Benchmarking aspects of weak interaction physics using beta decay and two-nucleon transfer experiments

Smarajit Triambak





UNIVERSITY of the WESTERN CAPE

$$\mathcal{L}_{\rm EW}^{q} = -eJ_{\rm em}^{\mu} - \frac{g}{2\sqrt{2}} \left\{ W_{\mu}^{+} J_{W}^{\mu} + W_{\mu}^{-} J_{W}^{\mu\dagger} \right\} - \frac{g}{2\cos\theta_{W}} Z_{\mu} J_{Z}^{\mu}$$

Key assumption

- Only left-handed chiral fields in both the charged and neutral current sectors
- Left-right symmetric extensions to the Standard Model
 - Pati and Salam (1974)
 - Senjanović and Mohapatra (1975)
 - Shaban and Stirling (1992)
 - Herczeg (2001)

Right-handed weak Interactions

- There exists a direct connection between right-handed weak currents, the see-saw mechanism and $0\nu\beta\beta$ decays
 - Bilenky, Faessler, Potzel and Šimkovic (2011)
 - Rodejohaan (2011)
 - Štefánik, Dvornický, Šimkovic, and Vogel (2015)
 - Deppisch, Hati, Patra, Pritimita and Sarkar (2018)

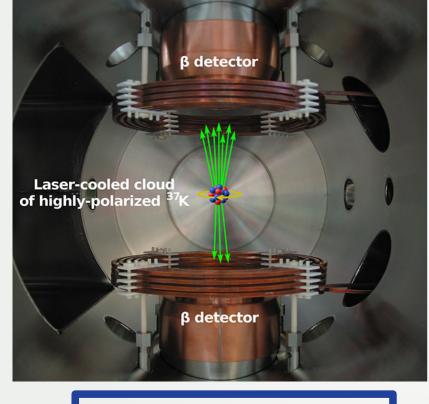
Probing RHCs with atomic nuclei

$$d\Gamma \propto (E_0 - E)^2 p E \left\{ f_1(E) + f_4(E) \frac{\langle \boldsymbol{J} \rangle}{J} \cdot \frac{\boldsymbol{p}}{E} + \cdots \right\} dE d\Omega_e$$

Holstein and Treiman, Phys. Rev. C 3, 1921 (1971)

$$f_1 \rightarrow f_1 + x^2 a^2 + y^2 c^2,$$

 $f_4 \rightarrow f_4 - \frac{y^2 c^2}{J+1} - 2\sqrt{\frac{J}{J+1}} xyac$



TRINAT at TRIUMF (picture from phys.org) RHC physics $\implies x \simeq \delta - \zeta; \ y \simeq \delta + \zeta$

Bég, Budny, Mohapatra, and Sirlin, Phys. Rev. Lett. 38, 1252 (1977)

Isotope	j = j'	$f_{V}t(s)$	Y_0	A_0	εςς
³ H	1/2	1141.3(21)	0.4778(6)	-0.9919(1)	-1.095
¹¹ C	3/2	3972.0(141)	1.3532(69)	-0.5992(2)	0.472
¹³ N	1/2	4694.5(193)	1.801(16)	-0.3330(2)	0.943
¹⁵ O	1/2	4407.4(80)	-1.5944(53)	0.7080(17)	~0.532
¹⁷ F	5/2	2314.0(69)	-0.7776(19)	0.9972(2)	-0.357
¹⁹ Ne	1/2	1725.1(44)	0.6250(11)	-0.0396(9)	24.23
²¹ Na	3/2	4106.4(116)	-1.4206(62)	0.8617(18)	-0.308
²³ Mg	3/2	4754.7(179)	1.852(16)	-0.5574(18)	0.324
²⁵ Al	5/2	3743.1(76)	-1.2493(34)	0.9362(8)	-0.238
²⁷ Si	5/2	4172.2(131)	1.4557(72)	-0.6973(8)	0.263
²⁹ P	1/2	4869.1(181)	-1.956(18)	0.6060(45)	-0.456
³¹ S	1/2	4860.9(274)	1.949(27)	-0.3301(7)	0.842
33Cl	3/2	5668.6(127)	3.463(52)	-0.3821(44)	0.161
³⁵ Ar	3/2	5717.7(142)	3.674(68)	0.4201(72)	-0.131
³⁷ K	3/2	4591.3(302)	1.721(23)	-0.5720(24)	0.353
³⁹ Ca	3/2	4347.3(111)	-1.5567(69)	0.8213(20)	-0.285
41Sc	7/2	2873.4(84)	-0.9377(26)	0.9983(2)	-0.237

B. Fenker et al, Phys. Rev. Lett 120 062502 (2018)

Naviliat-Cuncic, Girard, Deutsch and Severijns, J. Phys. G: Nucl. Part. Phys. 17 919 (1991)

Probing RHCs with ¹⁹Ne β decay

$$d\Gamma \propto (E_0 - E)^2 p E \left\{ f_1(E) + f_4(E) \frac{\langle J \rangle}{J} \cdot \frac{p}{E} + \cdots \right\} dE d\Omega$$

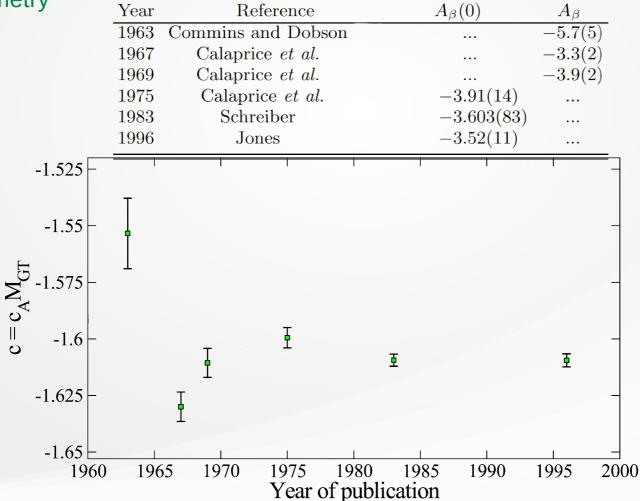
$$A_{\beta}(E) = \left[\frac{f_4(E)}{f_1(E)}\right]$$

 $f_4 \to f_4 - \frac{y^2 c^2}{J+1} - 2\sqrt{\frac{J}{J+1}}xyac$

 $f_1 \to f_1 + x^2 a^2 + y^2 c^2$,

RHC physics $\implies x \simeq \delta - \zeta; y \simeq \delta + \zeta$

Beta asymmetry



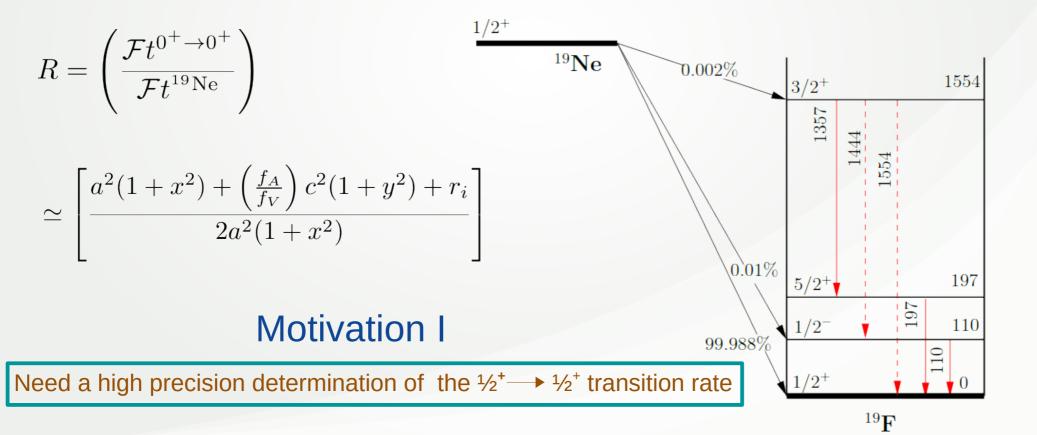
Probing RHCs with atomic nuclei

$$d\Gamma \propto (E_0 - E)^2 p E \left\{ f_1(E) + f_4(E) \frac{\langle J \rangle}{J} \cdot \frac{p}{E} + \cdots \right\} dE d\Omega_e \qquad f_1 \to f_1 + x^2 a^2 + y^2 c^2,$$

