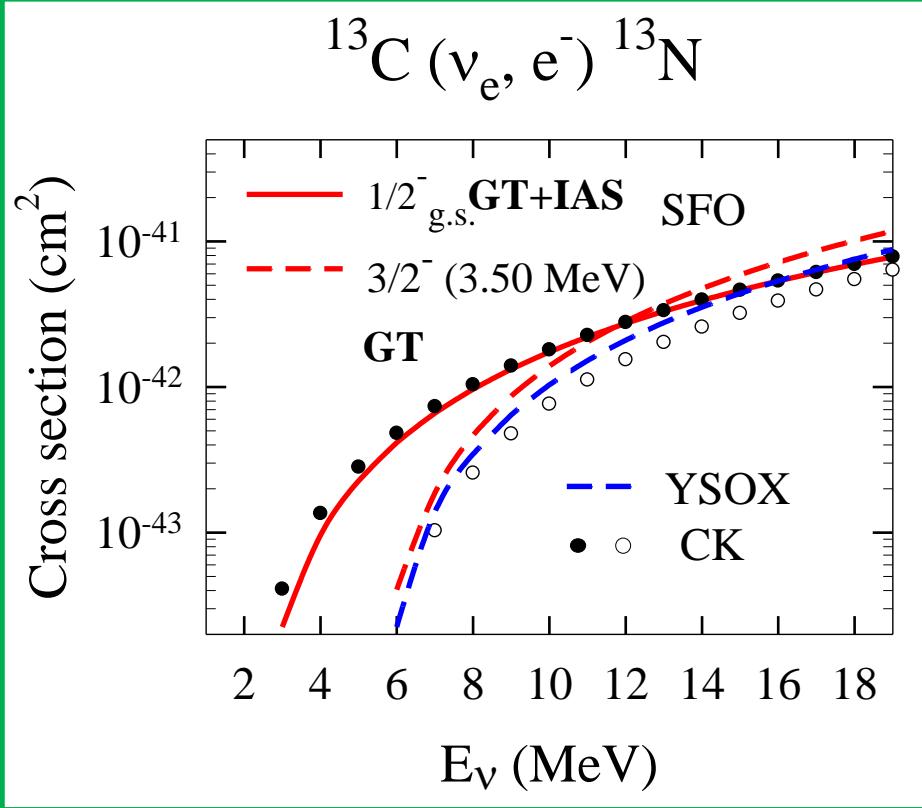
▪ ν -induced reactions on ^{13}C

^{13}C : attractive target for very low energy ν

$$E_\nu \leq 10\text{MeV} \quad E_\nu^{\text{th}}(^{12}\text{C}) \approx 13\text{MeV}$$

Natural isotope abundance = 1.07%

Detector for solar ν ($E < 15\text{MeV}$) and reactor anti- ν ($E < 8\text{ MeV}$)



$$g_A^{\text{eff}}/g_A = 0.95(\text{SFO}), 0.85(\text{YSOX}) \\ 0.69 (\text{CK})$$

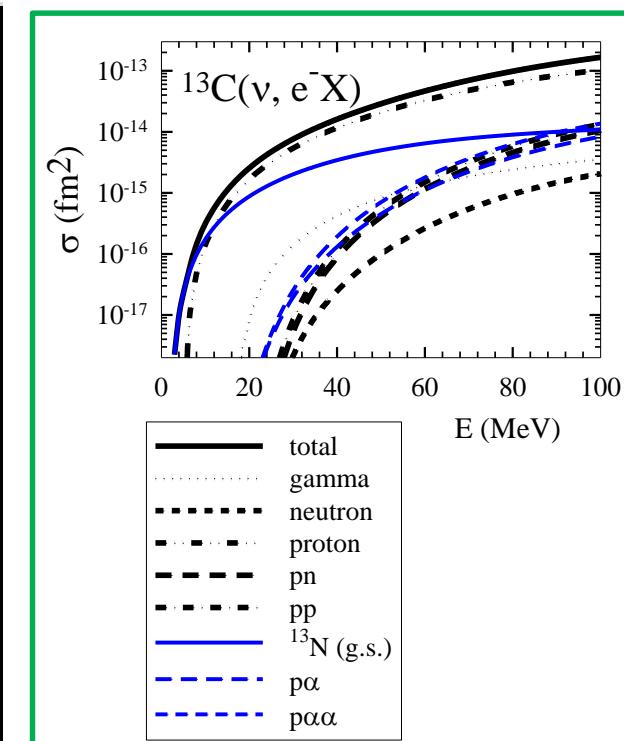
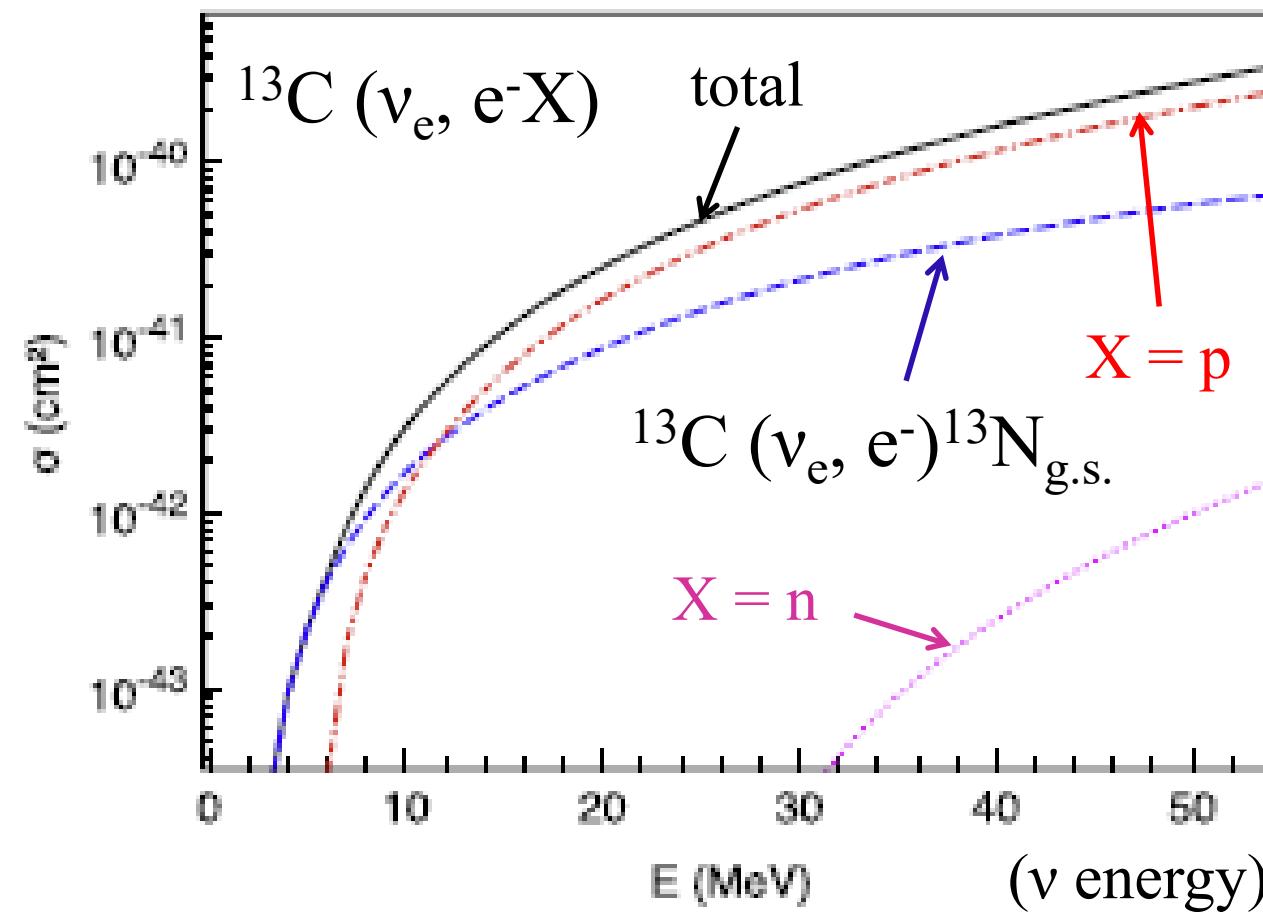
YSOX: Yuan, Suzuki, Otsuka et al.,

Charged-current cross sections at SN ν energies

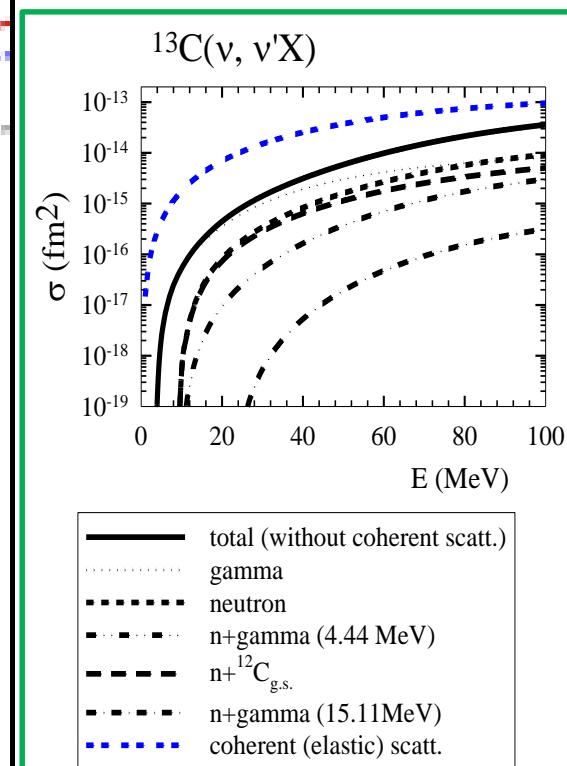
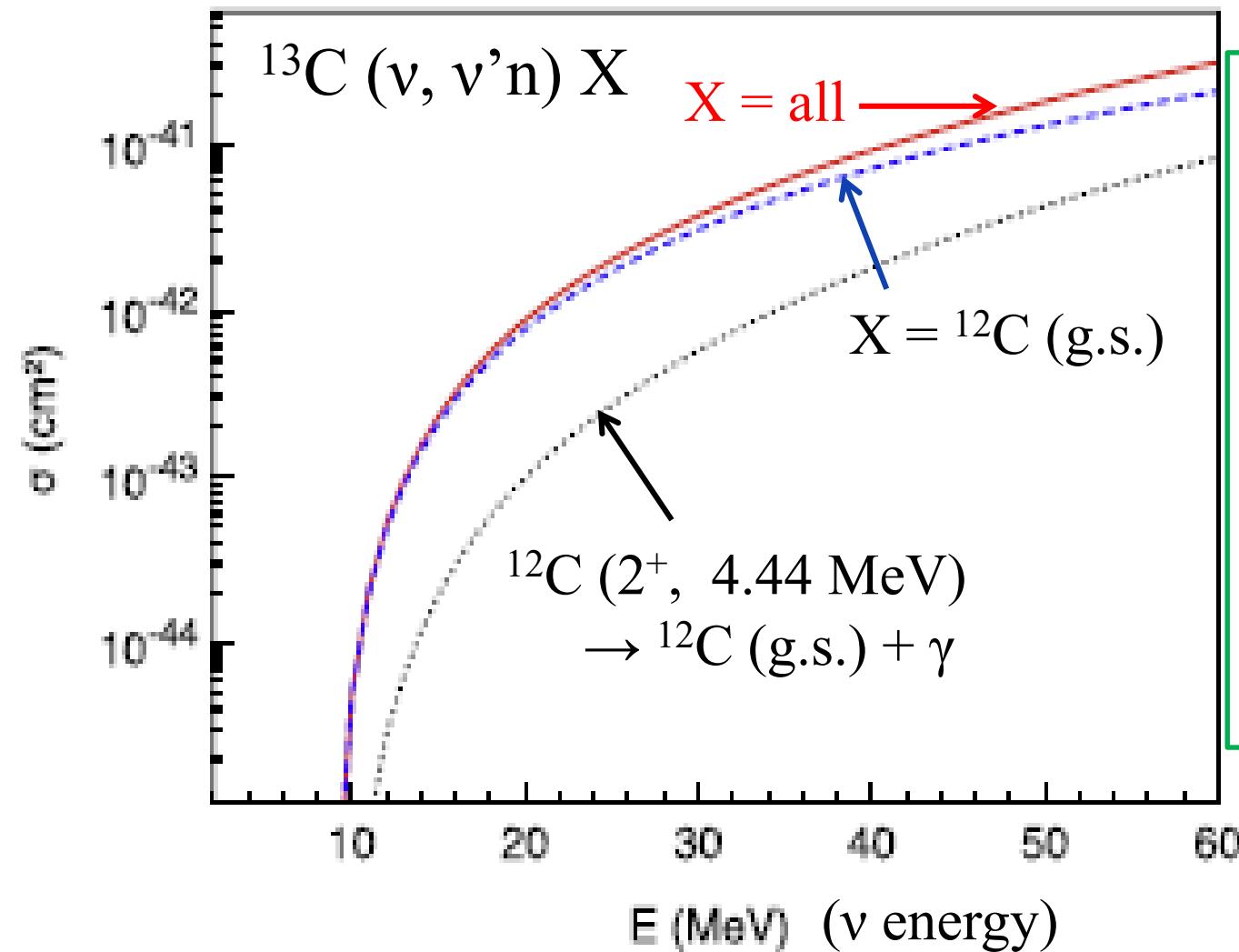
Hauser-Feshbach statistical model