$$f_4 \to f_4 - \frac{y^2 c^2}{J + 1} - 2\sqrt{\frac{J}{J + 1}} xyac$$

$$\downarrow A_\beta(E) = \left[\frac{f_4(E)}{f_1(E)} \right] \qquad \text{RHC physics} \qquad x \simeq \delta - \zeta; \ y \simeq \delta + \zeta$$

Beta asymmetry

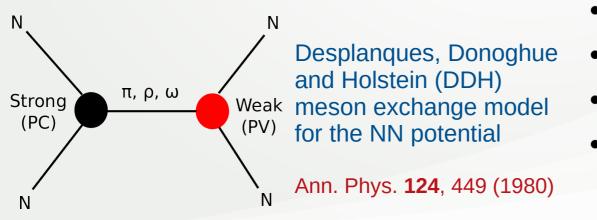


$$\mathcal{L}_{\rm EW}^{q} = -eJ_{\rm em}^{\mu} - \frac{g}{2\sqrt{2}} \left\{ W_{\mu}^{+} J_{W}^{\mu} + W_{\mu}^{-} J_{W}^{\mu\dagger} \right\} - \frac{g}{2\cos\theta_{W}} Z_{\mu} J_{Z}^{\mu}$$

Key assumption

- Only left-handed chiral fields in both the charged and neutral current sectors
- Flavor-conserving quark-quark weak interactions least understood





Experiment

- $A_L(\vec{p}, p)$: Bonn, Los Alamos, PSI, TRIUMF
- $A_L(\vec{p}, \alpha)$: PSI
- $P_{\gamma}(n,p)$: Gatchina
- $A_{\gamma}(\vec{n}, p)$: Los Alamos, Grenoble

$$\mathcal{L}_{\rm EW}^{q} = -eJ_{\rm em}^{\mu} - \frac{g}{2\sqrt{2}} \left\{ W_{\mu}^{+} J_{W}^{\mu} + W_{\mu}^{-} J_{W}^{\mu\dagger} \right\} - \frac{g}{2\cos\theta_{W}} Z_{\mu} J_{Z}^{\mu}$$

Key assumption

- Only left-handed chiral fields in both the charged and neutral current sectors
- Flavor-conserving quark-quark weak interactions least understood

Theory

- χ PT : Chiral perturbation theory
- EFT (র): Pionless EFT
- 1/Nc Expansion
- Lattice QCD

Gardner, Haxton and Holstein, Ann. Rev. Nucl. Part. Sci. **67**, 69 (2017),

Experiment

- $A_L(\vec{p}, p)$: Bonn, Los Alamos, PSI, TRIUMF
- $A_L(\vec{p}, \alpha)$: PSI
- $P_{\gamma}(n,p)$: Gatchina
- $A_{\gamma}(\vec{n}, p)$: Los Alamos, Grenoble

NPDGamma Expt

D. Blyth et al., PRL 121, 242002 (2018)

$$\mathcal{L}_{\rm EW}^{q} = -eJ_{\rm em}^{\mu} - \frac{g}{2\sqrt{2}} \left\{ W_{\mu}^{+} J_{W}^{\mu} + W_{\mu}^{-} J_{W}^{\mu\dagger} \right\} - \frac{g}{2\cos\theta_{W}} Z_{\mu} J_{Z}^{\mu}$$

Key assumption

- Only left-handed chiral fields in both the charged and neutral current sectors
- Flavor-conserving quark-quark weak interactions least understood
- Parity violation filter to isolate weak interaction effects

Theory

- χ PT : Chiral perturbation theory
- EFT (𝖈): Pionless EFT
- 1/Nc Expansion
- Lattice QCD

 $H_{weak}/H_{strong} \sim 10^{-7}$

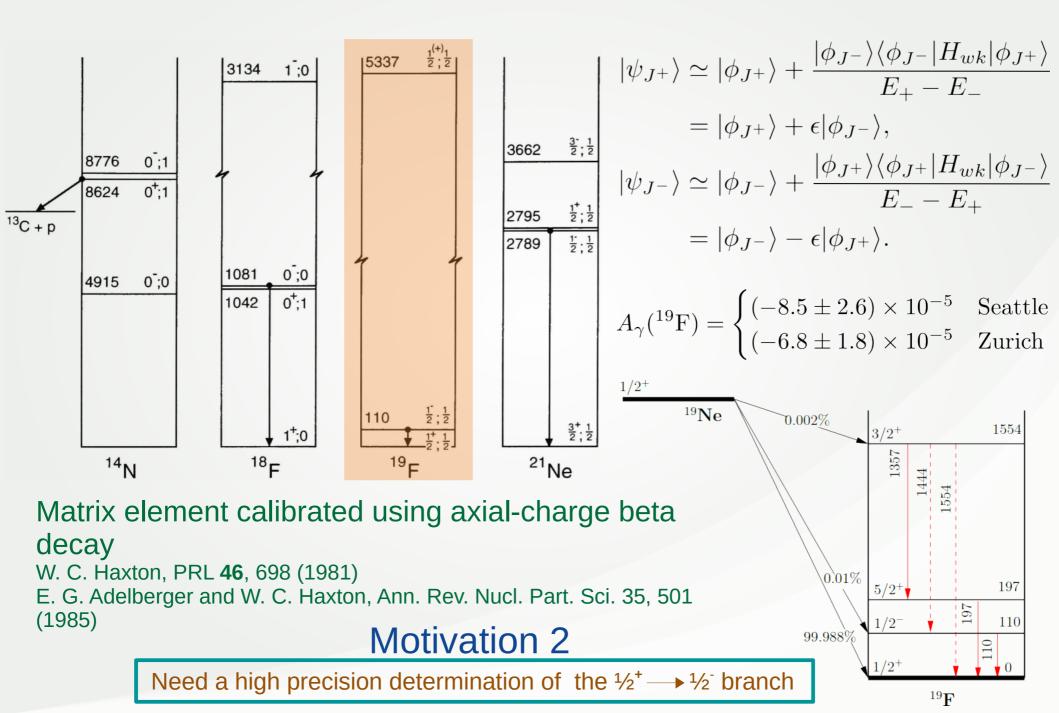
Experiment

- $A_L(\vec{p}, p)$: Bonn, Los Alamos, PSI, TRIUMF
- $A_L(\vec{p}, \alpha)$: PSI
- $P_{\gamma}(n,p)$: Gatchina
- $A_{\gamma}(\vec{n}, p)$: Los Alamos, Grenoble

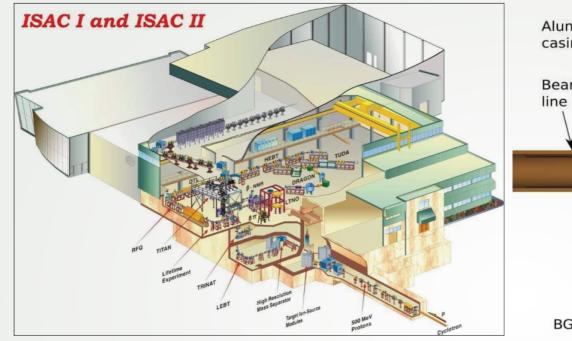
NPDGamma Expt

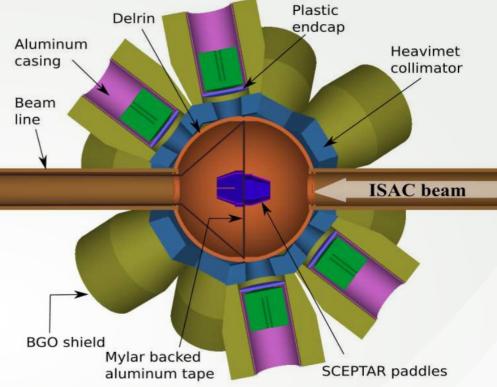
D. Blyth et al., PRL 121, 242002 (2018)

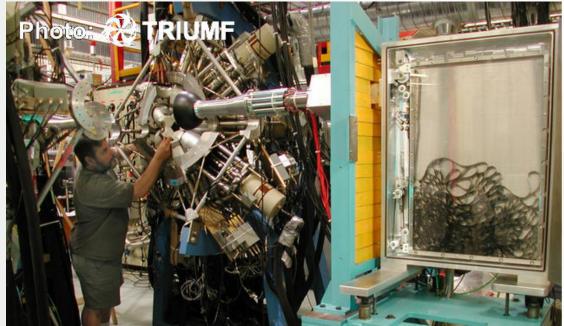
Parity doublets in light nuclei as amplifiers



Experimental details (8π at TRIUMF)

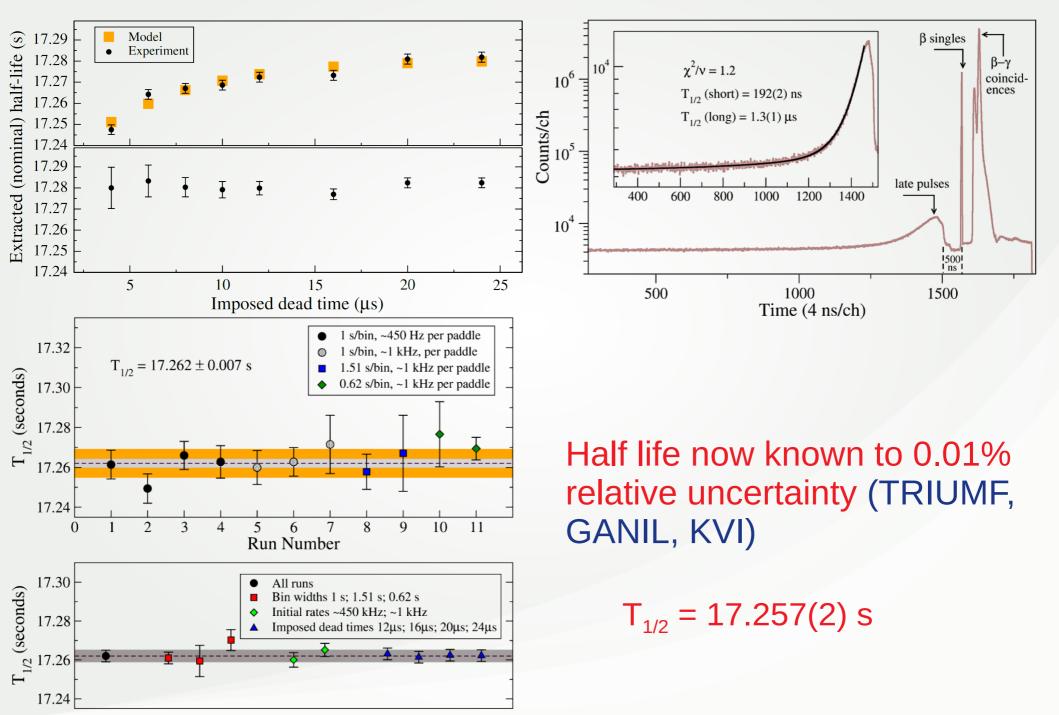




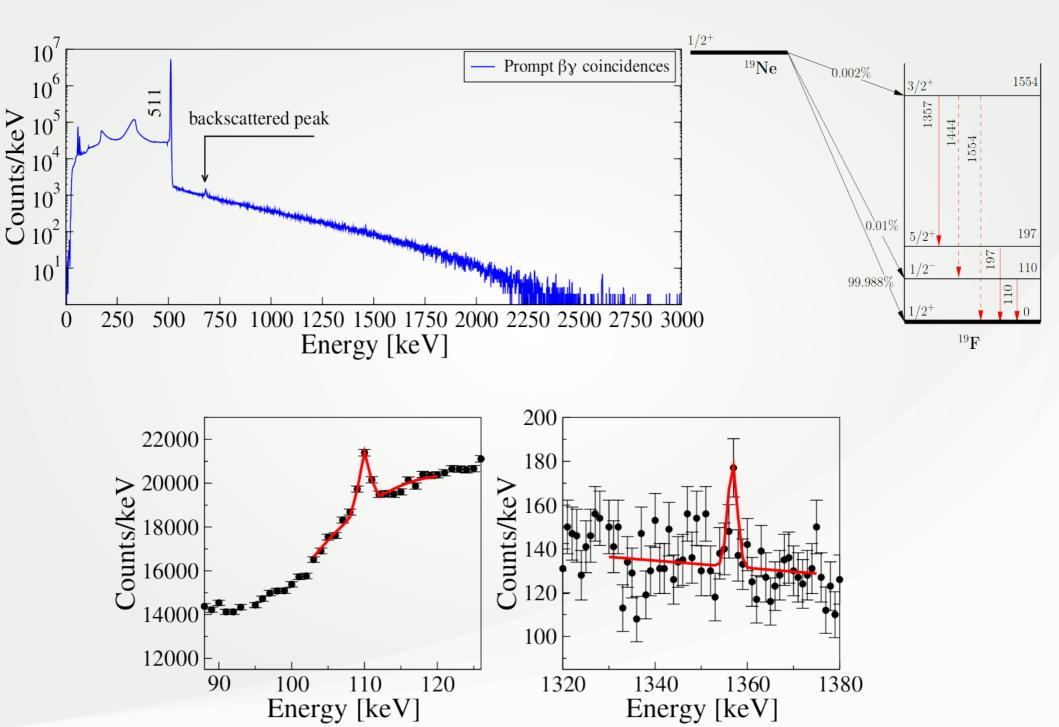




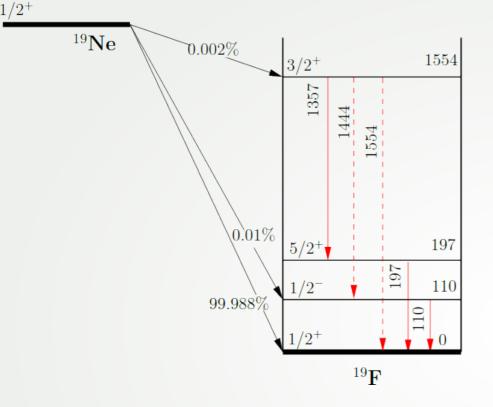
Half-life determination



Branching ratio determination



Branching ratio determination



$$\frac{N_{ij}^{\beta\gamma}}{N_{\beta}} = \frac{1}{\sum_{m} B_{m} \eta_{m}} \left[B_{i} \eta_{i} + \sum_{k>i} B_{k} \eta_{k} \gamma_{ki} \right] \gamma_{ij} \epsilon_{ij}$$
$$B_{1} \simeq k_{1} \left(\frac{N_{10}^{\beta\gamma}}{N_{\beta} \cdot \epsilon_{10}} \right)$$