Branching ratios for γ and particle emission channels (with multi-particle emission channels): γ , n, p, np (d), nn, pp, ^3H (nnp), ^3He (npp), α , αp , αn , αnn , αnp , αpp , ...

Isospin conservation is taken into account (S. Chiba)



Neutral-current neutron-emission cross sections



Particle physics origin of the 5 MeV bump in the reactor antineutrino spectrum?

PHYSICAL REVIEW D 99, 055045 (2019)

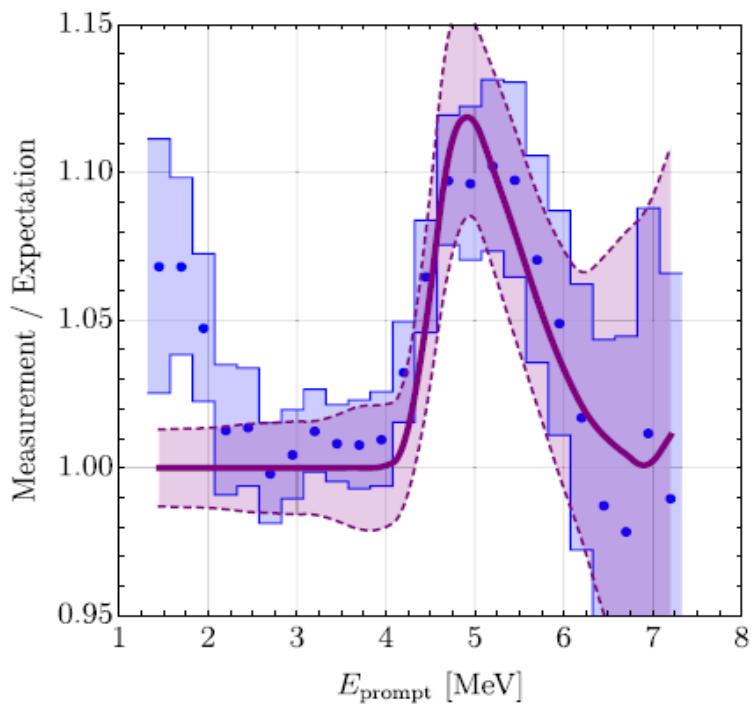
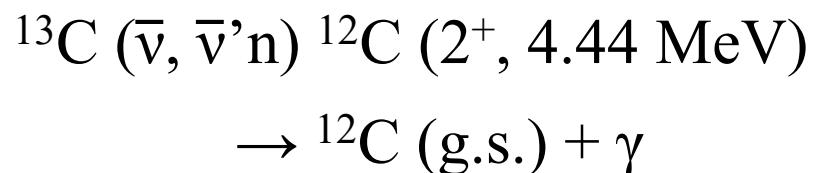
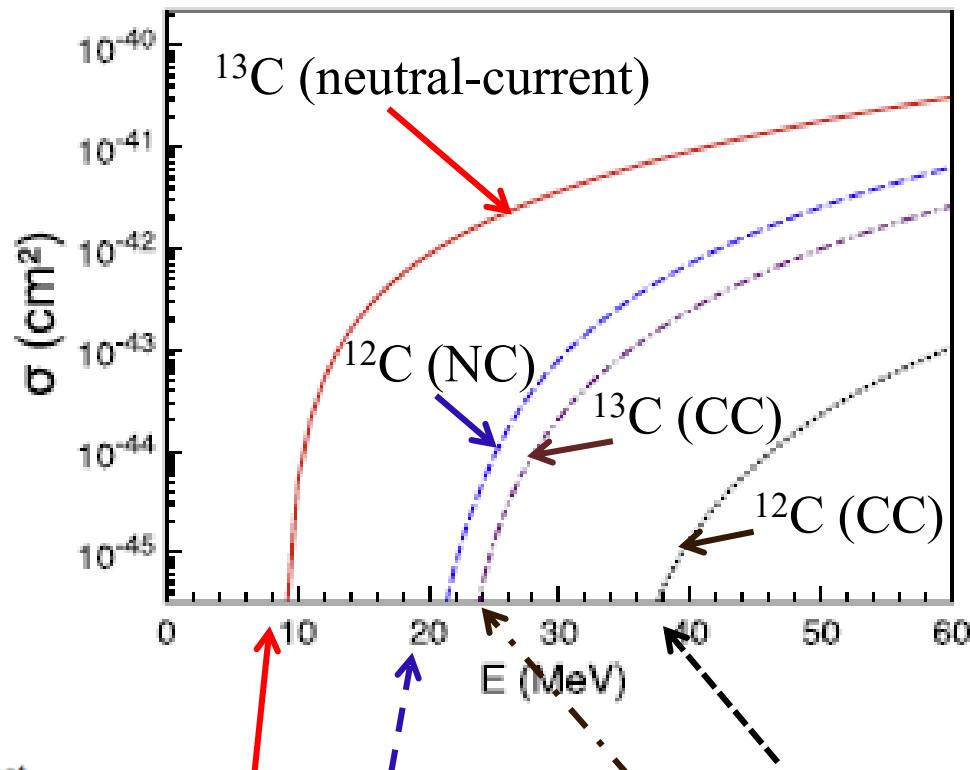


FIG. 1. The prompt energy spectrum corresponding to the best-fit point in Eq. (8). Only transitions to the first excited state of ^{12}C have been included. See text for details.



$E_{\text{th}} = 9.4 \text{ MeV}$ Reactor $\bar{\nu}$ with $E \sim 16 \text{ MeV}$ Fallot et al, PRL 109 (2012)

Neutron-emission cross sections for $\nu_e - ^{12}\text{C}$, ^{13}C reactions



$$E_{\text{th}} = 4.95, 18.72 \text{ MeV}, 22.28, 32.38 \text{ MeV}$$

The cross section for n emission with γ in the standard model is so small to make a bump in the reactor $\bar{\nu}$ spectrum.

Coherent (elastic) scattering on light target

Neutral current $A_\mu^S = V_\mu^S = 0$

$$J_\mu^{(0)} = A_\mu^3 + V_\mu^3 - 2 \sin^2 \theta_w J_\mu^\gamma$$

Vector part: $V_\mu^{(0)} = V_\mu^3 - 2 \sin^2 \theta_w J_\mu^\gamma$

C0: $(G_E^{IV} - 2 \sin^2 \theta_w G_E) \langle g.s. | j_0(qr) Y^{(0)} | g.s. \rangle$

$$\Leftrightarrow \frac{1}{2} G_E^p (1 - 4 \sin^2 \theta_w) \rho_p(r) - \frac{1}{2} G_E^n \rho_n(r) \quad (G_E^n \approx 0)$$

$$= -\frac{1}{2} G_E^p \{\rho_n(r) - 0.08 \rho_p(r)\} \quad (\sin^2 \theta_w = 0.23)$$

Probe of neutron density distribution

Patton, Engel, MacLaglin, Schunck, PRC 86, 024612 (2012)

$$\frac{d\sigma}{dT}(E, T) = \frac{G_F^2}{2\pi} M \left\{ 2 - \frac{2T}{T_{\max}} + \frac{T^2}{E^2} \right\} \frac{Q_w^2}{4} F^2(Q^2), \quad T_{\max} = 2E^2 / (2E + M)$$