Source	Correction	$\frac{\Delta B_1}{B_1}$ (%)
Coincidence summing	1.0089(6)	0.06
Random coincidences	0.961(9)	0.94
Pile up	1.00324(1)	0.001
Dead time	1.00577(6)	0.006
Q_{β} value dependence on β efficiency	1.000(2)	0.20
$N_{10}^{\beta\gamma}/N_{\beta}$ ratio		6.4
HPGe efficiency (ϵ_{10})		2.4

	Measured β branch (%)		
Transition	Previou	us work	This work
$1/2^+ \to 3/2^+$	$0.0021(3)^a$	$0.0023(3)^b$	0.0017(5)
$1/2^+ \to 1/2^-$	$0.012(2)^c$	$0.011(9)^{d}$	0.0099(7)

 a D.E. Alburger

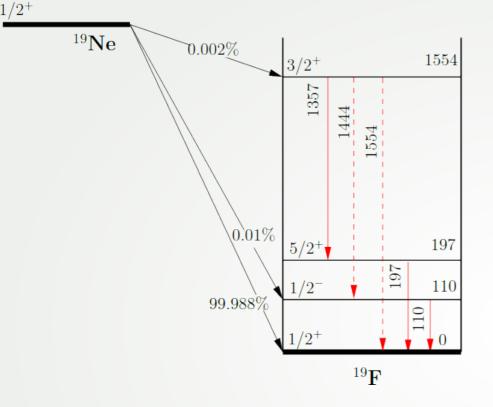
^b E.G. Adelberger *et al.*

 c E.G. Adelberger $et\ al.$

^d E. R. J. Saettler *et al.*

- First-forbidden β decay branch now known with three times better precision
- Superallowed ½ → ½ branch is now 99.9878(7)%

Branching ratio determination



$$\frac{N_{ij}^{\beta\gamma}}{N_{\beta}} = \frac{1}{\sum_{m} B_{m} \eta_{m}} \left[B_{i} \eta_{i} + \sum_{k>i} B_{k} \eta_{k} \gamma_{ki} \right] \gamma_{ij} \epsilon_{ij}$$
$$B_{1} \simeq k_{1} \left(\frac{N_{10}^{\beta\gamma}}{N_{\beta} \cdot \epsilon_{10}} \right)$$

Source	Correction	$\frac{\Delta B_1}{B_1}$ (%)
Coincidence summing	1.0089(6)	0.06
Random coincidences	0.961(9)	0.94
Pile up	1.00324(1)	0.001
Dead time	1.00577(6)	0.006
Q_{β} value dependence on β efficiency	1.000(2)	0.20
$N_{10}^{\beta\gamma}/N_{\beta}$ ratio		6.4
HPGe efficiency (ϵ_{10})		2.4

	Measured β branch (%)			
Transition	Previor	us work	This work	
$1/2^+ \to 3/2^+$	$0.0021(3)^a$	$0.0023(3)^b$	0.0017(5)	
$1/2^+ \to 1/2^-$	$0.012(2)^c$	$0.011(9)^d$	0.0099(7)	

 \overline{a} D.E. Alburger

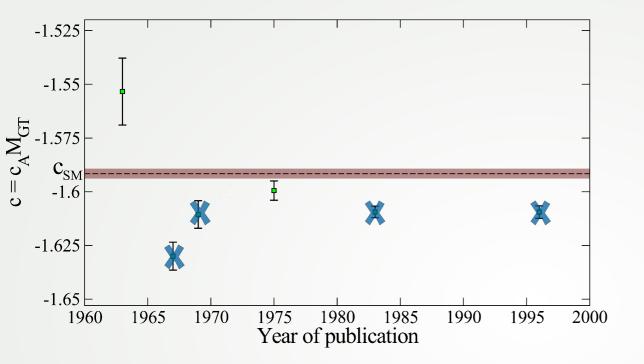
^b E.G. Adelberger *et al.*

 c E.G. Adelberger $et\ al.$

^d E. R. J. Saettler *et al.*

- First-forbidden β decay branch now known with three times better precision
- Precision in *Ft* value
 improved by a factor of ~3.5

Results



 \bullet Violates CKM unitarity by more than 5σ

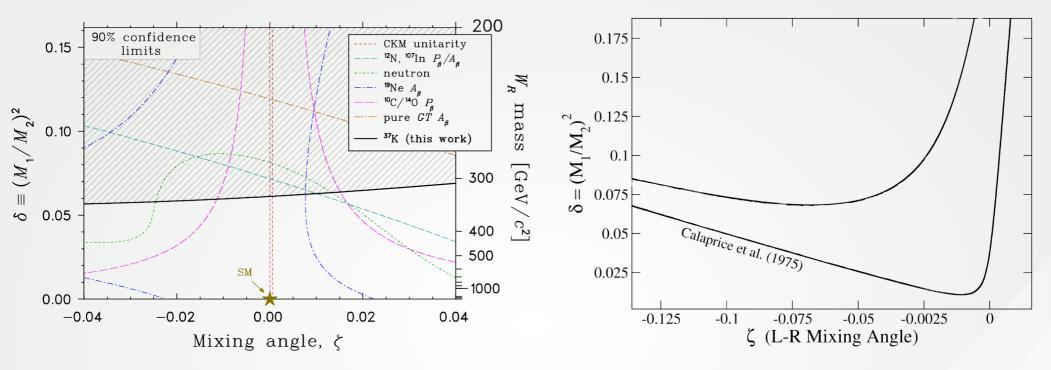
 Violates CKM unitarity at the 99.6% CL

$A_{\beta}^{\text{expt}} =$	-0.0391	± 0.0014
-----------------------------	---------	--------------

Year	Reference	$A_eta(0)$	A_{eta}
1963	Commins and Dobson		-5.7(5)
1967	-Calaprice <i>et al.</i>		-3.3(2)
1969	Calaprice et al.		-3.9(2)
1975	Calaprice <i>et al.</i>	-3.91(14)	•••
1983	Schreiber	-3.603(83)	
1996	Jones		
		()	

 $A_{\beta}^{\rm SM} = -0.0415 \pm 0.0006$

Results and conclusions



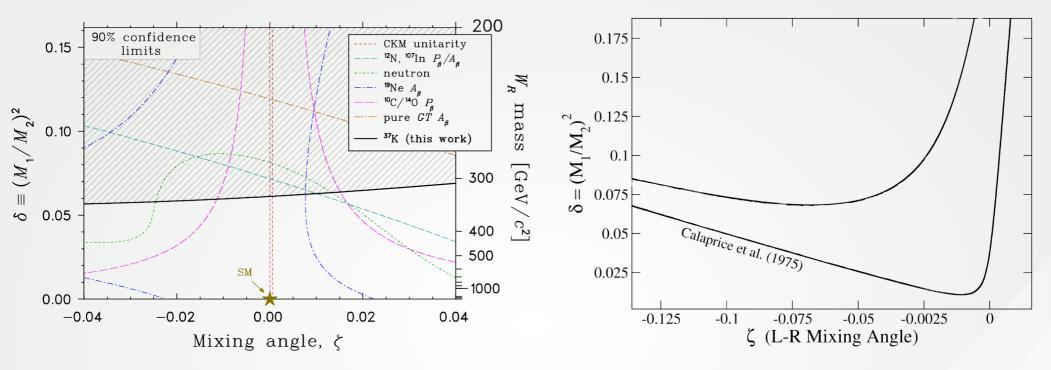
B. Fenker et al, Phys. Rev. Lett **120**, 062502 (2018)