T = recoil energy

$$Q_w = N - (1 - 4 \sin^2 \theta_w) Z$$

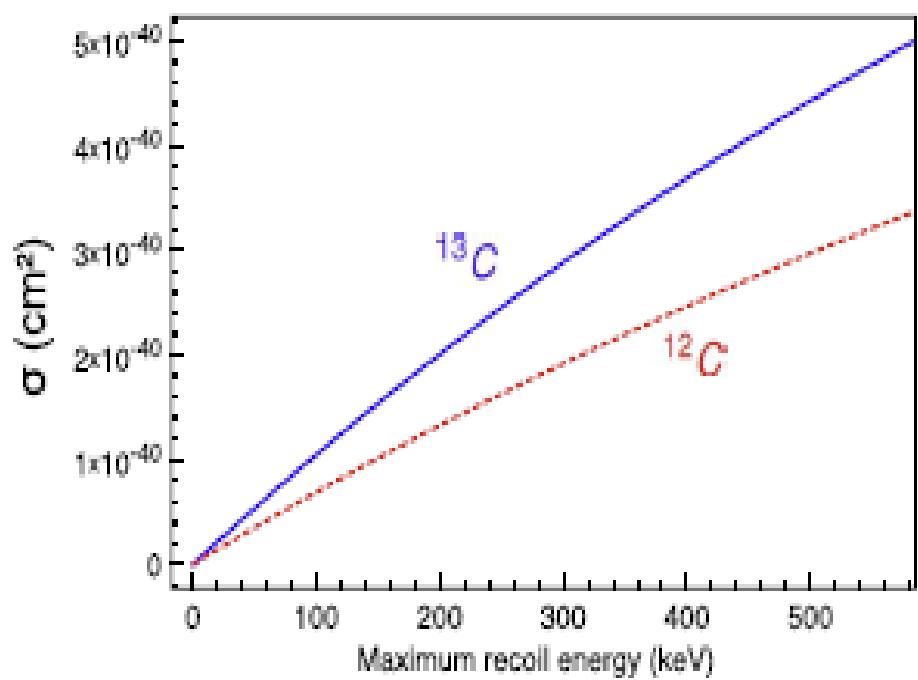
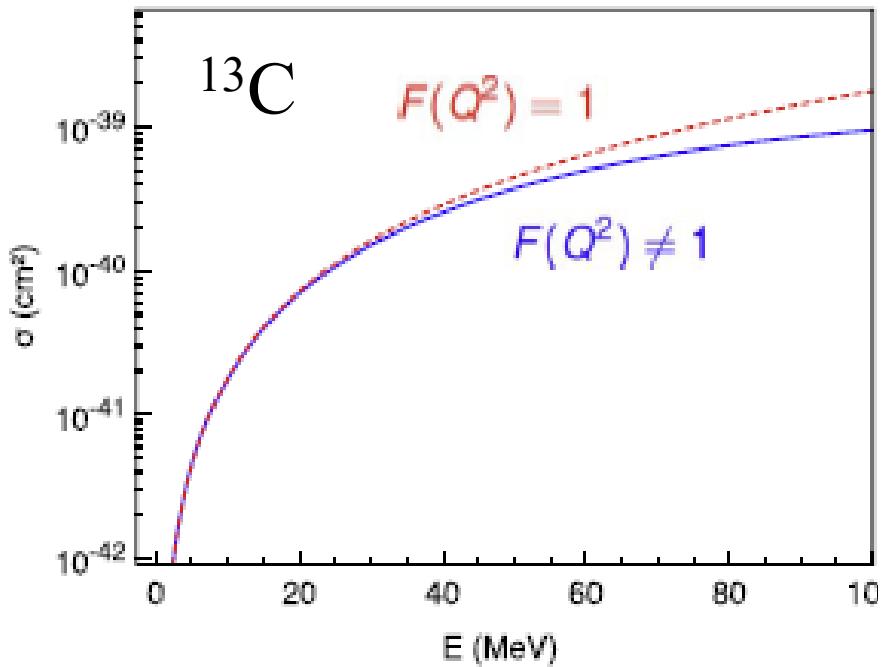
$$F(Q^2) = \{N F_n(Q^2) - (1 - 4 \sin^2 \theta_w) Z F_p(Q^2)\} / Q_w$$

$$Q^2 = 2MT + T^2$$

$$F_{n,p}(Q^2) = \int r^2 j_0(Qr) \rho_{n,p}(r) dr$$

$$\sigma(E) = \int_0^{T_{\max}} dT \frac{d\sigma}{dT}(E, T)$$

Nuclear effects and Isotope dependence in coherent scattering

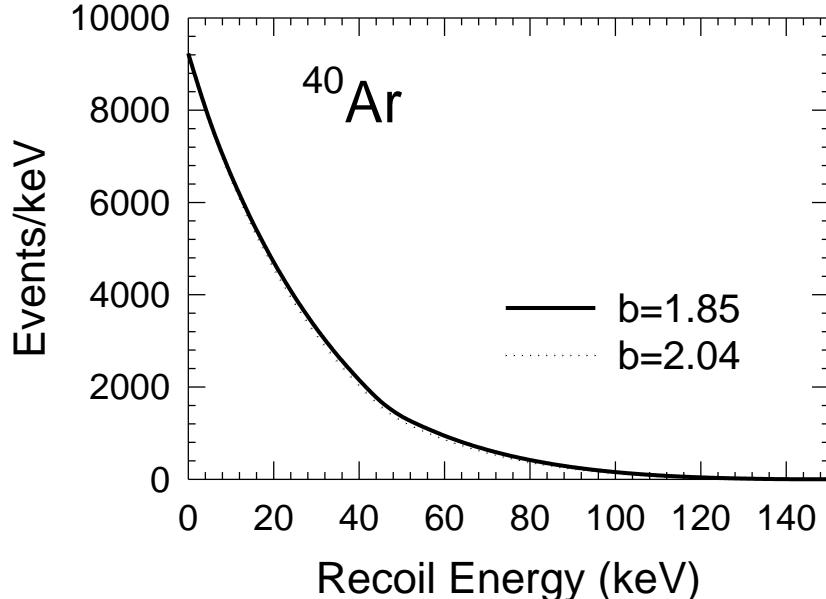
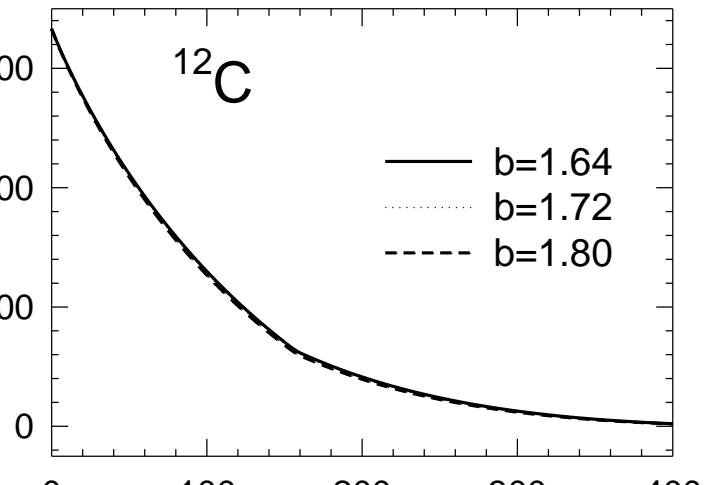


Events/keV - Recoil energy (keV)

DAR ν (3-flavors)