This work + 1975 measurement of A $_{\!\beta}$ (Best fit disagrees with the SM by only 1.7 $\!\sigma$)

- One of the most precisely measured $\mathcal{F}t$ values for T = ½ mirror β decays is from ¹⁹Ne: $\mathcal{F}t = 1721.44(92)$ s
- First-forbidden decay rate is found to be ~ 10 times lower than shell model calculations that used PNC nucleon-meson couplings recommended by Desplanques, Donoghue and Holstein

B. M. Rebeiro et al, Phys. Rev. C 99, 065502 (2019)

Results and conclusions



B. Fenker et al, Phys. Rev. Lett **120**, 062502 (2018)

This work + 1975 measurement of A $_{\beta}$ (Best fit disagrees with the SM by only 1.7 σ)

- One of the most precisely measured $\mathcal{F}t$ values for $T = \frac{1}{2}$ mirror β decays is from ¹⁹Ne: $\mathcal{F}t = 1721.44(92)$ s
- First-forbidden decay rate is found to be ~ 10 times lower than shell model calculations that used PNC nucleon-meson couplings recommended by Desplanques, Donoghue and Holstein

Remeasurements of the asymmetry measurements are welcome!

Revisiting weak interaction symmetries

$$\mathcal{L}_{\rm EW}^{q} = -eJ_{\rm em}^{\mu} - \frac{g}{2\sqrt{2}} \left\{ W_{\mu}^{+} J_{W}^{\mu} + W_{\mu}^{-} J_{W}^{\mu\dagger} \right\} - \frac{g}{2\cos\theta_{W}} Z_{\mu} J_{Z}^{\mu}$$

Key assumption

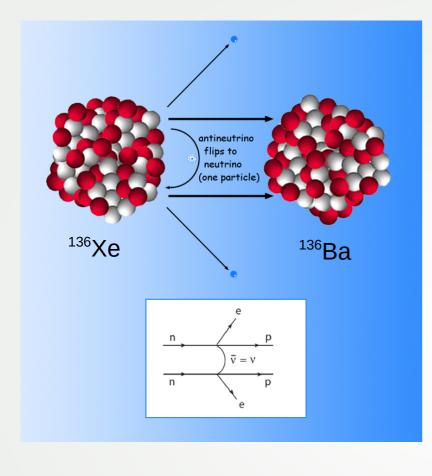
- Only left-handed chiral fields in both the charged and neutral current sectors
- Left-right symmetric extensions to the Standard Model



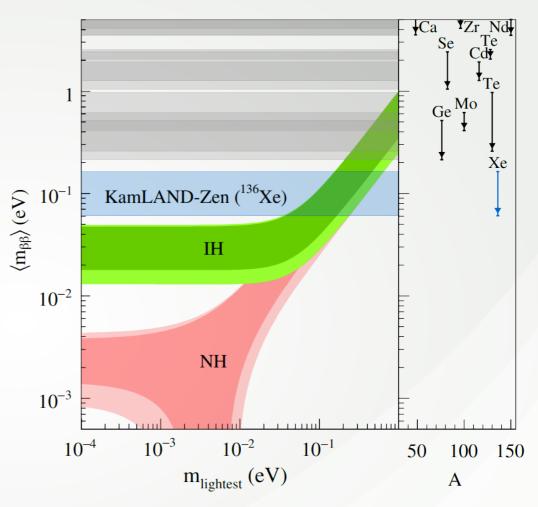
• There exists a direct connection between right-handed weak currents, the see-saw mechanism and $0\nu\beta\beta$ decays

- Bilenky, Faessler, Potzel and Šimkovic (2011)
- Rodejohaan (2011)
- Štefánik, Dvornický, Šimkovic, and Vogel (2015)
- Deppisch, Hati, Patra, Pritimita and Sarkar (2018)

The $0\nu\beta\beta$ decay of ¹³⁶Xe

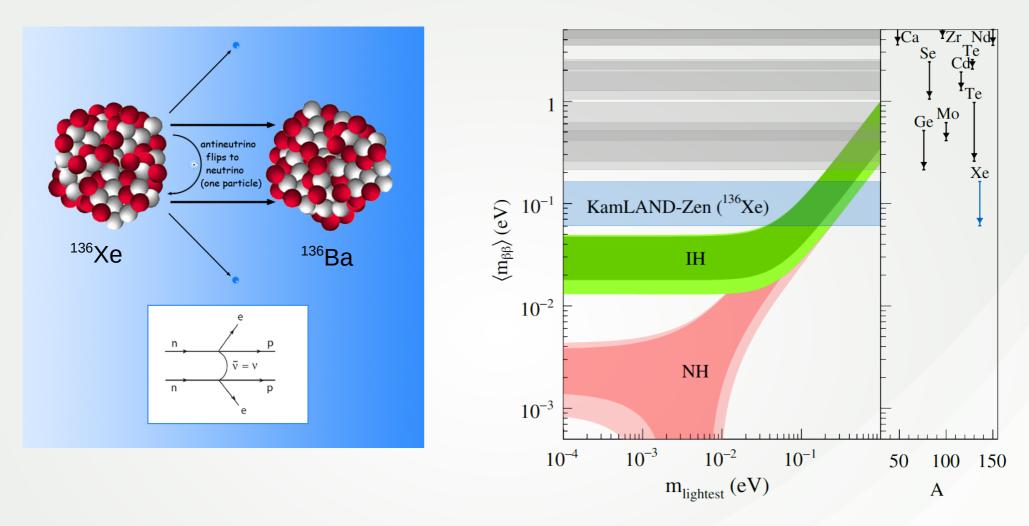


$$T_{1/2}^{0\nu}]^{-1} = G^{0\nu}(Q,Z) |M^{0\nu}|^2 \left(\frac{\langle m_{\beta\beta} \rangle}{m_e}\right)^2$$



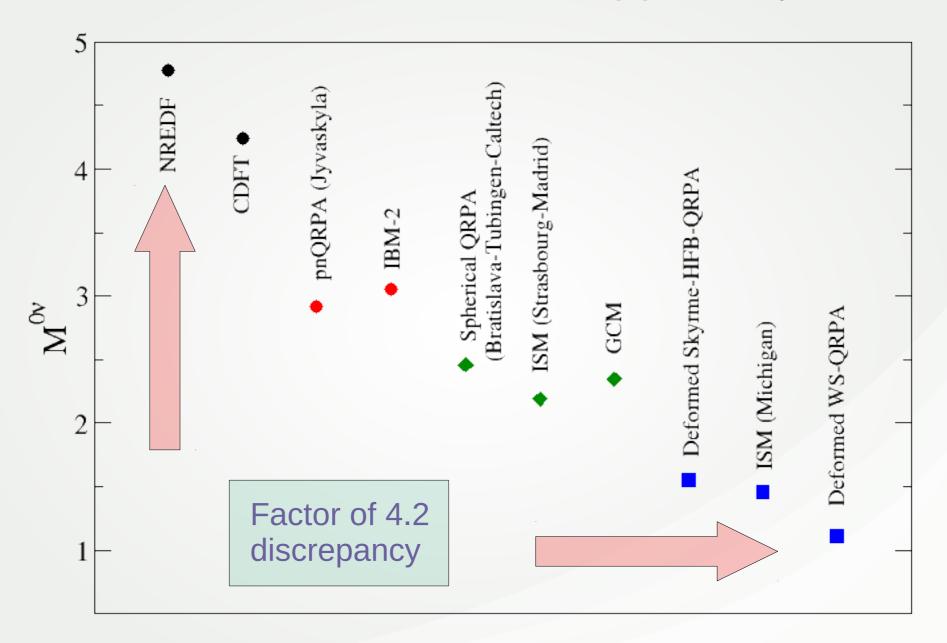
A. Gando et al., PRL 117, 082503 (2016)