$\Phi = 3 \times 10^7 / \text{cm}^2/\text{s}$, 1 year, target=1 ton

Events/keV

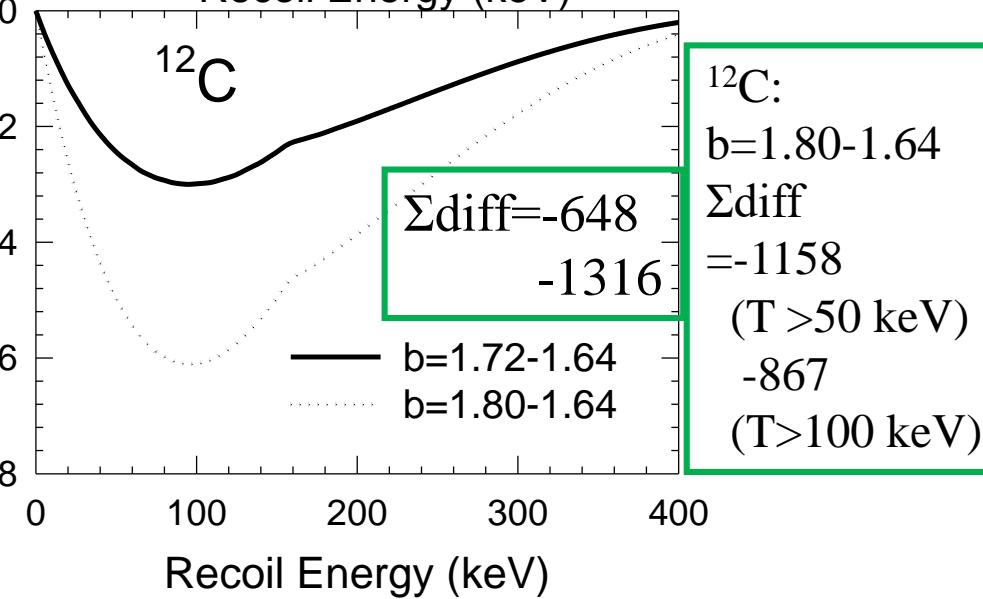


$$\Sigma_{\text{diff}} = -8770$$

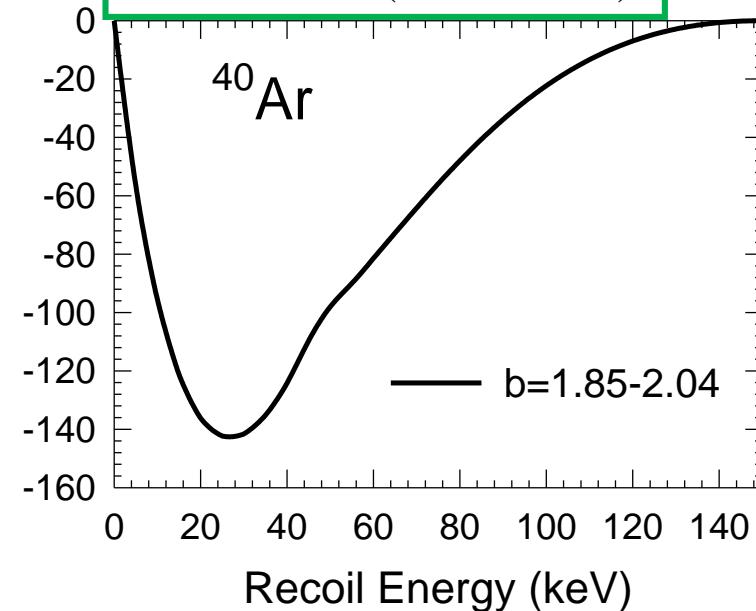
$$-2970 \text{ (T>50 keV)}$$

$$-287 \text{ (T>100 keV)}$$

Difference in events/keV



Difference in events/keV

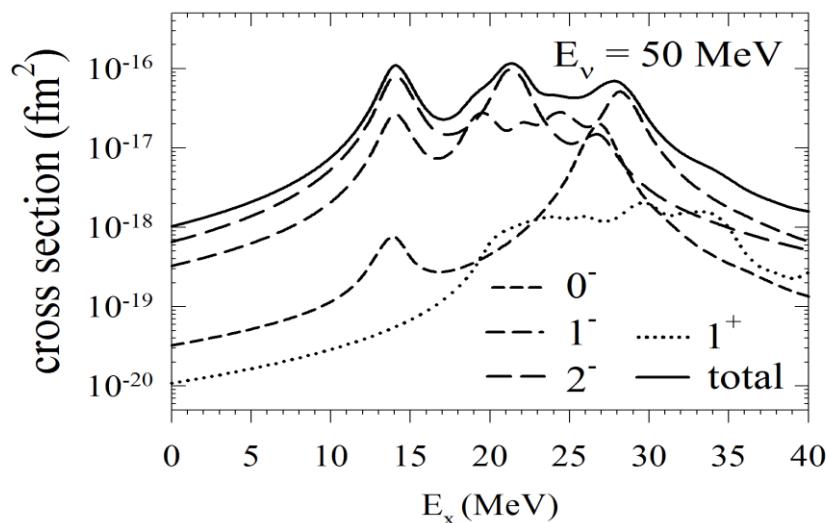
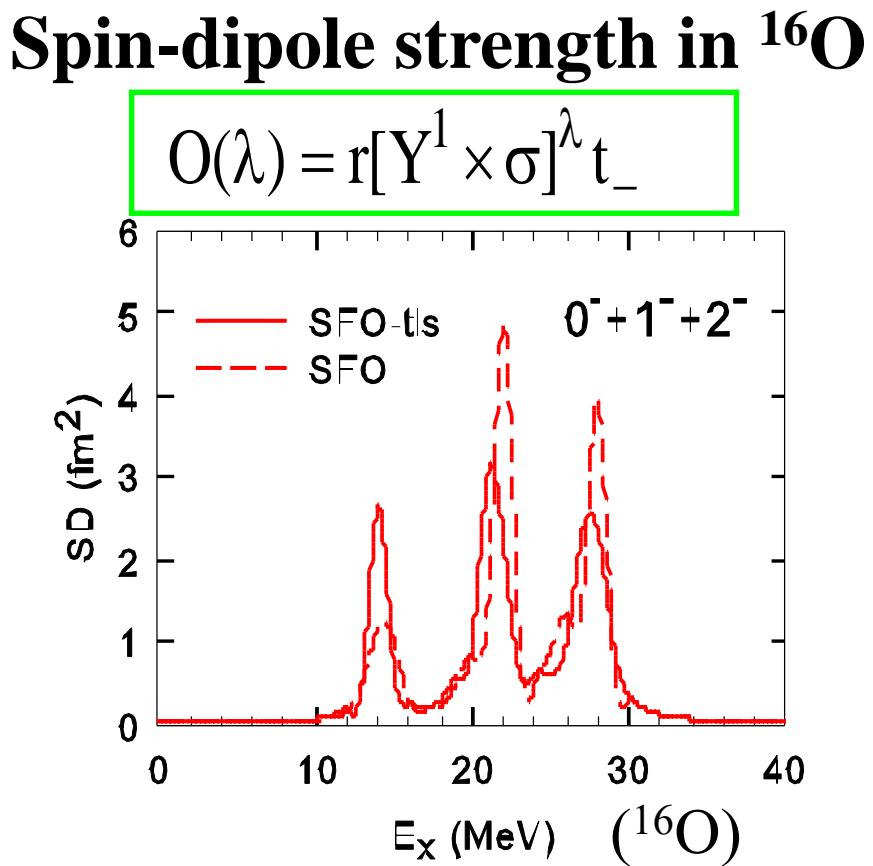
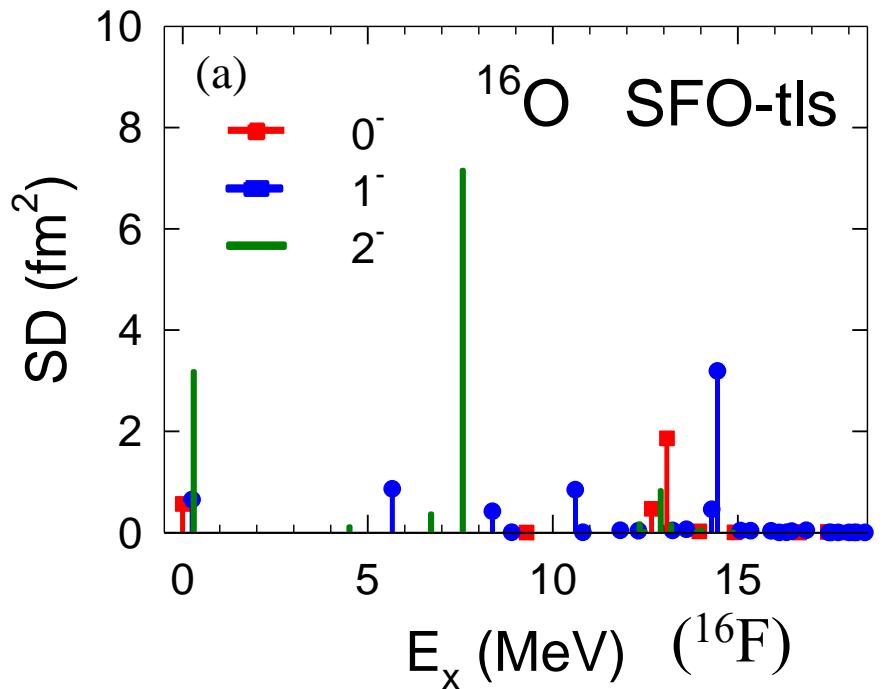


- ν -induced reactions on ^{16}O
- Modification of SFO \rightarrow SFO-tls
- Full inclusion of tensor force
- p-sd: tensor-> $\pi+\rho$
LS $\rightarrow \sigma+\rho+\omega$

$$V = V_C + V_T + V_{LS}$$

$$V_T = V_\pi + V_\rho$$

$$V_{LS} = V_{\sigma+\omega+\rho}$$



Spin-dipole sum

$$B(SD\lambda)_{\mp} = \frac{1}{2J_i + 1} \sum_f |\langle f \parallel S_{\mp}^{\lambda} \parallel i \rangle|^2 \quad S_{\mp,\mu}^{\lambda} = r [Y^1 \times \vec{\sigma}]_{\mu}^{\lambda} t_{\mp}$$

NEWS-rule: $S_{-}^{\lambda} - S_{+}^{\lambda} = \langle 0 | [\hat{S}_{-}^{\lambda}, \hat{S}_{+}^{\lambda}] | 0 \rangle = \frac{2\lambda + 1}{4\pi} (N\langle r^2 \rangle_n - Z\langle r^2 \rangle_p)$

Energy-weighted sum

$$EWS_{\pm}^{\lambda} = \sum |\langle \lambda, \mu | S_{\pm,\mu}^{\lambda} | 0 \rangle|^2 (E_{\lambda} - E_0),$$

$$EWS^{\lambda} = \overset{\mu}{EWS_{-}^{\lambda}} + EWS_{+}^{\lambda} = \frac{1}{2} \langle 0 | [S_{-}^{\lambda\dagger}, [H, S_{-}^{\lambda}]] + [[S_{+}^{\lambda\dagger}, H], S_{+}^{\lambda}] | 0 \rangle$$

kinetic energy term (K) for $H = \frac{p^2}{2m}$

= 0 for LS-closed core

$$EWS_K^{\lambda} = \frac{3}{4\pi} (2\lambda + 1) \frac{\hbar^2}{2m} A \left[1 + \frac{f_{\lambda}}{3A} \right] \langle 0 | \sum_i \vec{\sigma}_i \cdot \vec{l}_i | 0 \rangle$$

: $f_{\lambda} = 2, 1$ and -1 for $\lambda^{\pi} = 0^{-}, 1^{-}$ and 2^{-} , respectively.

One-body spin-orbit potential term $V_{LS} = -\xi \sum_i \vec{l}_i \cdot \vec{\sigma}_i$

$$EWS_{LS}^{\lambda} = \frac{3}{4\pi} (2\lambda + 1) \frac{f_{\lambda}}{3} \xi \langle 0 | \sum_i (r_i^2 + g_{\lambda} r_i^2 \vec{l}_i \cdot \vec{\sigma}_i) | 0 \rangle$$

$g_{\lambda} = 1$ for $\lambda^{\pi} = 0^{-}, 1^{-}$ and $g_{\lambda} = -7/5$ for $\lambda^{\pi} = 2^{-}$.

For $N=Z$, $EWS_{-}^{\lambda} = EWS_{+}^{\lambda}$, and $EWS^2/5 < EWS^1/3 < EWS^0$

Spin-dipole sum

$$S_\lambda(SD) = \sum_{\mu} | \langle \lambda, \mu | S_{-, \mu}^\lambda | 0 \rangle |^2 = \begin{cases} \frac{3}{4\pi} 4b^2 = 2.99 \text{fm}^2 & \lambda^\pi = 0^- \\ \frac{3}{4\pi} 12b^2 = 8.98 \text{fm}^2 & \lambda^\pi = 1^- \\ \frac{3}{4\pi} 20b^2 = 14.96 \text{fm}^2 & \lambda^\pi = 2^- \end{cases}$$

p → sd
∞ 2λ+1

<i>EWS</i> ^λ	0^-	1^-	2^-	
K+LS	56.4	144.1	155.9	MeV·fm^2
SFO-tls (/K+LS)	73.0 (1.29)	173.2 (1.20)	246.5 (1.58)	
SFO (/K+LS)	76.1 (1.35)	175.0 (1.21)	258.2 (1.66)	

$\bar{E}_\lambda = EWS_\lambda^{\lambda}/NEWS_\lambda^{\lambda}$,	0^-	1^-	2^-	
SFO-tls	24.5	25.1	20.1	MeV
SFO	25.8	25.2	21.0	

Tensor interaction: attractive for 0-, 2-, & repulsive for 1-

$$V_T(r) = F(r) \{ [\sigma_1 \times \sigma_2]^{(2)} \times [r^2 Y_2(\hat{r})]^{(2)} \}^{(0)},$$

$$V_T(r) = F(r) \sum_{\lambda} \frac{\sqrt{4\pi}}{6} \left(\frac{10}{3} \right)^{1/2} \begin{Bmatrix} -2\sqrt{5} \\ \sqrt{15} \\ -1 \end{Bmatrix} \times \{ r_1 [\sigma_1 \times Y_1(\hat{r}_1)]^{(\lambda)} \}$$

$$\times r_2 [\sigma_2 \times Y_1(\hat{r}_2)]^{(\lambda)} \}^{(0)}, \quad \text{for } \lambda = \begin{Bmatrix} 0^- \\ 1^- \\ 2^- \end{Bmatrix}.$$

Splitting of the strength comes from one-body LS term and two-body tensor interaction

● μ -capture rate on ^{16}O and the quenching factor

The muon capture rate for $^{16}\text{O} (\mu, \nu_\mu) ^{16}\text{N}$ from the 1s Bohr atomic orbit

$$\omega_\mu = \frac{2G^2}{1 + \nu/M_T} |\phi_{1s}|^2 \frac{1}{2J_i + 1} \left(\sum_{J=0}^{\infty} |< J_f \parallel M_J - L_J \parallel J_i >|^2 + |< J_f \parallel T_J^{el} - T_J^{mag} \parallel J_i >|^2 \right),$$

$$|\phi_{1s}|^2 = \frac{R}{\pi} \left(\frac{m_\mu M_T}{m_\mu + M_T} Z \alpha \right)^3 \quad R = 0.79$$

Induced pseudo-scalar current $F_P(q_\mu^2) = \frac{2M_N}{q_\mu^2 + m_\pi^2} F_A(q_\mu^2)$ Goldberger-Treiman