The $0\nu\beta\beta$ decay of ¹³⁶Xe

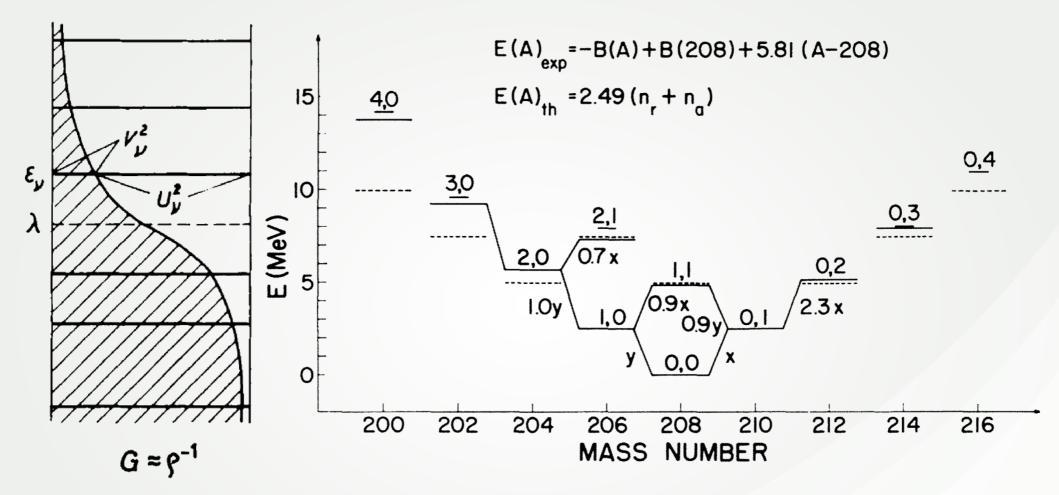


- ¹³⁶Xe $\beta\beta$ decay experiments have certain advantages...
- ¹³⁶Xe has singly closed shell (N = 82) nearly spherical

The NME for ¹³⁶Xe $0\nu\beta\beta$ decay



Nucleon pairing and the BCS approximation

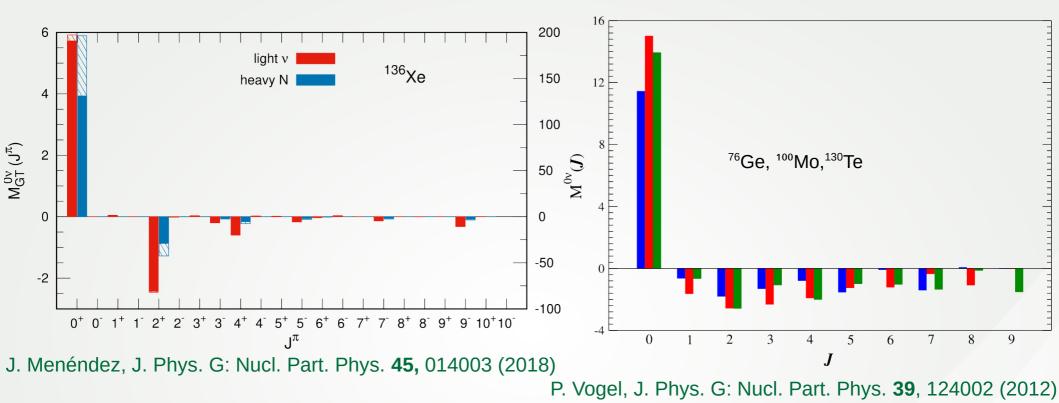


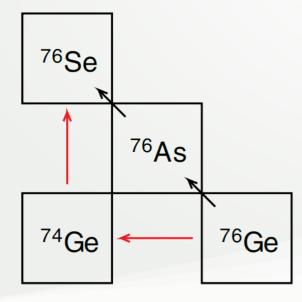
Nathan and Nilsson, Alpha, beta and gamma-ray spectroscopy (Ed. Kai Siegbahn)

Broglia, Hansen and Riedel, Advances in Nuclear Physics: Vol 6

Two-nucleon transfer reactions such as (p,t), (t,p), (3He,n) are useful probes **Strong population** of the ground states in the superfluid limit

Anatomy of $0\nu\beta\beta$ decay NMEs





$$M^{0\nu}(E_x, J_m) = \sum_{E_m < E_x, J_m} V(f, i, m)$$

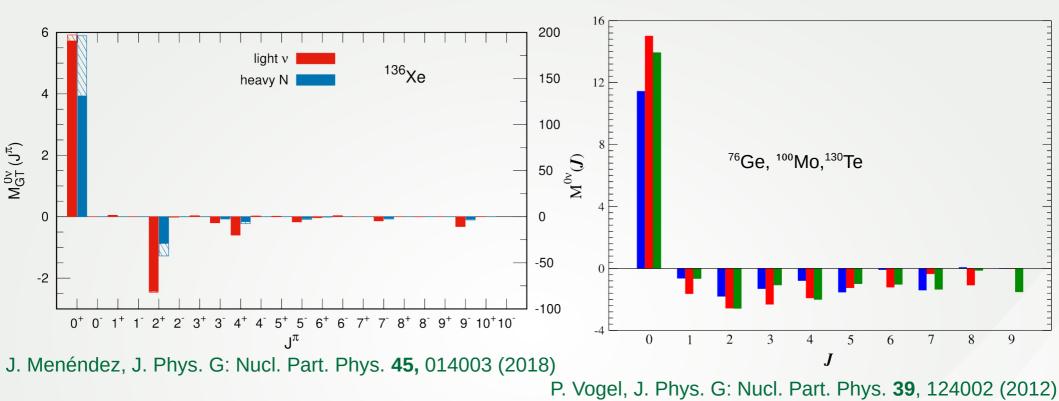
where

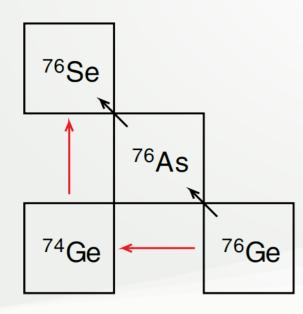
$$V(f, i, m) = \sum_{k_{\alpha} \le k_{\beta}, k_{\gamma} \le k_{\delta}} \langle k_{\alpha}, k_{\beta}, J_{m} | V | k_{\gamma}, k_{\delta}, J_{m} \rangle$$

× TNA
$$(f, m, k_{\alpha}, k_{\beta}, J_0)$$
TNA $(i, m, k_{\gamma}, k_{\delta}, J_0)$

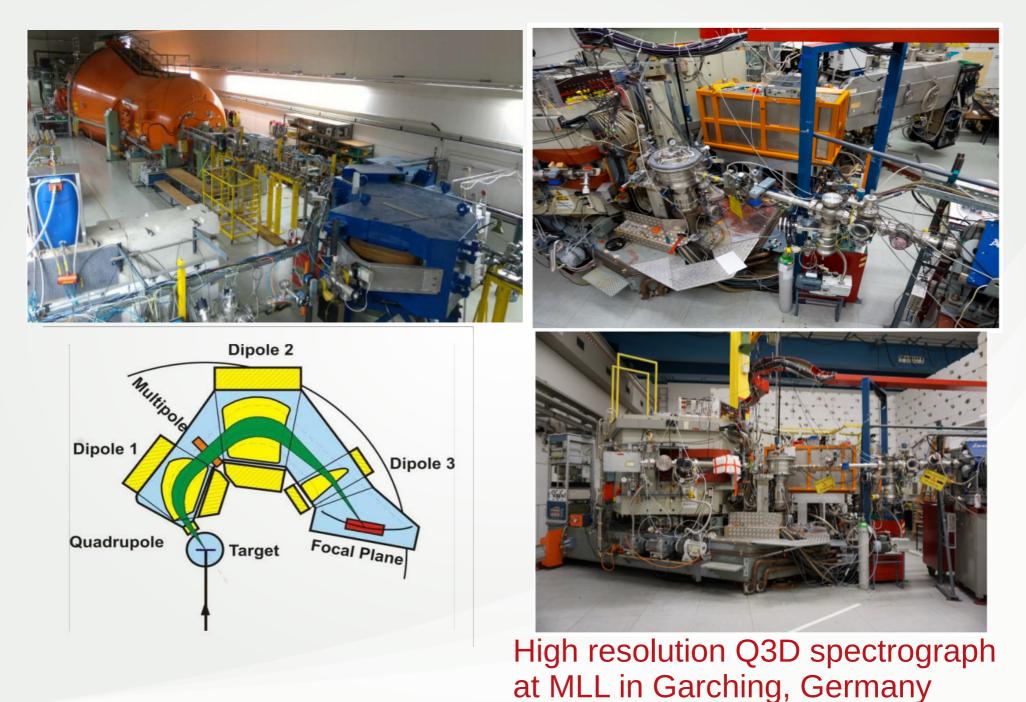
B. A. Brown, M. Horoi and R. A. Senkov, Phys. Rev. Lett. **113**, 262501 (2014)

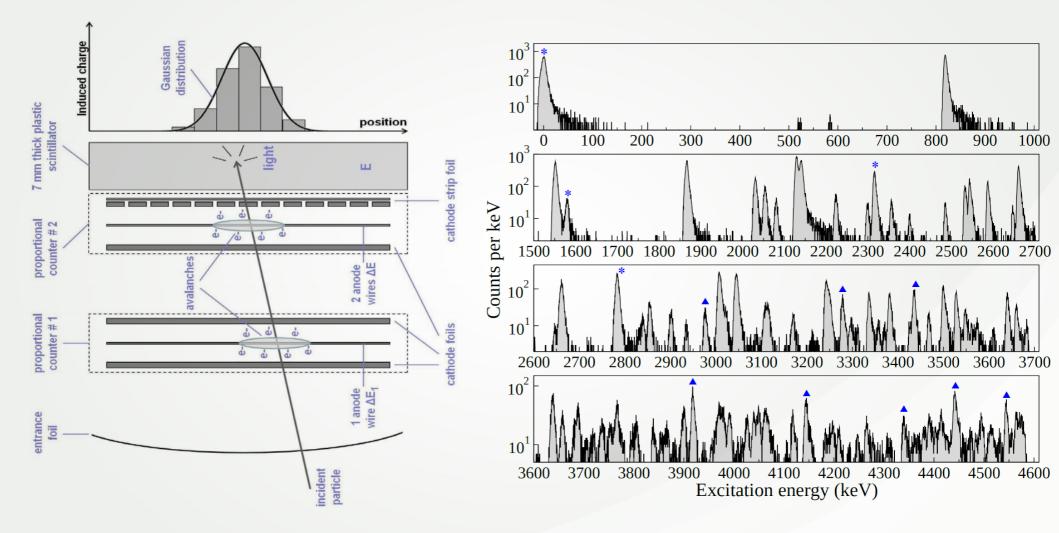
Anatomy of $0\nu\beta\beta$ decay NMEs

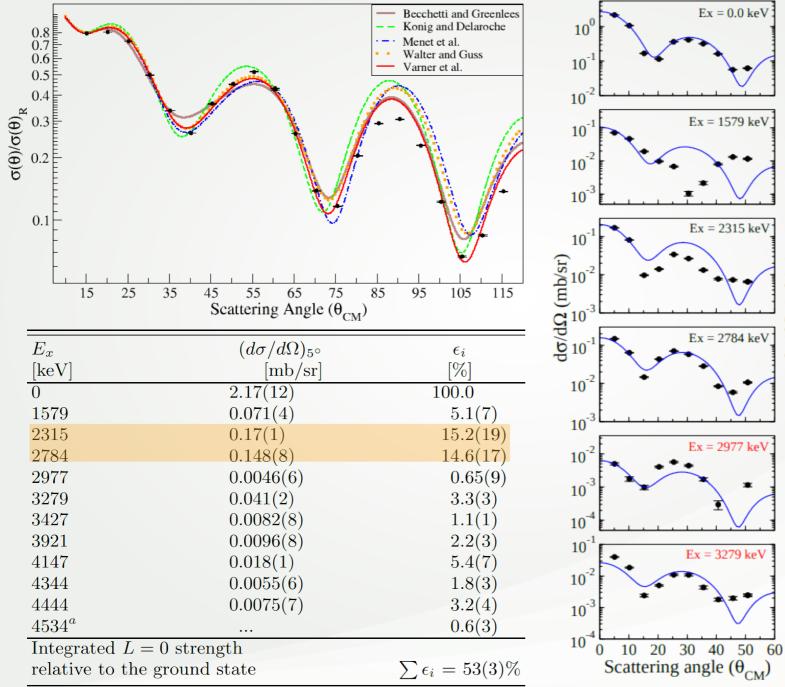


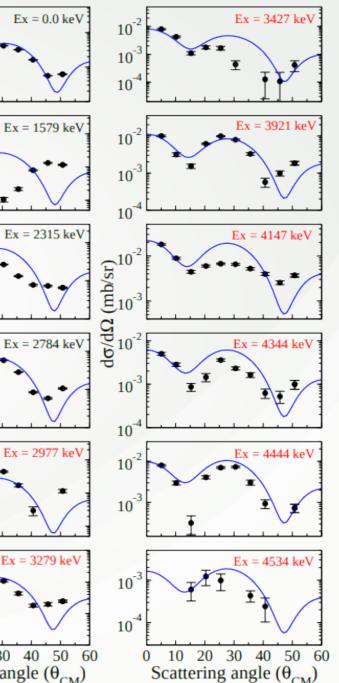


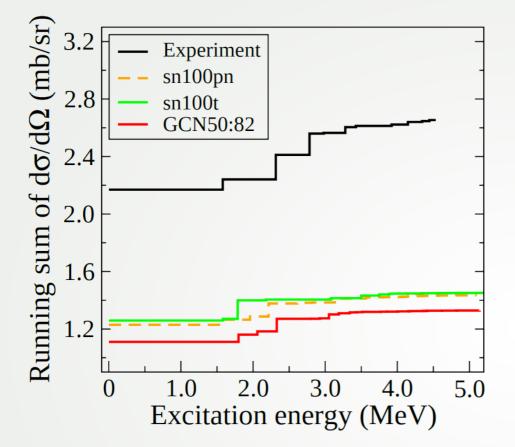
- The NME is dominated by the J⁺ = 0⁺ ground state in ⁷⁴Ge
- There are cancellations from intermediate states with J > 0, dominated by the 2⁺ contributions
- Relates to pair-transfer properties of the ground states