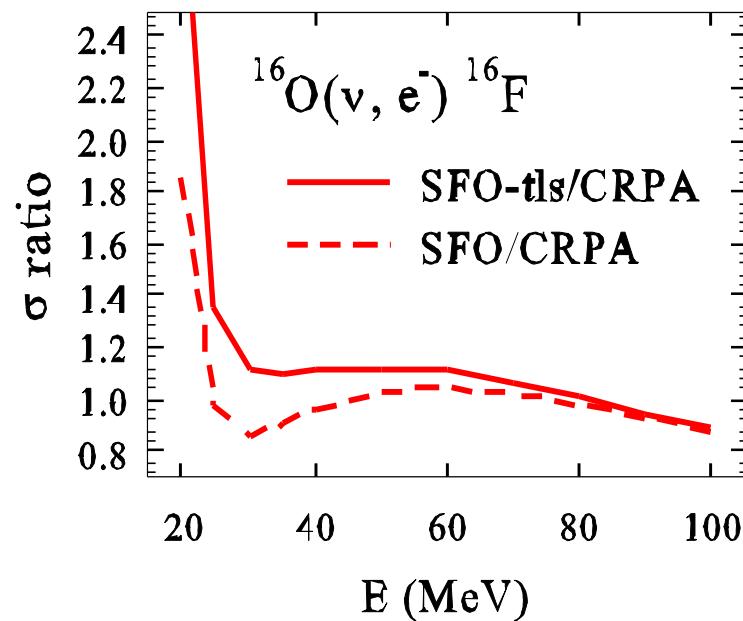
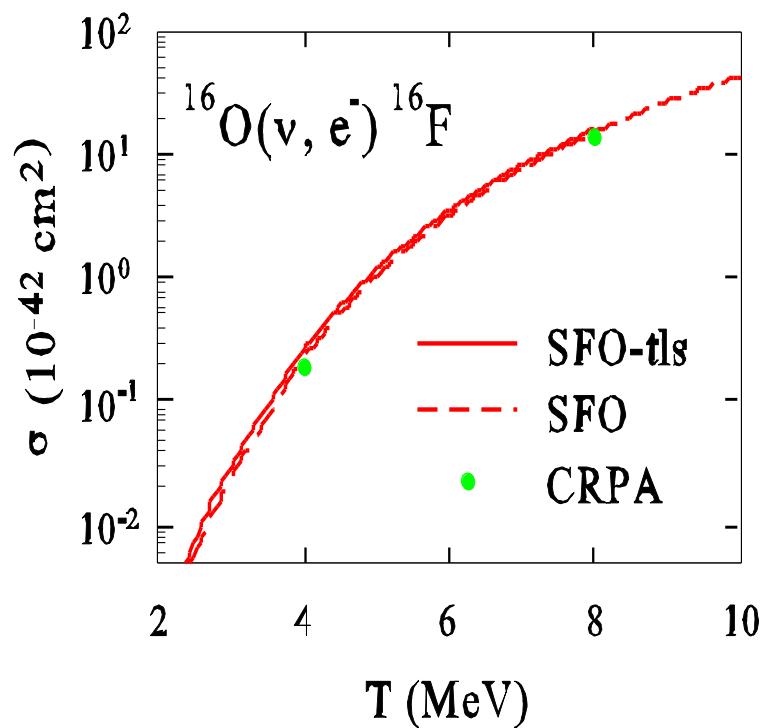
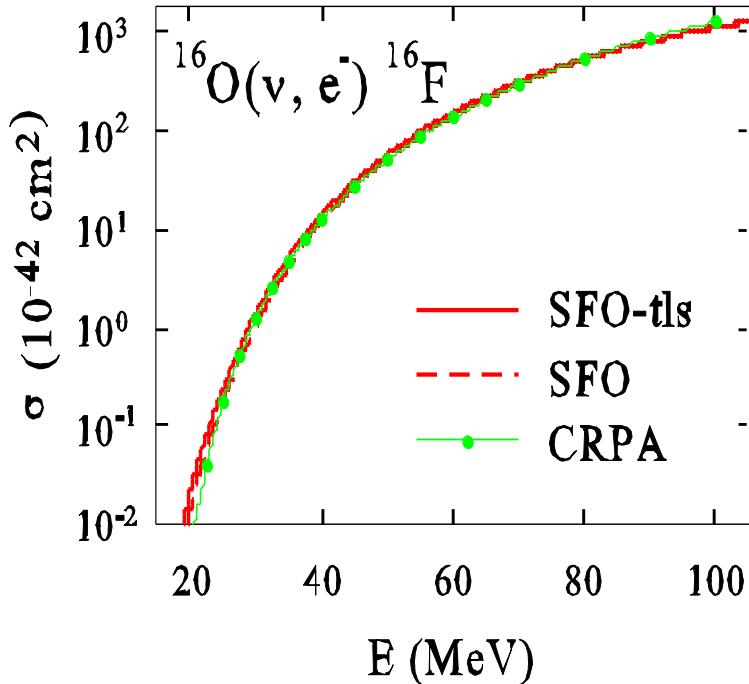
$$f = g_A^{eff}/g_A = 0.95$$

$$\text{SFO} \quad 10.21 \times 10^4 \text{ s}^{-1} \quad (\text{SFO/exp} = 0.995)$$

$$\text{SFO-tls, } 11.20 \times 10^4 \text{ s}^{-1} \quad (\text{SFO-tls/exp} = 1.092)$$

$$\text{Exp.} \quad 10.26 \times 10^4 \text{ s}^{-1}$$

$$-2M_N F_A = \sqrt{2} g_\pi F_\pi$$

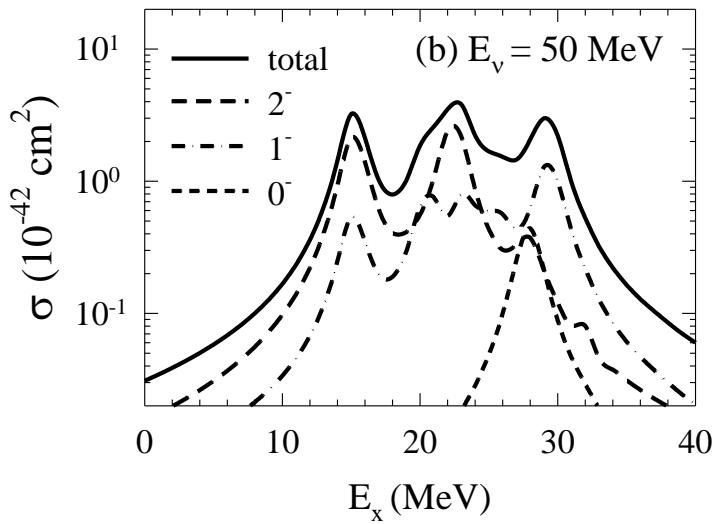
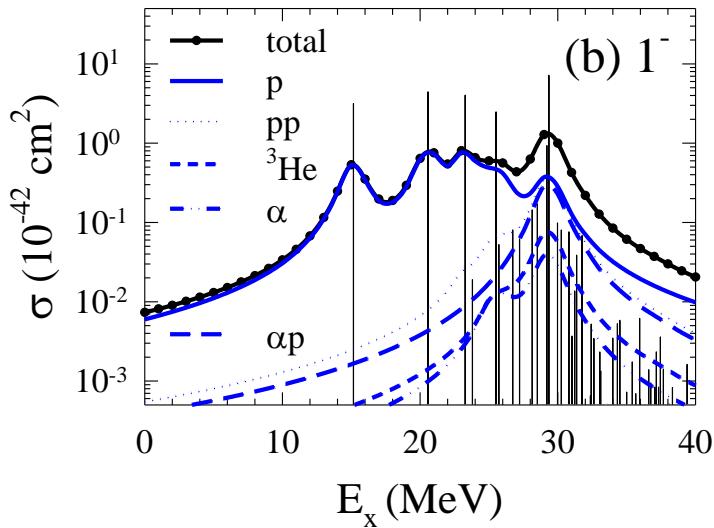
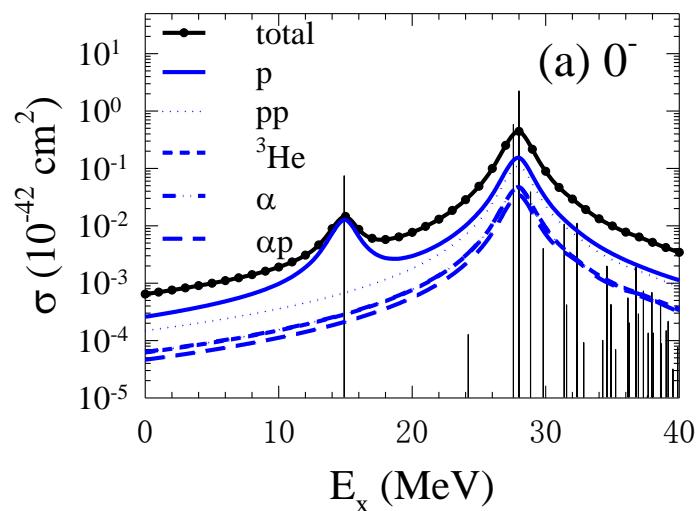
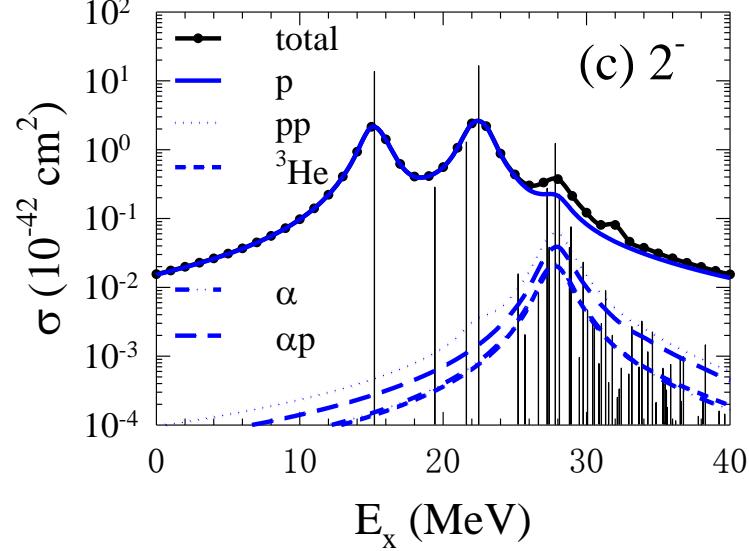