- Used the NuShellX code with the five-orbital $(0g_{7/2}, 1d_{5/2}, 1d_{3/2}, 2s_{1/2}, 0h_{11/2})$ valence space to get the wavefunctions for ¹³⁸Ba and first 50 0⁺ states in ¹³⁶Ba
- NuShellX > two-neutron transfer amplitudes (TNA) > coherent sum of both direct and sequential two-step transfer

LEVELS OF ⁵²Fe STUDIED WITH THE (p, t) REACTION [†]

P. DECOWSKI ^{††}, W. BENENSON, B. A. BROWN and H. NANN

Cyclotron Laboratory and Physics Department, Michigan State University, East Lansing, Michigan 48824

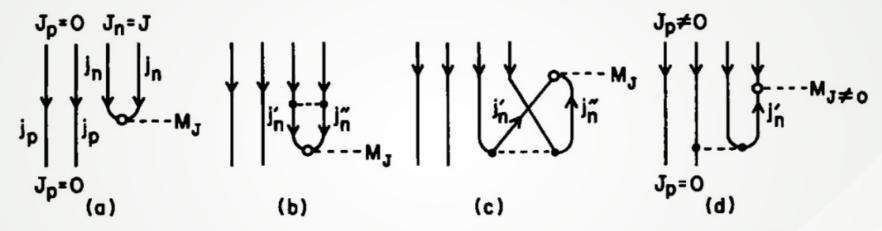
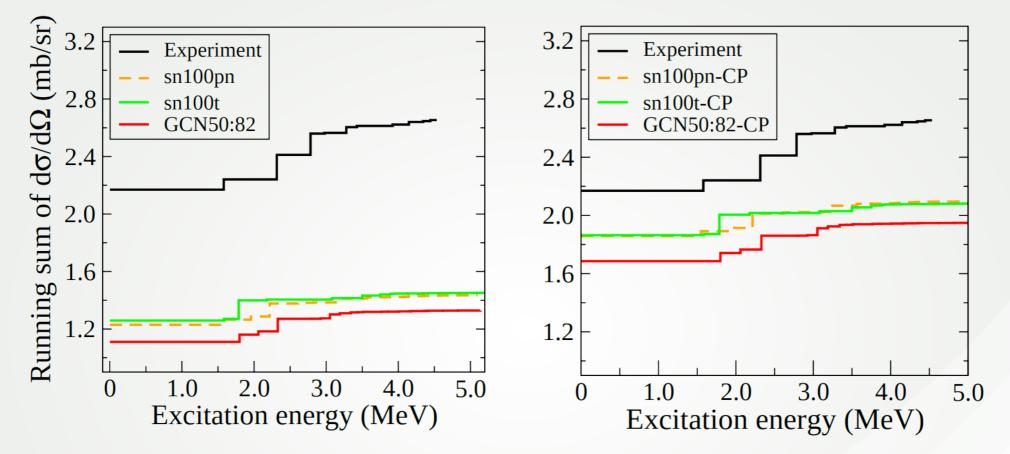


Fig. 8. Diagrams of the ⁵⁴Fe(p, t)⁵²Fe reaction assuming, (a) the zeroth-order process with ⁵⁴Fe in a pure $(j_p = 1f_{7/2})_{J_p=0}^{-2}(j_n = 1f_{7/2})_{J_n=J}^{-2}$ configuration, (b) a first-order process which includes two-hole admixtures in ⁵²Fe, and (c) a first-order process which includes two-hole admixtures in ⁵²Fe, and (c) a first-order process which includes two-hole admixtures in ⁵⁴Fe. Diagram (d) shows a first-order process due to three-hole one-particle admixtures with $(j_p = 1f_{7/2})_{J_n\neq 0}^{-2}$ in ⁵⁴Fe.

Nucl. Phys. A302, 186 (1978)

Coherent contributions from orbitals outside the valence space enhance the L = 0 (p,t) cross section



 We obtain better agreement after incorporating these ladder-diagram corrections to the TNA (assumed the scattering of pairs of neutrons to twenty three orbitals beyond the model space)

• $^{136}Xe \rightarrow ^{134}Xe$ is very similar to $^{138}Ba \rightarrow ^{136}Ba$ (both are N = 82 \rightarrow N = 80)

Results

QRPA: Šimkovic, Rodin, Faessler and Vogel (2013) – 23 orbitals

 $M^{0v}(GT) = 2.18$

• QRPA: Fang (this work) – 28 orbitals

 $M^{0v}(GT) = M(J = 0) + M (J > 0) = 9.63 - 7.65 = 1.98$

ISM: E. Caurier, J. Menéndez, F. Nowacki, and A. Poves (2008)

 $M^{0v}(GT) = M(J = 0) + M (J > 0) = 5.72 - 3.95 = 1.77$

- ISM: Horoi (this work) sn100t + five orbitals: PRL 110, 222502 (2013)
 M^{0v}(GT) = M(J = 0) + M (J > 0) = 5.67 3.73 = 1.94
- ISM: Brown (this work) $M_{GT}(J = 0; G.S) = 5.72$ $M_{GT}(J = 0; G.S) = 9.04$ Ratio = 1.58
- Using this ratio, we get a corrected ISM value $M_{GT} (J = 0) = 8.96$ Based on comparison with our experimental data

Conclusions

- Our ¹³⁸Ba(p,t) work indicates a large breakdown of the BCS pairing approximation for neutrons in ¹³⁶Ba
- A similar analysis of ¹³⁶Ba(p,t) data shows that this persists in ¹³⁴Ba: See Jespere Ondze's poster
- Quite likely due to dissimilar deformations in initial and final nuclei shape-transitional Ba nuclei with N \leq 82
- Our ISM analysis (after taking into account core-polarization corrections to the TNA) results in a value of M_{GT} (J = 0) that agrees with a large model-space QRPA calculation
- We recommend improved calculations of this part of NME as well as the canceling M_{GT} (J > 0) terms, taking into account physics contributions from beyond the model space.

PHYSICAL REVIEW C 87, 064315 (2013)

Effective double- β -decay operator for ⁷⁶Ge and ⁸²Se

Jason D. Holt*

Institut für Kernphysik, Technische Universität Darmstadt, 64289 Darmstadt, Germany, ExtreMe Matter Institute (EMMI), GSI Helmholtzzentrum für Schwerionenforschung GmbH, 64291 Darmstadt, Germany, Department of Physics and Astronomy, University of Tennessee, Knoxville, Tennessee 37996, USA, and Physics Division, Oak Ridge National Laboratory, Post Office Box 2008, Oak Ridge, Tennessee 37831, USA

Jonathan Engel[†]

Department of Physics and Astronomy, University of North Carolina, Chapel Hill, North Carolina, 27516-3255, USA (Received 16 April 2013; published 24 June 2013)

Collaboration

University of the Western Cape: **B. M. Rebeiro**, M. Kamil, J. Ondze, J. Mukwevho, J. N. Orce

Michigan State University: B. A. Brown, C. Sumithrarachchi

Central Michigan University: M. Horoi

Institute of Modern Physics: D.L. Fang

University of Guelph: P. E. Garrett, C. E. Svensson, V. Bildstein, C. Burbadge, A. Radich, R. Dunlop, A. Diaz Varela, P. Finlay

TU, Munich: T. Faestermann

LMU, Munich: R. Hertenberger, H.F. Wirth

TRIUMF: G. C. Ball, A. Garnsworthy, G. Hackman, R. Churchman, R. Kshetri, H. Al Falou, M. Pearson, S. Sjue, E. Tardiff, R. Kshetri, M. Djongolov

Colorado School of Mines: K. Leach

University of Zululand: P. Z. Mabika, S. Ntshangase

iThemba LABS/Wits: Phil Adsley