$T = \text{temperature of supernova } v$

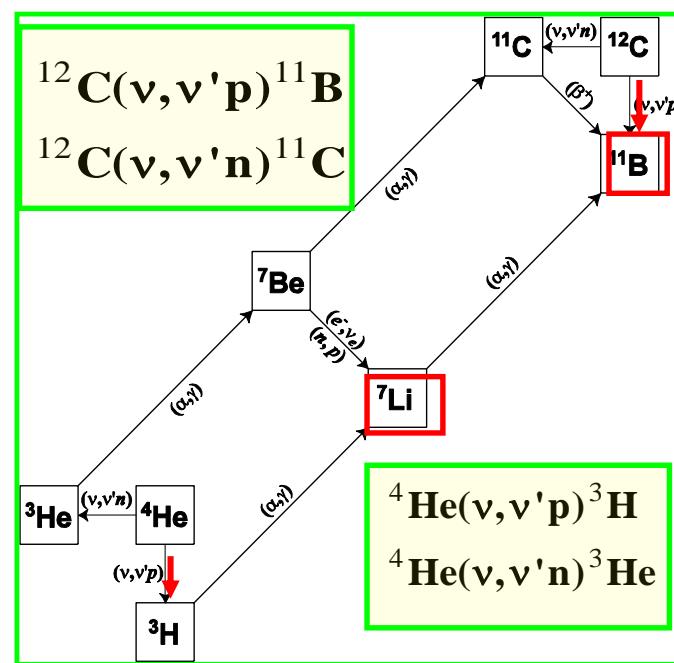
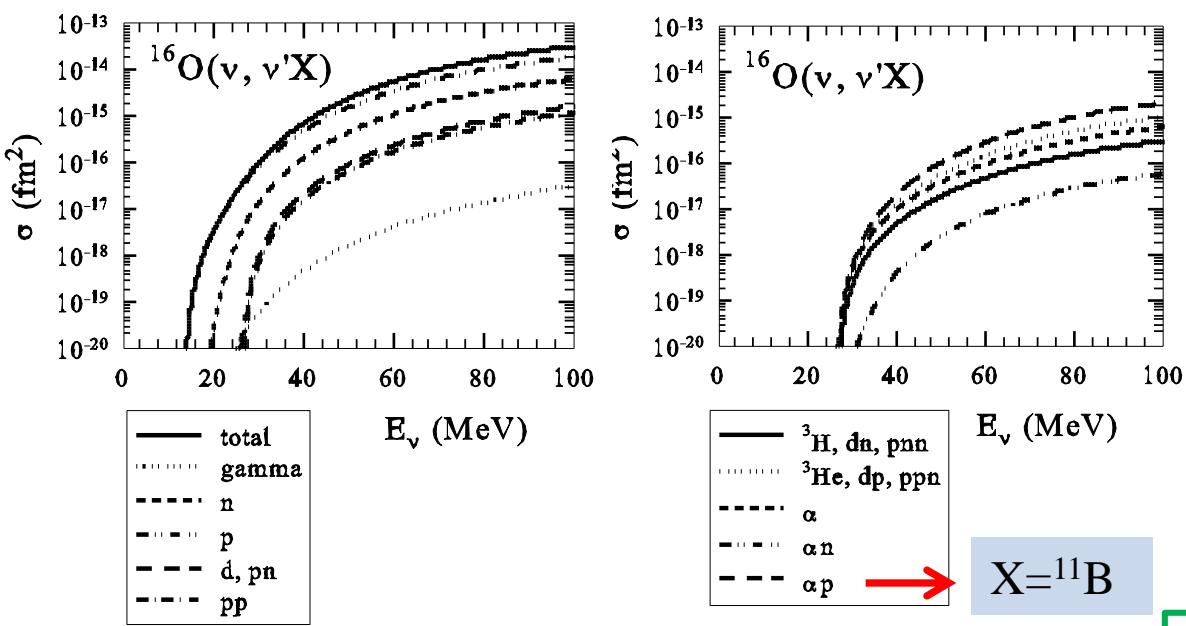
T	$\sigma(\text{SFO-tls})/\sigma(\text{CRPA}):$
4	1.41
8	1.17

$$g_A^{\text{eff}}/g_A = 0.95$$

CRPA: Kolbe, Langanke & Vogel, PR D66 (2002)
 cf. CRPA: Jachowicz et al., PR C65 (2002)
 RPA/QRPA: Lazauskas and Volpe, NP A792 (2007)

$^{16}\text{O}(\nu, e^-)^{16}\text{F}$  $^{16}\text{O}(\nu, e^- X) \quad E_\nu = 50 \text{ MeV}$  $^{16}\text{O}(\nu, e^- X) \quad E_\nu = 50 \text{ MeV}$  $^{16}\text{O}(\nu, e^- X) \quad E_\nu = 50 \text{ MeV}$ 

Synthesis of ^{11}B and ^{11}C in SNe



$$\frac{\sigma(^{16}\text{O}(\nu, \nu'\alpha p)^{11}\text{B})}{\sigma(^{12}\text{C}(\nu, \nu'p)^{11}\text{B})} \approx 10\%$$

Case1: previous branches used in ^{16}O (γ , n, p, α -emissions) and HW92 cross sections

Case2: previous branches, and new cross sections

Case3: multi-particle branches and new cross sections

Production yields of ^{11}B and ^{11}C (10^{-7}M_\odot)

yields	$15M_\odot$			$20M_\odot$		
	Case 1	Case 2	Case 3	Case 1	Case 2	Case 3
$M(^{11}\text{B})$	2.94	2.92	3.13	6.77	6.58	7.66
$M(^{11}\text{C})$	2.80	2.71	3.20	9.33	8.91	9.64
$M(^{11}\text{B}+^{11}\text{C})$	5.74	5.62	6.33	16.10	15.49	17.29

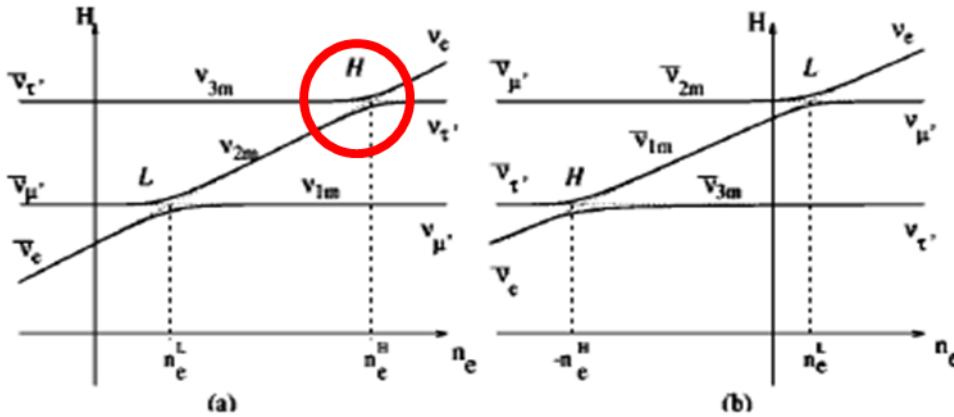
T. Yoshida

ν oscillation effects → ν mass hierarchy

MSW ν oscillations

Normal hierarchy

Inverted hierarchy



Normal – hierarchy : $\nu_\mu, \nu_\tau \rightarrow \nu_e$

Inverted – hierarchy : $\bar{\nu}_\mu, \bar{\nu}_\tau \rightarrow \bar{\nu}_e$

$$N(\nu_e) = P * N^0(\nu_e) + (1-P) * N^0(\nu_x)$$

$$N(\text{anti-}\nu_e) = P' * N^0(\text{anti-}\nu_e) + (1-P') * N^0(\nu_x)$$

Normal hierarchy: $(P, P') = (0, 0.68)$

Inverted hierarchy: $(P, P') = (0.32, 0); \sin^2 \theta_{12} = 0.32$

Dighe and Smirnov, PR D62, 033007 (2000)

Resonance condition

$$\rho Y_e = N_e = \frac{\Delta}{2\sqrt{2}EG_F} \cos 2\theta$$

$$= 6.55 \times 10^6 \left(\frac{\Delta m_{ij}^2}{1 \text{ eV}^2} \right) \left(\frac{1 \text{ MeV}}{E_\nu} \right) \cos 2\theta_{ij} \text{ g} \cdot \text{cm}^{-3}$$

H – resonance: θ_{13}

$\rho Y_e = 300 - 3000 \text{ g} \cdot \text{cm}^{-3}$ He/C layer

L – resonance: θ_{12}

$\rho Y_e = 4 - 40 \text{ g} \cdot \text{cm}^{-3}$

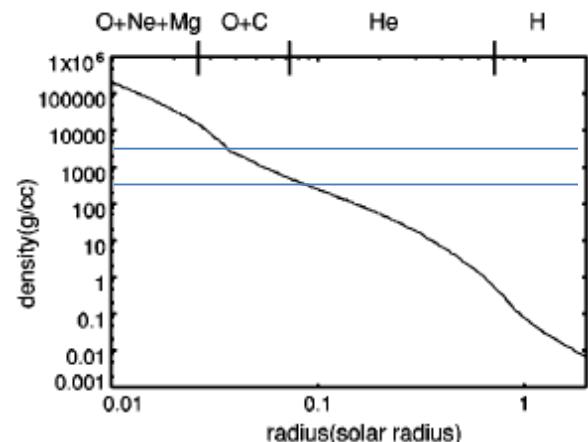
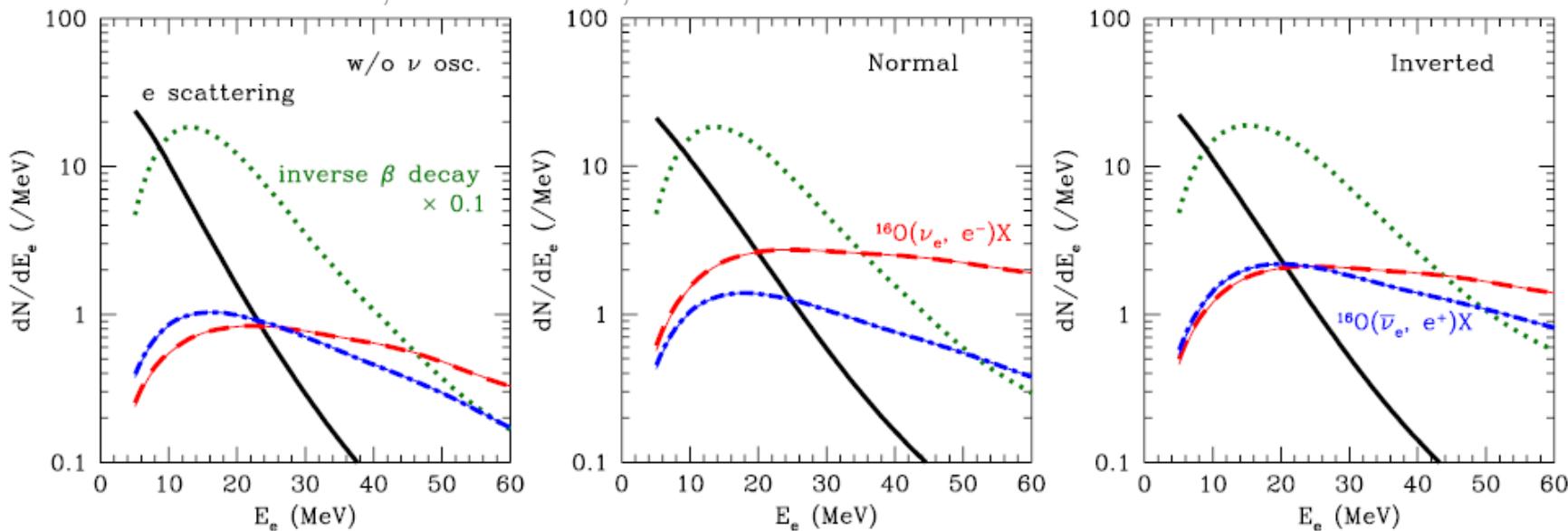


FIG. 3. Density profile of the presupernova star model used in the paper [20]. The progenitor mass is set to be $15 M_\odot$.

Charged current scattering off ^{16}O nucleus as a detection channel of supernova neutrinos

Ken'ichiro Nakazato¹, Toshio Suzuki², and Makoto Sakuda³

PTEP 2018, 123E02 82018)



$(M, Z) = (20M_{\odot}, 0.02)$ Z = metalicity

$\langle E_{\nu_e} \rangle = 9.32 \text{ MeV}$, $\langle E_{\bar{\nu}_e} \rangle = 11.1 \text{ MeV}$, $\langle E_{\nu_X} \rangle = 11.9 \text{ MeV}$

Expected event numbers

Nakazato et al., ApJ. Suppl. 205, 2 (2013)

reaction	ordinary supernova		
	no osc.	normal	inverted
$^{16}\text{O}(\nu_e, e^-)\text{X}$	41	178	134
$^{16}\text{O}(\bar{\nu}_e, e^+)\text{X}$	36	58	103
electron scattering	140	157	156
inverse β -decay	3199	3534	4242
total	3416	3927	4635

10 kpc, Super-K (32.8 kton)

Table 6 Expected event numbers with a threshold energy of $E_e = 5$ MeV for the models in Table 5.

reaction	black hole formation		
	no osc.	normal	inverted
$^{16}\text{O}(\nu_e, e^-)\text{X}$	2482	2352	2393
$^{16}\text{O}(\bar{\nu}_e, e^+)\text{X}$	1349	1255	1055
electron scattering	514	320	351
inverse β -decay	17525	14879	9255
total	21870	18806	13054

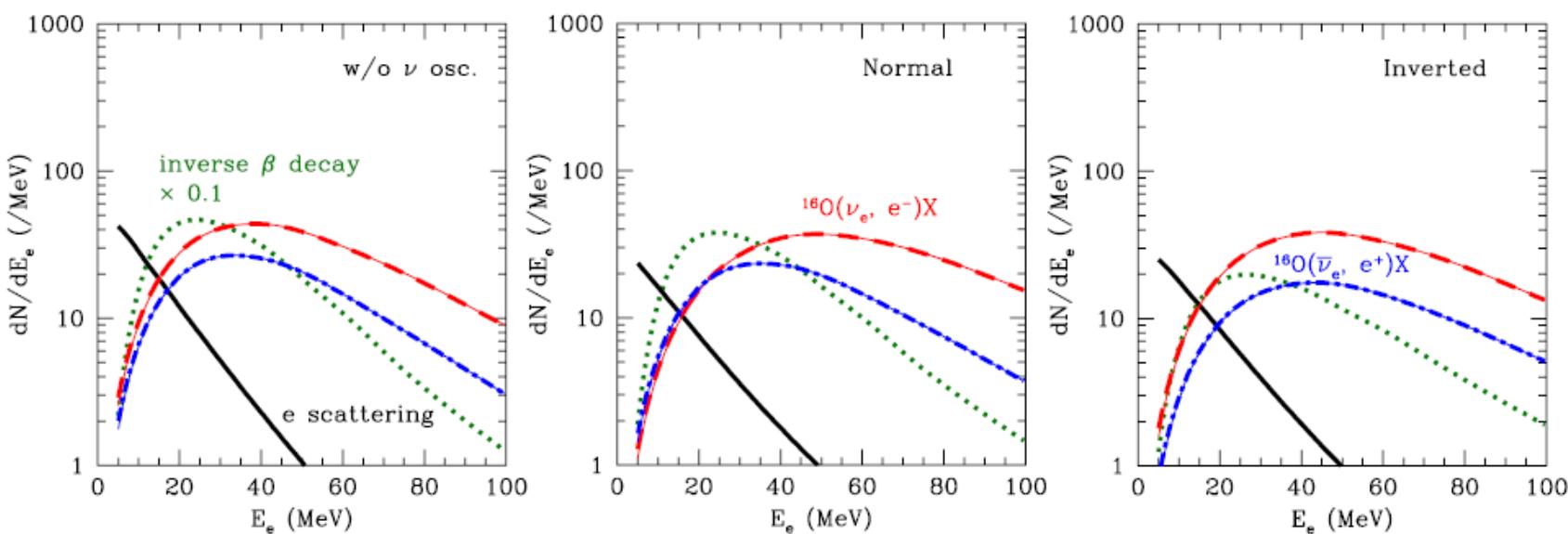


Fig. 5 Same as Fig. 4 but for the model with $(M, Z) = (30M_\odot, 0.004)$, which corresponds to a black-hole-forming collapse.

Summary

1.
 - ν - ^{12}C GT + SD shell-model with SFO
Coherent scattering
 - ν - ^{13}C GT + SD, n-emission channel, coherent scatt.
 - ν - ^{16}O SD shell-model with SFO-tls
 - Partial cross sections for particle and γ emission channels with Hauser-Feshbach statistical model
 - Synthesis of ^{11}B : $^{12}\text{C}(\nu, \nu' p) ^{11}\text{B}$, $^{16}\text{O}(\nu, \nu' \alpha p) ^{11}\text{B}$
 ^{11}C : $^{12}\text{C}(\nu, e^- p) ^{11}\text{C}$, $^{16}\text{O}(\nu, e^- \alpha p) ^{11}\text{C}$
2. MSW ν oscillation effects
Mass hierarchy dependence:
Cross sections of $^{16}\text{O}(\nu, e^-) X$ and $^{16}\text{O}(\bar{\nu}, e^+) X$ induced by SN ν

Collaborators

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Backups

Effects of collective ν oscillation

- Splitting (swapping) of ν spectrum occurs for inverted (normal) hierarchy for ν , and for normal (inverted) hierarchy for anti- ν .

Bimodal instability: Raffelt et al., PPNP 64 (2010)

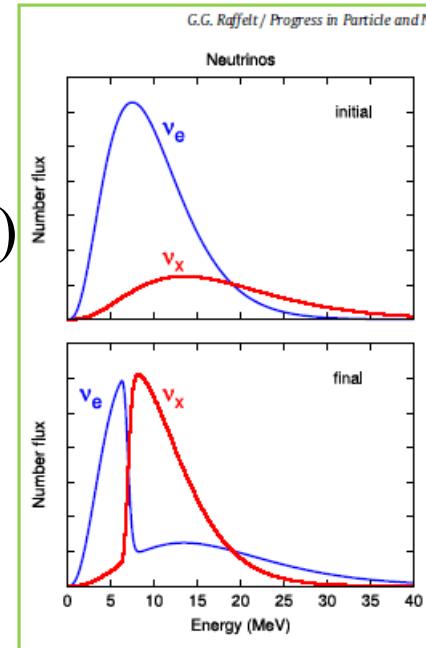
ν :	Collective	MSW	Collect.+MSW
normal	×	○	○
inverted	○	×	○

- MAA: Multi-azimuthal-angle instability
Splitting also occurs for normal (inverted) hierarchy for ν (anti- ν); $N(\nu_e) > N(\bar{\nu}_e)$

Raffelt et al., PRL111, 091101 (2011)

Chakraborty and Mirizzi, PRD 90, 033004 (2014)

ν :	Collective	MSW	Collect.+MSW
normal	○	○	×
inverted	○	×	○



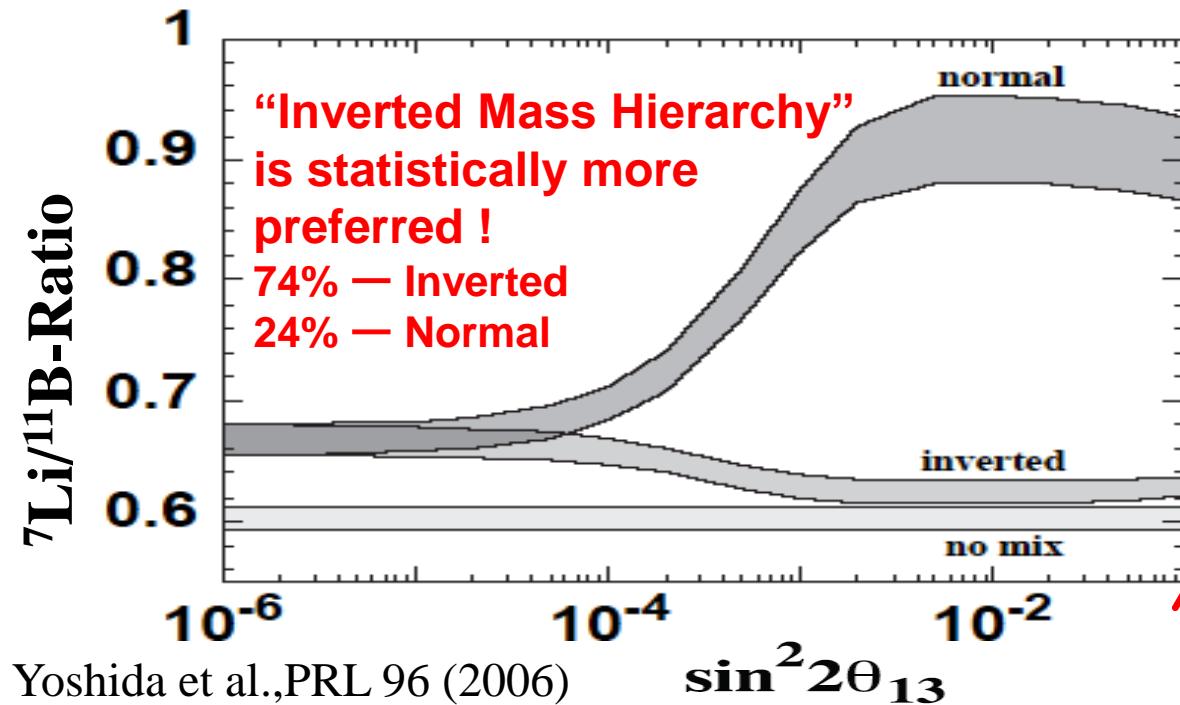
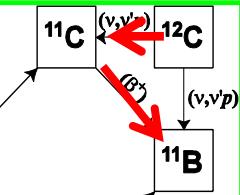
MSW ν oscillations

Normal – hierarchy : $\nu_\mu, \nu_\tau \rightarrow \nu_e$

Increase in the rates



in the He/C layer



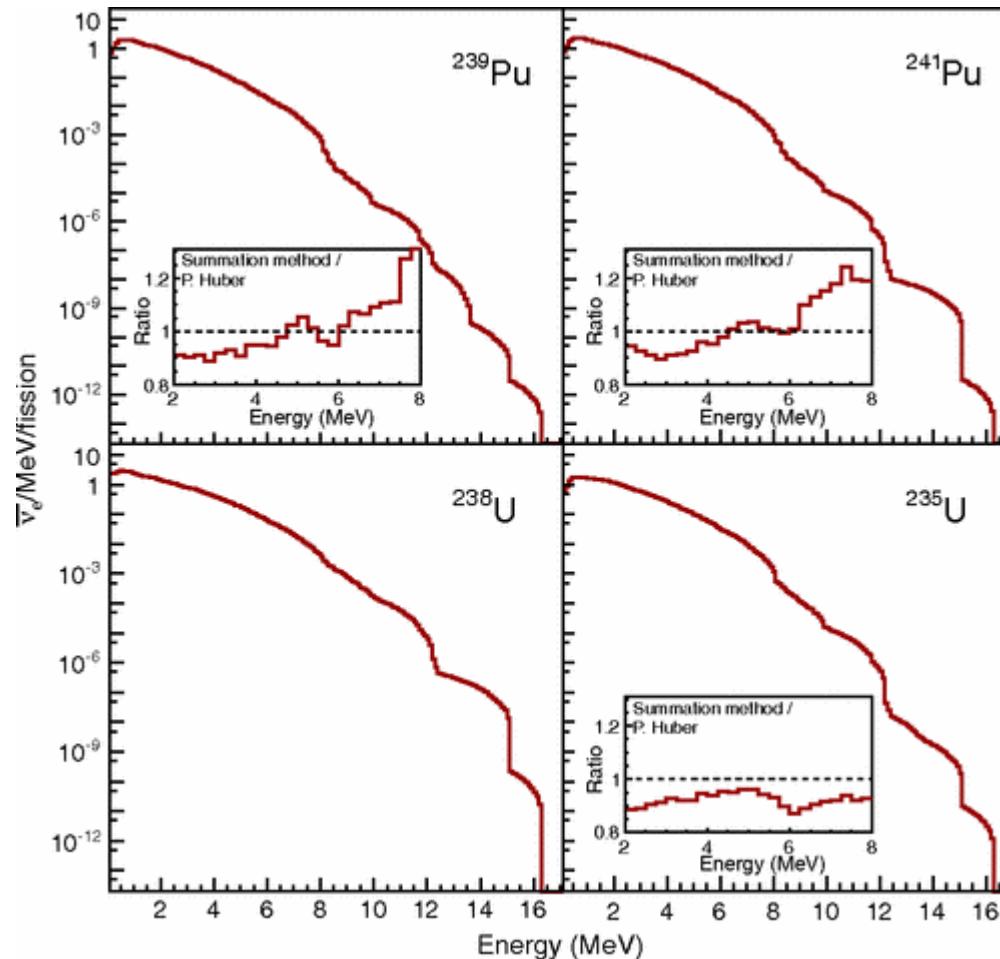
- T2K, MINOS (2011)
 - Double CHOOZ,
Daya Bay, RENO (2012)
- $\sin^2 2\theta_{13} = 0.1$

First Detection of ${}^7\text{Li}/{}^{11}\text{B}$ in SN-grains in Murchison Meteorite
• W. Fujiya, P. Hoppe, & U. Ott, ApJ 730, L7 (2011).

Bayesian analysis:
Mathews, Kajino, Aoki and Fujiya,
Phys. Rev. D85,105023 (2012).

For MAA instability case:
 ${}^7\text{Li}/{}^{11}\text{B} \rightarrow$ normal hierarchy (?)

New Antineutrino Energy Spectra Predictions from the Summation of Beta Decay Branches of the Fission Products
M. Fallot, S. Cormon, M. Estienne, A. Algora, V. M. Bui, A. Cucoanes, M. Elnimr, L. Giot, D. Jordan, J. Martino, A. Onillon, A. Porta, G. Pronost, A. Remoto, J. L. Taín, F. Yermia, and A.-A. Zakari-Issoufou
Phys. Rev. Lett. 109, 202504 – Published 13 November 2012

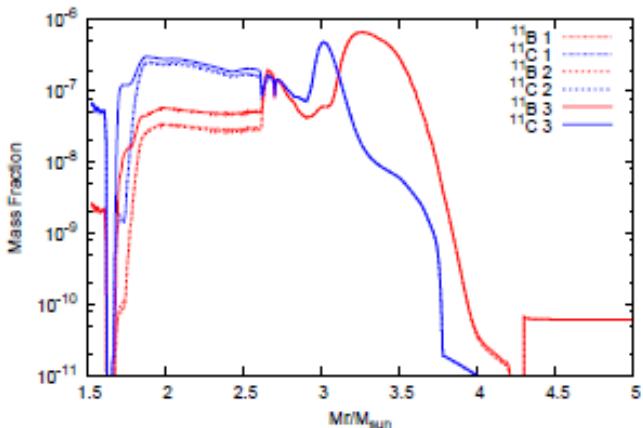
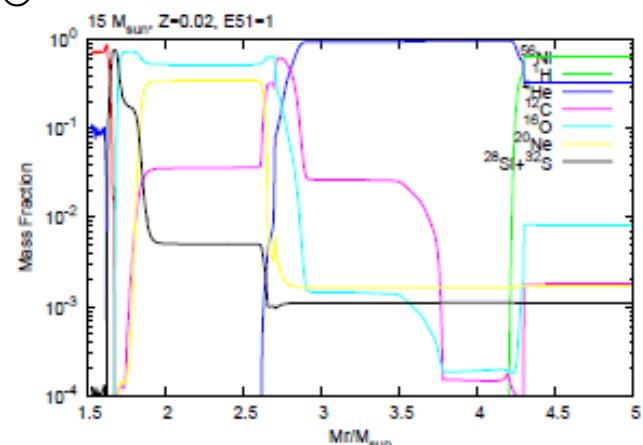


Production yields of ^{11}B and ^{11}C (10^{-7}M_\odot)

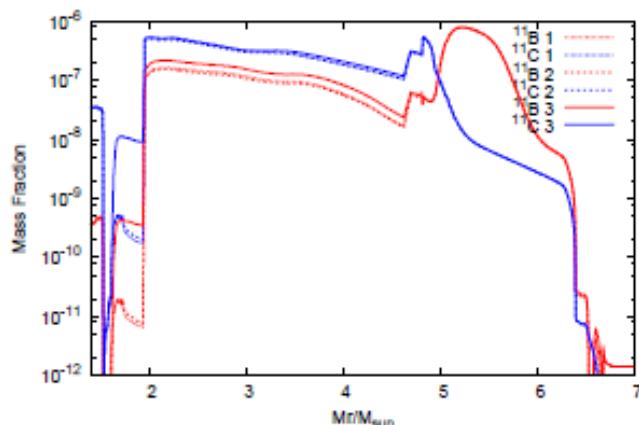
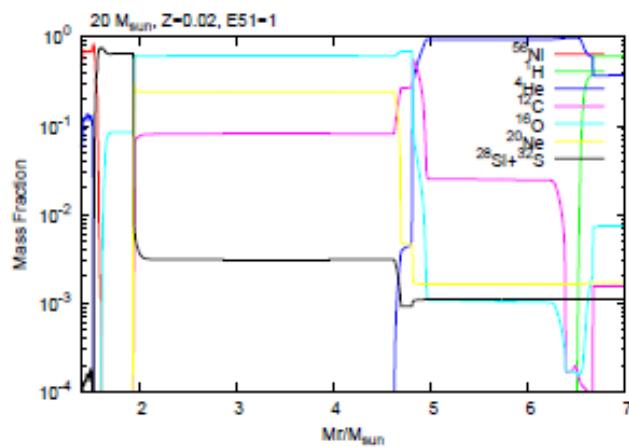
核種生成量	15 M_\odot モデル			20 M_\odot モデル		
	Case 1	Case 2	Case 3	Case 1	Case 2	Case 3
$M(^{11}\text{B})$	2.94	2.92	3.13	6.77	6.58	7.66
$M(^{11}\text{C})$	2.80	2.71	3.20	9.33	8.91	9.64
$M(^{11}\text{B}+^{11}\text{C})$	5.74	5.62	6.33	16.10	15.49	17.29

T. Yoshida

15 M_\odot



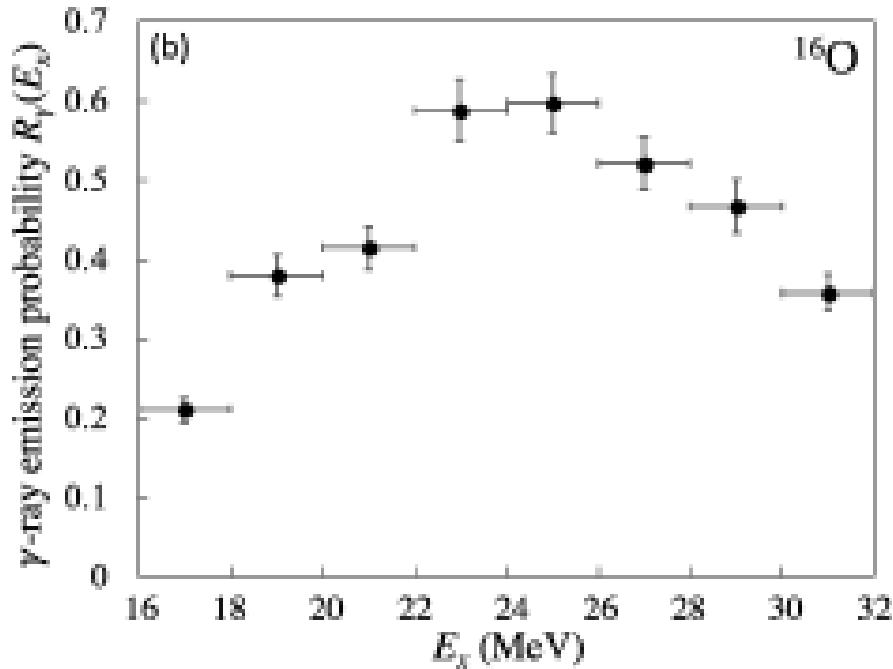
20 M_\odot



Case1: previous branches used in ^{16}O (γ , n, p, α -emissions) and HW92 cross sections

Case2: previous branches, and new cross sections

Case3: multi-particle branches and new cross sections



Sakuda et al.,
Proc. OMEG15 Conference

Reaction	FD	mMB	NK1	NK2	Beacom-Vogel [8] FD
$p(\bar{\nu}_e, e^+)n$	6000	6000	3260	17300	8300
NC $^{16}\text{O}(\nu, \nu')^{16}\text{O}'(E_\gamma > 5 \text{ MeV})$	456	9	57	940	710
Cf. CC $^{16}\text{O}(\nu_e, e^-) + ^{16}\text{O}(\bar{\nu}_e, e^+)(E_e > 5 \text{ MeV})$ [26]	-	-	77	3831	-
ne elastic scattering [26]	-	-	140	514	-

Table III. Expected number of neutrino events from a core-collapse supernova at 10 kpc to be detected at Super-K (32.8kton).